Design, modeling and control of inherently compliant actuators with a special consideration on agonist-anthropomorphic configuration

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Design, modeling and control of inherently compliant actuators with a special consideration on agonist-antagonist anthropomorphic configuration

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Abstract

"Design, modeling and control of inherently compliant actuators with a special consideration on agonist- antagonist anthropomorphic configuration"

The research aims at the design, modeling and control of inherently compliant actuators for anthropomorphic systems. The first part of the work focuses on the study of various existing designs and look for the possibility of alternative actuators other than the conventional electric motors. Special attention is given to electroactive polymer based soft actuators which have good potential in future robotic applications. In parallel, a model of the actuator dynamics and the model-based controller (MPC and optimal control) have been synthesized for an anthropomorphic 7 Dofs arm actuated by antagonist-agonist pair of Pneumatic Artificial Muscles (PAMs) at each joint. Such model and controller is then integrated within the software environment developed by the team. Using the PAMs based anthropomorphic manipulator arm and the numerical simulator, tests are done in order to evaluate the potential of this actuator and compare with the human body capabilities.
Acknowledgement

This thesis work was achieved thanks to collaboration and support of various people who I would like to gratefully acknowledge.

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Thanks to Jerome Manhes who contributed in the electronic and hardware development of the project. Working with him was a great pleasure. Because of him, I was able to learn and understand all the aspects (hardware, electronics, data communication) of my experimental set-up. I would also like to acknowledge his work on NI module which is the backbone of our data capturing system on the robot.

I would thank Florent Forget for great support in the software development. Because of him it was possible to test the robot in real time with different control methods. Kevin Gerard has contributed in CAD modeling of the robot which was an necessary input the modelling of my experimental set-up. Working with Kevin and Florent was not only good for my work and my own learning but its also relaxing and fun.

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Introduction

Bio-inspired robotic is one of the emerging research interests among the robotics community. In particular, the human physiology is even more fascinating which makes the human perform various manipulation tasks efficiently and robustly. From the study of the human movement, or the movement of mammals in general, we can understand that the conventional robotics development has taken a path which is quite counter intuitive to our own physiology. The conventional way of designing a robot is to make it as stiff as possible. Also the axes are aligned in such a way to facilitate computational tasks in control design. These constraints of computational power, lack of mature algorithm for modeling and controlling non-linear systems have been the motivation behind the design of robots for decades. But with the rapid evolution in computer technology and the exponential growth in computational power, it is the time now to revisit our approach to design a robot. But before that we must ask ourselves what do we expect from a robot in this modern era. Conceiving a human friendly robot is a great objective. A robot which can perform routine tasks easily and in close collaboration with human. In such environment, collision with the obstacles or with the human is inevitable. Safety and efficiency in task execution executing are important criteria for designing any such robots. Due to this requirements, it seems necessary to have some sort of compliance in the joint or in the structure of the robot body. The search for the most suitable actuator which can make robot efficient and compliant is ongoing. This is the main motivation behind my thesis.

0.1 Motivation

A human friendly robot should be able to imitate some human behaviour. And to make this possible, we may look back to the nature - Our own body. A simple joint model of a mammal can show the musculoskeletal structure with agonist-antagonist muscle bundles spanning the joint. In order to imitate the human behaviour, a robot should have some morphological resemblance with the human body. This motivates the agonist-antagonist actuator design. In such design, actuator can be active compliant, passive compliant or a combination of both. The shift of interest from rigid to compliance is well justified. But before comparing stiff actuators and compliant actuators, a broader definition is necessary. Stiff joint means that once the joint attain its desired position, it maintains this position (within its physical limit) even if disturbed with any external force/torque. At the opposite, a compliant joint is an actuator which allows deviations from its equilibrium position when external forces/torques are applied. Each of them has its own advantage and disadvantage. For example, rigid robots have good precision and therefore are suitable in deterministic environment. But robots are conceived to be used not only inside laboratories but in out-door environment where safety is paramount. Therefore, many desirable
properties of a rigid actuator like stability, repeatability, high payload, force and torque capability and high bandwidth control are sacrificed in a compliant actuator. But inducing the compliance in the actuators have significant advantages which are very crucial for robotics applications in an unstructured unknown environment.

- lower reflected inertia (Due to elastic component, link and drive inertia are decoupled);
- safer interaction with the environment (due to reduced reflected inertia);
- reduced impact on collision (peak forces during the collision are filtered out by the elasticity in robotic joint);
- stability and accuracy in force control (In many case like Serial Elastic actuators, the force control problem is translated to position control since the output force is proportional to the desired and achieved position difference multiplied by effective stiffness);
- energy storage capability (This could be used in application involving energy optimization or performing extreme motions).

Having understood the advantages of compliant actuators and the challenges associated with them, a closer insight of the properties characterizing the human musculoskeletal actuation system will help to design a robot which can imitate the human behaviour more closely. These properties are: antagonism, compliance, non-linearity, and muscle-tendon coupling. The different benefits that these properties can bring are described below:

- Antagonism can provide the possibility of controlling both position and stiffness. This phenomenon is widely common in mammals and therefore enables us to understand bio-inspired actuation better;
- Compliance increases the overall safety for both the robot and its environment. It acts a passive low pass filter to absorb the impact forces. Due to energy absorbing capacity, it can be exploited to increase energy efficiency of the whole system by transferring kinetic energy to elastic energy of elastic elements, and vice versa;
- Non-linearities pose a great challenge from control point of view. But with the capability to adjust stiffness, one can optimize a task by making a balance between accuracy and safety;
- Tendon coupling enables faster motion as it reduces inertia, friction, backlash and static load.

Therefore, in the present thesis, antagonist inherent compliant system is considered to be our primary area of study. In addition to this, after having a wide survey of the different compliant actuators, we have also considered electro-active polymer based actuators. The motivation behind this study is coming from the previous work of our laboratory which is very inquisitive in search of potential soft actuators for the future generation of robots or microbots. In the next subsection, our primary subject of study, which is the actuators based on Mckibben muscles is introduced and our contribution in the design, modeling and control is highlighted. We will then present our contribution towards the nonlinear control of an electro-active polymer based actuators.
0.2 Pneumatic actuators

Pneumatic actuators are inherently compliant and have very high power to weight ratio. These factors motivate researchers to use pneumatic actuation for exoskeleton, prosthesis, rehabilitation or even in walking robot and human robot interaction. Our goal in this thesis is to use an arm actuated by McKibben muscles to perform explosive tasks like hammering or kicking balls. Recent works [Kumar 2013] advocates other kind of actuation system which are easier to control but come with a high price tag. Our goal was to demonstrate here that with minimal modification of an existing platform [B.Tondu 2005], it is possible to perform such kind of explosive motions, and not fine manipulation as in [Kumar 2013]. The Mckibben artificial muscle is known for its non-linearities and hence pose a great control challenge. These non-linearities are mainly due to hysteresis, saturation and internal friction between fabrics. So far these challenges were dealt with traditional controllers like high gain PID controller, sliding mode controller for position control [Tondu 2009]. These methods usually lead to stiff system dynamics with higher impedances. Recent developments in pneumatic actuation control [Tassa 2013, Kumar 2014] are use Model Predictive Control (MPC). For instance in [Andrikopoulos 2013], the control scheme is based on a switching Piece Wise Affine (PWA) system model approximation. The method is able to capture the high non-linearities of the Pneumatic Artificial Muscle (PAM). In [Tassa 2013] a linear formulation of the actuation system is proposed to simplify the algorithm implementation and makes it real-time.

Our contribution :
- First we propose a new model which provides a good compromise between accuracy and simplicity.
- The second contribution is to show that, on this model an iLQR control scheme can be used to generate with good precision positioning task and explosive movements.

This is achieved with the introduction of an empirical model of pressure generation from the Intensity-Pressure converter (I/P). Each of the seven Degrees of Freedom (DoFs) of the manipulator arm of LAAS-CNRS is actuated by a pair of agonist-antagonist Mckibben muscles. The capabilities of the non-linear iLQR control to execute some simple tasks of reaching a point, maximizing the velocity of joint and end effector are demonstrated on this platform.

0.3 Ion-polymer actuators

Ionic polymer based actuators constitute a class of electro-active polymer. They have great potential in future nano or micro robotics applications. They have already found some applications in the medical field. It is primarily due to the fact that these polymer actuators are having a very low operational voltage range. This makes them very suitable to be used in a close environment with humans. When the
voltage is applied, it generates mechanical stress or strain. In this way, the shape and volume change of Electro-Active polymers are due to the mass transport of ions within the polymer and their uneven distribution. The challenge for such actuators is the complicated fabrication process and requirement of liquid environment for the electrode. As recent advancements have overcome this problem and such actuator could be used in open air ([Annabestani 2015, Bennett 2004]). And this makes it possible to see the potential of such actuator in the filed of robotics. From the control point of view, the system being very non-linear is not so easy to model and then control.

**Our contribution**
- Our first contribution is to have proposed a simpler non-linear model for the ionic polymer actuator.
- Then we have shown that using this proposed model, a simple conventional PID controller could be deployed to control accurately this system.

### 0.4 Thesis organisation

The thesis is organised in five chapters. The first chapter is presenting a brief survey of different existing compliant actuators. We have covered actuators which are as simple as SEA with just one linear spring up to a complex mechanical arrangement of VSA and AWAS developed by University of PISA and IIT. In order to understand these actuators, they are loosely divided in different groups based on their similar mathematical structure. In all of these groups, a mathematical model is given and it is shown with formulas and functions how these actuators vary their compliance. Later, artificial muscles and their different types and broad classification are presented. Following this, we have given an introduction to the Mckibben muscles and the definition of various terminology. This is the base for later chapters in the thesis. Since our work evolved in two direction; actuators based on the Mckibben muscles and Ionic-polymer actuator, a separate chapter is dedicated to our work done on Ionic polymer actuator. In this chapter, we have tried to show its potential for being a soft actuator along with the problems associated with it. More importantly, the chapter reports our effort to characterize the actuator and the control strategy for controlling this system.

The rest of the thesis presents our extensive work we have done on our experimental set-up which is a 7 Dofs anthropomorphic arm.

Chapter 3 describes in detail the static and dynamical model of joints actuated by Mckibben muscles. Also the agonist-antgonist model in different configuration, namely symmetric or generic case, is discussed. After proposing the model, different control strategies are discussed in Chapter 4. We have tried to show that a generic single-I controller could be possible to avoid the modelling details. However, for practical purposes, a model based PI controller is used. The optimal control formulation and introduction to the iterative Linear Quadratic Regulator(iLQR)
algorithm is explained. This algorithm is extensively used for generating control sequences for the high performance motion. Chapter 5 reports all the simulations results and various results of the experiments performed on our robot. Many technical details regarding the parameters of the different components of the robotic arm, cad models, electronics, NI modules, data communication and software packages are given in appendix. In the appendix, we also present an analytical proof for stability of the close-loop single-I controller.

0.5 Publications

The work done on this thesis have given rise to the following publications:

Chapitre 1
State of the art

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Traditionally, robots installed in the manufacturing plants and assembly lines are working in isolated confinements. The vision of robotic co-worker is still a long way to go. In fact, most today’s robots are made very rigid at the joints to have good position accuracy and easier control with traditional PI controllers. But this comes at the cost of safety to human and that limits the possibility of human-robot physical interactions. As the field of robotics is evolving rapidly, the need of robots working in human friendly environment has become a necessity. It is then thought that compliance in the robots is in fact a desirable property. It cannot only minimise the damage to the human in case of collision but also saves the gears and motors of the robots. To address this question, there have been several attempts to make the robots more and more friendly to human interaction. Software controlled compliance is one of the attractive solutions used nowadays. In this way, software depends on the sensors which detects the interaction or collision and a close loop action ensures that the robot responds smoothly and softly to minimize the impact. However, the time delay due to sensing and feedback control loop could be fatal in some scenarios of sudden collision. Also the possibility of failure of circuitry or sensors makes the software controlled compliance vulnerable in many situations and limit robotic applications in high speed tasks. Therefore, it is interesting to consider inherent compliance within the structure of the robot or at the joints level. Compliance within the structure and flexibility in the links of the robot cause several complex non-linearities. Modelling these kind of robots is known to be difficult and hard to control. In this chapter we present a survey which provides a state of the art of the different actuators which can induce compliance in the robots at joint level. The ability of the stiff actuation units to interact with their surroundings
can be increased by means of active control approaches, however the existence of delays at all stages of the software system make these conventionally stiff actuated systems incapable of managing high-speed contact transients because of their limited bandwidth. This poses a requirement of inherent compliance at actuator level. A special attention has been paid to pneumatic system based actuators and two different kinds of pneumatic systems (Pleated pneumatic artificial muscles and the Mckibben muscles) are explained in more details. Before that, we would like to introduce the basic definition of compliance/stiffness and some terminology that will be used throughout in the thesis.

1.1 Compliance actuators

Nowadays robots are expected to work closely with humans. Since human safety is of high priority, robots have to be compliant during interaction. Therefore, compliance in robotic is now considered as one of the desirable properties. This requirement motivates the design of a new kind of compliant actuators called Variable stiffness actuators (VSAs). In parallel, there have been several studies to learn how vertebrates control their motion perfectly while maintaining a good compliance. The design of artificial muscle is motivated by such studies. Artificial muscles are expected to have some properties found analogous to biological skeletal muscle. This section starts with a final definition of compliance in the scope of robotics and a rapid description of the functionality of skeletal muscles in humans.

1.1.1 Compliance definition

Here a brief definition of some important terms are given which will be used in the paper extensively. Stiffness is the differential of force/torque with respect to position. Compliance and stiffness are inverse to each other. Damping is the differential of force/torque with respect to velocity. Impedance and admittance are complimentary terms to each other and define a mechanical interaction between two bodies using their intrinsic properties. Admittance describes the dynamical relation of force with respect to displacement [Hogan 1985]. Let us elaborate this with the help of a simple example of a single link with flexible element as illustrated in figure 1.1. [F. 2011] has defined two stiffness terms. One is called internal or passive stiffness which is due to flexible elements and another stiffness term is called external stiffness which is observed at the output link level. However, in literature slightly different definitions are also available [Grioli 2011, Ozawa 2002].

\[ \sigma_{\text{internal}} = \frac{\partial \tau_e}{\partial \phi} \]  

\[ \sigma_{\text{external}} = \frac{\partial \tau_{\text{ext}}}{\partial q} \]  

Where, \( \theta, q \) are motor position and link position respectively and \( \phi = q - \theta \) is the deformation. \( \tau \) is the motor torque, \( \tau_{\text{ext}} \) is the net torque applied on the link. \( \tau_e \) is
1.1. Compliance actuators

![Figure 1.1 – A single link with flexible transmission](image)

the flexibility torque generated due to the twisting of the flexible element.

1.1.2 Compliance in Human arm

Human joints are far more complicated due to the complex arrangement of several muscles, tendons and their insertion into the bones. However, the simplest equivalent model is the revolute joint. The force, $\mu$, generated by any muscle is translated into torque on the joint by its moment arm \[\tau = \rho \mu;\] Where $\rho$ is the moment arm defined as the perpendicular distance between the axis of rotation of the joint and the line of action of the muscle-tendon spanning the joint. This is explained in figure 1.2. The co-contraction of muscles changes the line of action of the muscle-tendon on the bones, thus changing the moment arm and in turn varies the torque. So the moment arm is related to muscle length ($\lambda$) and joint angle ($q$) in this manner $\rho = \frac{\partial \lambda}{\partial q}$. Hence, Joint stiffness and damping can be

![Figure 1.2 – Human muscle-tendon spanning a joint.](image)
described by the following equations.

\[ K = \frac{\partial \tau}{\partial q} = \rho \frac{\partial \mu}{\partial q} = \rho^2 \frac{\partial \mu}{\partial \lambda} = \rho^2 K \mu \tag{1.3} \]

\[ D = \frac{\partial \tau}{\partial \dot{q}} = \rho \frac{\partial \dot{\mu}}{\partial \dot{q}} = \rho^2 \frac{\partial \dot{\mu}}{\partial \dot{\lambda}} = \rho^2 D \mu \tag{1.4} \]

The dependency of joint stiffness and damping on moment arm and intrinsic muscle properties like muscle stiffness \((K_\mu)\) and muscle damping \((D_\mu)\) is quite evident. A pair of muscles spans the joint and acts antagonistically to move the arm. So the net torque on the joint is defined by the difference of agonist and antagonist muscle action.

\[ \tau = \tau_+ - \tau_- = \rho_+ \mu_+ - \rho_- \mu_- \tag{1.5} \]

For any particular joint, \(\tau\) depends on muscle force \(\mu\) which in turn depends on neural activation history, muscle length and its connection to the bones. It has been established by [Milner] that a wide range of \(\mu\) can satisfy the above equation due to the fact that numerous muscles are spanning a particular joint. So it is possible to find the set of \(\mu\) which can just change the stiffness by modulating the moment arm by co-contraction while keeping the torque constant.

### 1.2 Review of Variable Stiffness Actuators (VSA’s)

In order to allow safe interactions with humans, several designs have been proposed for actuators. Most of them are VSA which modulate the stiffness, some are variable damping actuators to resist to the velocity deflection and some are the combinations of both. In this section a short survey of VSAs are presented. A broad classification of these actuators has been presented in [van Ham 2009] where the four main classes have been defined on the basis of the method of stiffness control.

**Equilibrium controlled**: The compliance element with fixed intrinsic stiffness is placed in series with conventional motors. The stiffness is varied by moving the equilibrium position of the spring. One common example is SEA[Pratt 1995].

**Antagonistic controlled**: Two actuators with nonlinear force-displacement relationship are coupled antagonistically to act against each other. Using both motors simultaneously equilibrium position and stiffness can be controlled. Examples are VSA-I[Tonietti 2005], VSA-II[Schiavi 2008], VSA-HD[Catalano 2010b], PDAU[Kim 2010a], AMASC[Hurst 2004], PPAM[Verrelst 2005] and QA-Joint[Catalano 2010a].

**Structure controlled**: The compliance is varied by controlling the structural property of flexible element like material modulus, moment of inertia or effective length. Examples are Jack spring[Hollander 2005] and MIA[Morita 1995].

**Mechanically controlled**: The actuators have usually one main compliant element. The stiffness is changed by mechanically adjusting the pretension or preloading of the compliant part. Examples are MACCEPA[van Ham 2007], VS-Joint[Wolf 2008], AWAS-I[Jafari 2010], AWAS-II[Jafari 2011], CompAct-
1.2. Review of Variable Stiffness Actuators (VSA’s)

VSA [Tsagarakis 2011], vsaUT [Groothuis 2013], SDAU [Kim 2010a] and HDAU [Kim 2010b].

1.2.1 Fixed compliance actuators

Fixed compliance actuators can be considered as one of the first attempts towards the development of compliant actuation systems. These actuators contain a passive compliant element with fixed stiffness which is usually placed between the rigid actuators and the load. These kinds of fixed compliance actuators can be implemented in antagonistic or series configuration. Here, the series configuration is discussed as it is the most common implementation. A conceptual schematic of such implementation is shown in Fig. 1.1.

The link is actuated by motor-gearbox but these two components are separated by a fixed stiffness compliant element. Such an implementation has two control variables $\theta$ and $q$. $\theta$ is the angle of the input pulley of the compliant element and the output angle is $q$ which is also the angular position of the link. One of such set-up introduced in [Pratt 1995] used a DC motor coupled to a planetary gearbox and a fixed stiffness torsion spring. Some of the great advantages with SEA are their low impedance due to series compliance and low friction. These properties make SEA achieve high fidelity force control and hence make them a suitable actuators for robotic applications in unstructured environment. So far, most force/torque controlled robots rely on load cells/torque sensors [Hirzinger 2001]. These are not only expensive and sophisticated but may induce chatter in force control due to their high stiffness. On the other hand, compliant element used in SEAs (usually springs) are inexpensive, robust and stable. The following relationship describes the force delivered by a linear SEA actuator and the measurement of the compression of the compliant element:

$$F = kx,$$

where $F$ is the force applied by the actuator, $k$ and $x$ are the stiffness and compression of the linear compliant element respectively. In the case of rotary implementations typically using torsional spring, the above relationship can be described as:

$$T_{rotation} = k_t S,$$

where $T_{rotation}$ is the torque delivered by the actuator while $k_t$ and $S$ are the stiffness and compression of the rotary compliant element, respectively. Fig. 1.3 shows the implementation of force control using SEAs. The compliant element deflection state can be used in the precise estimation of the torque or force in SEAs.

The force $F_{load}$ is estimated from the deflection of the spring element and is compared with the reference $F_{desired}$ in order to return an error $F_{error}$. Thus the appropriate control signal for the electric motors are generated by $F_{error}$ together with the measured position $x_{load}$ and the reference. Fixed compliance actuators have been used also in rehabilitation robotics where a prosthetic ankle device has been actuated using SEA [Au 2008]. Those applications have shown significant per-
formance improvements brought by SEAs. Actuators have the capability to absorb the shocks which can ultimately improved safety in human-robot interaction and protect the motor-gearbox group from shock loads generated during the foot strike. Moreover, the use of SEAs increases the torque control bandwidth which allows the prosthesis controller to imitate the torque-velocity behaviour of the human ankle in walking. SEAs were a good start for a safe human-robot interaction but the stiffness level in them is usually a fixed preset value. It is then thought to have the ability to vary the stiffness level depending on the nature of the task or the interactions with the environment. This motivates for the alternative designs of variable compliance actuators.

1.2.2 Variable compliance

Variable compliance actuators are actuators which are capable of regulating their physical compliance. Compliance and stiffness are inversely proportional and hence used interchangeably and therefore such actuators are more commonly known as Variable Stiffness Actuators or VSAs. Unlike fixed compliance actuators, they can control both stiffness and position simultaneously. Most importantly they enjoy wider range of stiffness and have energy storage capability. These actuators could make the robot more closer to the mammals with respect to the movement. It is well known that muscles and tendons in the mammals change their stiffness as a function of the motion they have to perform. For example, muscles at arm acquire a a stiff configuration when the arm has to perform an accurate task, while they are compliant when they are performing the loading phase of a throw. Similarly, while jumping one can observe that leg muscles are compliant during the loading phase of the jump or during the landing phase where they absorb the shock [Cheung 2004], while during the pushing phase, they are stiff. The underline principle behind the variation in stiffness is the exploitation of the elastic energy stored within the muscles and tendons [Ishikawa 2005]. In [Hirzinger 2008], the authors had compared a rigid joint and a compliant joint. Different tasks were performed in
both cases and it was observed that there is a clear difference between the velocities of the links and the throw distances obtained in the two cases. Thus, it is concluded that joints with variable compliance actuators can achieve performance that is not possible with a conventional stiff robotic system. This motivates researchers to introduce different designs to incorporate variable compliance into the actuation systems. In the following section, various such designs are presented. The physical set-up, conceptual working principle along with their mathematical models are described. Broadly, variable compliance actuators can be categorized into two main groups: Series configuration and antagonist configuration. The division is based on the physical realization of the compliance element with respect to the motor and the load.

### 1.2.2.1 The series configuration

In this configuration, a variable compliance element is placed in series between the actuator and the load. Two different actuators are employed to set the equilibrium position of the joint and the stiffness independently. In both actuators one big motor changes the position and a small motor tunes the stiffness.

Adjusting the stiffness in both actuators is done through a lever mechanism (Fig. 1.5 and Fig. 1.7). A lever has three principal points: the pivot: the point around which the lever can rotate, the spring point: the point at which springs are located and the force point: the point at which the force is applying to the lever. The variation in stiffness is achieved by varying and controlling these principal points. For example, stiffness variation in AWAS ([Jafari 2010]) is carried out by moving the spring point while the pivot point is controlled to achieve stiffness variation in AWAS-II ([Jafari 2011]).

Before going into any particular design of serial VSAs, basic functioning and a simple but generic model of such actuator is presented. Fig. 1.4 shows a schematic model of a serial VSA. It consists of a principal motor and a secondary motor. While the principal motor is used to command the link motion through the flexible transmission, the secondary motor is used to modify the stiffness of the transmission.

\[
M\ddot{q} + \tau_e(\theta_e, \phi) + g(q) = \tau_{ext} \\
B\ddot{\theta} + D_\theta\dot{\theta} - \tau_e(\theta_e) = \tau \\
B_e\ddot{\theta}_e + D_\theta\dot{\theta}_e + \psi_e(\theta_e, \phi) = \tau_e
\] (1.10)

In the above Eq. 1.8, the first line is the general robotic equation for the link side. Principle motor side dynamics is expressed in second line while the third line represents the secondary motor side dynamics. \(M\), \(B\) and \(B_e\) are mass inertial matrix while \(D_\theta\) is the viscous term. \(\tau_{ext}, \tau, \tau_e\) and \(\psi_e\) are the external torques on the link side, torque on the primary motor side, restoration torque due to deformation and the reaction torque on the secondary motor. The device stiffness is given by the
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Figure 1.4 – Working principle of Serial VSA.

\[ \sigma(\theta_c, \phi) = \frac{\partial \tau_e(\theta_c, \phi)}{\partial \phi} \]  

(1.11)

Some examples of variable stiffness actuators implemented with the series approach are presented next.

Actuators with Adjustable Stiffness (AwAS) In AwAS ([Jafari 2011]), the force and pivot point are kept fixed and the spring point is changing in order to regulate the stiffness. The schematic and cad model are shown in figures : 1.5 and 1.6. The stiffness in this case can be defined as :

\[ K = 2K_s r^2 (2 \cos^2 \phi - 1), \]  

(1.12)

Figure 1.5 – Basic principle of AWAS-I actuator.
where $K_s$, $r$ and $\phi$ represent stiffness of the springs, the distance between the spring point and the pivot and the angular deflection, respectively. The range of stiffness depends on the stiffness of the springs and length of the lever. In this design, stiffness can be achieved in a good range since it depends on the square of the arm $r$.

**Actuators with Adjustable Stiffness-II (AwAS-II)** In AwAS-II ([Jafari 2011](#)), force and spring points are kept fixed but instead the pivot point is changing. The modification is done to make the system more energy efficient while enjoying larger stiffness range. It was made possible due to the fact that the displacement needed to change the stiffness by moving the pivot is perpendicular to the force generated by the springs. Therefore the stiffness motor does not need to directly work against spring’s forces. The schematic and cad model are shown in figures below : 1.7 and 1.8. The stiffness in this case can be
defined as :
\[
K = 2K_s\alpha^2(L_1 + L_2)^2\cos\phi,
\]
(1.13)
where \(L_1\) represents the distance between the pivot and the springs and \(L_2\) is the distance between the pivot and the force. \(\alpha\) is the ratio (adjustable) which is \(\frac{L_1}{L_2}\).

Using this mechanism the stiffness can be achieved in the largest possible range from zero to infinite since it depends on the ratio. The ratio becomes zero when the pivot reaches the spring point and it becomes infinitive when the pivot reaches the force point. This range does not depend on the stiffness of the springs and lever’s length. Therefore shorter lever and softer springs can be used in this mechanism which leads to have a lighter and more compact set-up compared to the mechanism applied to AwAS.

The Jack Spring actuator A linear series-type variable stiffness actuator is the Jack Spring, [Hollander 2005]. In this solution, stiffness is varied by changing the number of active coils of the series spring. The adjustment of the stiffness is done by rotating the spring about the coil axis. This rotation is transformed into a linear motion of the spring along its axis due to the geometry of the shaft on which the spring is mounted. In fact, this shaft is machined with the same coil geometry of the spring and the inside/outside motion of the spring is achieved by screwing/unscrewing the spring on its shaft. This motion changes the effective stiffness of the actuator by varying the active spring coils. Also refer Fig. 1.9. The following formula describes a coil spring stiffness :
\[
K = \frac{Gd^4}{8D^3n_a}
\]
(1.14)
\(G\) is the material shear modulus, \(d\) is the wire diameter, \(D\) is the coil diameter, and finally \(n_a\) is the number of active coils. The Jack Spring actuator principle works on this last parameter to vary the stiffness of the overall actuator. In this concept,
one motor is used to adjust the equilibrium position of the actuator and a second motor is used to adjust the stiffness.

\[ T = kBC\sin(\alpha)(1 + \frac{P - L}{\sqrt{B^2 + C^2 - 2BC\cos(\alpha)}}) \]  

where \( k \) is the spring stiffness and \( L \) is the natural length of the spring. The relationship between the compression angle \( \alpha \) and the delivered torque depends on the spring pre-load \( P - L \) meaning that the overall joint stiffness can be regulated acting on the pre-load of the spring using the motor \( m \). The angle \( \psi \) imposed by the main actuator sets the equilibrium position of the joint.
1.2.2.2 The antagonistic configuration

Amongst all the configurations of VSAs, agonist-antagonistic actuators are closest to the mammalian anatomy. A mammalian joint is usually actuated by two muscles arranged in an agonistic-antagonistic manner. The muscles and tendon work in cooperation to have a controllable and variable compliance while driving the arm or leg. Based on the same concept, antagonist actuators have two compliant elements to power the joint. It is interesting to note that this type of antagonistic controller compliance can be achieved using both conventional electric motors and other more biologically inspired actuators such as Pneumatic Artificial Muscles (PAM). While an electrical design relies on incorporating the external compliance element (typically spring) into the system and on the other hand, compliance is an inherent characteristic of the actuator in the case of PAM. Each of these designs have their own advantages and drawbacks. PAM are mechanically easier to design and fabricate but pose a great challenge to control. Whereas electric motors driven VSAs are too bulky and cumbersome. In the following subsection, electrically driven antagonistic VSAs are considered. The conceptual basic operations and their dynamical behaviour are explained with the help of some most common VSAs like VSA-I and VSA-II.

Fig. 1.11 shows a schematic model of an antagonistic VSA where two motors working in parallel and antagonistically are connected to the link through non-linear transmissions. Non-linearity of deformation/torque characteristics of the transmissions is to be exploited for regulating the stiffness. It is achieved either by the use of nonlinear (e.g., cubic or exponential) springs or by the arrangement of linear springs in a non-linear kinematic mechanism. The two motor-transmission units are modelled with two similar equations of the form 1.16, where each motor-transmission undergoes a deformation $\phi_i = q - \theta_i$, for $i = 1$; 2. The dynamics of an antagonistic VSA is shown below
And the total flexibility torque transmitted to the driven link and the total device stiffness are given below

\[
\tau_{e,t} = \tau_{e,t}(\phi_1) + \tau_{e,t}(\phi_2) \\
\sigma_t = \sigma_1(\phi_1) + \sigma_1(\phi_2)
\] (1.18) (1.19)

There are several actuators which were designed based on the model described in 1.16. Migliore’s Actuator was one of the pioneer design in this direction. In order to make the actuator more compact and energy efficient, there had been a constant ongoing effort to innovate new design which resulted into VSA-I, VSA-HD, VSA-II, vsaUT [Groothuis 2013] and compactVSA [Tsagarakis 2011]. As appeared in many literature, We present the design construction and mathematical model of few such actuators which set a new paradigm in the field of electric driven actuators.

**Migliore’s Actuator** Migliore’s Actuator proposed in [Migliore 2005] uses two conventional electrical drives connected in an antagonistic manner to the output joint through non-linear springs. A positive angle \(\alpha\) of the agonist servo motor provides positive rotation of the angle \(\theta\) of the output drive, while the antagonist actuator sets an angle \(\beta\) in opposition to the output joint angle, Fig. 1.12. Using linear springs in this configuration, the output joint stiffness will be:

\[
S_{\text{linear}} = R_2^2 (k_1 + k_2),
\] (1.20)
where $R_J$ is the radius of the output pulley, $k_1$ and $k_2$ are the stiffness of the springs of the agonist and antagonist servos. The output joint stiffness depends only on the constructive parameters of the joint and on the springs stiffness which is constant. The variation of stiffness of the spring components can be set to be linearly related with the co-contraction by using elastic elements with quadratic force-elongation relationship as follows:

$$F(x) = a(x - x_0)^2 + b(x - x_0) + c,$$  \hspace{1cm} (1.21)

where $F$ is the force applied by the motors, $x$ is the elongation of the spring component, $x_0$ is the natural length of the spring and $a, b$ and $c$ are constants. Using such spring components, the stiffness of the output joint, $S$ will be:

$$S = 2\alpha R_S R_J^2 (\alpha + \beta) + 2bR_J^2,$$  \hspace{1cm} (1.22)

where $R_S$ is the radius of the driving pulleys. In this case stiffness can be varied by means of the co-contraction of the drives (given by the sum of $\alpha$ and $\beta$), with constant offset $2bR_J^2$. On the other hand, the displacement of output joint is achieved by means of the agonistic motion of the motors. Schematic shown in Fig. 1.13 elaborates the mechanical implementation of the non-linear spring component by means of a quadratic profile of the part named 'Frame'. The assembly shown in Fig. 1.13 replaces the conventional extension springs shown in the antagonistic setup of Fig. 1.12 therefore permitting the regulation of the joint stiffness.

![Schematic model of a Milgiore’s Actuator (VSA)](image_url)

**Figure 1.12** – Schematic model of a Milgiore’s Actuator (VSA). Figure adopted from [van Ham 2009]

**Variable Stiffness Actuator (VSA)** The VSA is a Variable Stiffness Actuator which enjoys the cross-coupled arrangement unlike Migliore’s actuator which is the simple arrangement. The modification is done to make the actuator more compact. The stiffness regulation scheme in this design can be better explained using a CAD
1.2. Review of Variable Stiffness Actuators (VSA’s)

Figure 1.13 – Mechanism to implement the stiffness non-linearity. Figure adopted from [van Ham 2009]

Model shown in Fig. 1.6. The VSA consists of three pulleys (2, 3, 4) connected by means of a timing belt (1). Pulleys 2 and 3 are actuated by means of position-controlled backdrivable DC motors, while the output pulley (4) is connected to the link. The output joint stiffness can be computed to be:

\[
\sigma = 2KR\left(\frac{\bar{h}_{m,1} - \bar{h}_{m,1}}{h_{m,1}} + \frac{\bar{h}_{2,m} - \bar{h}_{2,m}}{h_{2,m}}\right) - 2KR\left(\frac{\bar{h}_{m,1}L_{m,1}}{4h_{m,1}^3} + \frac{\bar{h}_{2,m}L_{2,m}}{4h_{2,m}^3}\right) \quad (1.23)
\]

where \(K\) is the linear spring stiffness, \(R\) is the radius of the pulleys 2, 3 and 4, \(\bar{h}_{m,1}, \bar{h}_{m,1}\) and \(\bar{h}_{2,m}, \bar{h}_{2,m}\) are the natural and active lengths of springs 5 and 7. \(L_{m,1}\) and \(L_{2,m}\) are the lengths of the belt between the pulley pairs 2-4 and 3-4. This means that stiffness can be changed by acting on the active length of the springs and on the belt length. In detail, by means of high/low co-contraction, high/low compression of the springs 2 and 4 (Fig. 1.15) will generate high/low apparent output joint stiffness. Fig. 1.15 further shows the geometric details of any pair of pulleys around a spring.

In practice, the antagonist motion of the drives varies changes the apparent angle between the spring axis and the belt and this creates the non-linear stiffness/compression relationship which permits the stiffness adjustment. Agonist motion of the drives only generate displacements of the output shaft.

**Variable Stiffness Actuator - II (VSA-II)** The VSA - II, as proposed in [Schiavi 2008], is an antagonistic actuator which uses the bi-directional actuation principle and can be represented in the schematic of Fig. 1.16. The VSA-II shows several improvements with respect to the previous VSA-I. For example, the introduction of a 4-bar mechanism which shows higher load capacity and robustness. This mechanism implements a variable transmission system used to obtain a non-linear relationship between input and output torque/displacements. Using a linear
spring on the input, the relationship between deflection and torque on the output shaft can be made non-linear. Referring to the Fig. 1.17. The link OA is actuated by a motor at O. The torsion spring of stiffness $k$ is linear, however the stiffness at O is nonlinear with angles $\beta$ and $\theta$ and is described by the following relationship,

$$\sigma(\theta) = \frac{1}{4} k \left[ \left( \frac{R L \cos \theta}{1 - \left( \frac{R L \sin \theta}{2} \right)^2} - 1 \right)^2 + \frac{R L \left( R^2 \sin^2 \theta - 1 \right) \beta \sin \frac{\theta}{2}}{1 - \left( \frac{R L \sin \theta}{2} \right)^2} \right]$$

$$\sigma = (a)$$

(1.24)
1.3 Artificial muscles

Traditional actuators are stiff and having high low power density, power-to-mass ratio and efficiency. VSAs are compliant however mechanical complexity, bulkiness and low power to mass ratio make them difficult to be integrated in small multi-joint robots. There is a growing interest in robots working with or in close vicinity of humans. So, it is desirable to make the next generation robots with lightweight materials having inherent compliance and adapted control strategies combined with passive compliant dynamics.

1.3.1 Review of Artificial Muscles

In this section, we are presenting briefly different types of muscle-like actuators or simply called artificial muscles. These actuators, even though they are still in development, have shown a good potential to replace prevalent ac-
It is possible to extend the applications of robotics in medical devices like invasive surgical or diagnostic instruments [Guimard 2007, Ruiz 2015, Tozzi 2011], prosthetics, rehabilitative exoskeleton, soft robotics (as grippers and manipulators) [Choi 2007] and recreation toys using such actuators due to their fabrication flexibility.

Artificial muscle can generate reversible contraction, expansion, or rotation within the body by the application of an external stimulus. These stimulus could be voltage, current, pressure, temperature etc and are the basis of division of the artificial muscles into different types [Mirvakili 2013]. They can be divided broadly into (1) pneumatic, (2) thermal, (3) electric field and (4) ionic actuators. The comparison of the currently investigated artificial muscles is shown in Fig. 1.1. Even though, the combination of the efficiency (40), strain rate (50/s) and specific power (284 W/kg) of a human skeleton muscle are hard to compete (Fig. 1.18b), artificial muscles are often compared to it.

The current state-of-the-art tendencies and challenges of prevalent artificial muscles are discussed in the following sections.

**Pneumatic actuation**  Pneumatic actuation generates contraction force using elastomer stress. So the linear motion, thus generated, is due to inflating and deflating a rubber tube beneath the structure. This actuation system has been used widely [Daerden 2002, De Volder 2010, Ilievski 2011, Zhang 2011] because it is extremely lightweight and inherently compliant. One of the most common type of Pneumatic actuators are McKibben-type actuators which have been further developed in order to improve their lifetime and control [Meller 2014, Tondu 2012, Zhang 2011] due to their mechanical design of braided sheath structure. However, there is a constant development going on in pneumatic based actuators and new inflatable materials are being suggested such as the pneumatically-driven flexible microactuators (FMAs) [Gorissen 2011, Gorissen 2014] or the embedded pneumatic networks of channels in elastomer (PneuNets) [Ilievski 2011]. These actuators are capable of generating complex motions with the single source of pressure and hence different motions like gripping, bending or crawling can be created simply by changing their configurations and size [Martinez 2014, Morin 2014, Mosadegh 2014, Shepherd 2013]. As the experimental setup considered in this thesis will be using Mckibben muscle, we will extensively discuss in the latter sections, the model, geometric and mechanical construction, advantages and challenges of using Mckibben muscle based actuators.

**Thermal actuation**  Thermal actuation normally uses a Shape-memory alloy (SMA) materials which can undergo a phase and shape change with temperature or stress. To use SMAs as actuator, they are usually heated by running current through them (reviewed by [Kheirikhah 2011]). Nitinol is one of the most well known lightweight solid-state SMA. However, the major drawback with most of the solid-state materials is that they have limited life cycle and they fail due to the micro-
1.3. Artificial muscles

Figure 1.18 – (a) Stress versus strain and (b) work density versus strain rate of typical artificial muscles (defined by lines) and some state-of-the-art actuators (stars). Types of actuations: blue - electric, orange - ionic, green - thermal, red - CNTs, gray - others, black - mammal skeletal muscle. Adopted from [249, 269] and other sources mentioned in the text.

Structural crack propagation and fracture. Furthermore, cooling of the actuator is significantly slower than heating and causes a response asymmetry. In order to deal with this problem, Shape memory polymers (SMPs) are proposed. They are low cost and are able to produce larger strains of up to 700% [Koerner 2004] (typical strain of SMAs is 0.1%). Furthermore, due to easier processing and synthesis flexibility, SMPs could be tailored to required applications (reviewed by [Behl 2013, Sun 2014]).

Thermal expansion phenomenon has been recently used for actuation purpose by the twisted yarns of metals [Mirvakili 2013], carbon nanotubes (CNTs) [Lima 2012], nylon or polyester [Haines 2014]. When the length of the yarn is kept constant during heating, the yarn untwists and its diameter increases. Alternatively, when the change in the twist is restrained, during the actuation yarn contracts in length and its diameter increases. Multiwall carbon nanotubes (MWCNTs) are one of the first actuators of this kind [Zhang 2004]. MWCNTs have very high strength (up to
electric-field actuation. When a voltage is applied, the electrostatic pressure between the electrodes (Maxwell Stress), arising due to the Coulomb forces, compresses the thickness and expands the area of the elastomer in between. DEAs usually produce large strain $\varepsilon_3$ (Fig. 1.18a). The fabrication of DEAs requires low-cost, lightweight and conformable materials [Brochu 2010], [Kornbluh 2013]. One of the challenges of DEAs based actuator is the need of flexible and stretchable electrodes. Also DEAs require high electric fields (150 M V /m) and, consequently, voltages up to 5 kV, therefore their applications in the fields that require contact with humans is very limited [Madden 2004a, Mirfakhrai 2007].

**Ion-based actuation** Ion-based actuation relies on the production of mechanical stress or strain of several percent by application of voltage within a very small range $(1 - 3V)$. In this method, the shape and volume change of Electro-Active polymers are due to the mass transport of ions within the polymer and their uneven distribution. It is essential to have a low voltage devices when working in the vicinity of human. For this reason, these Ion-based actuators have already found various applications [Doring 2013] in biotechnology and medicine [Bawa 2009, Cabane 2012]. Several types of ionic EAPs are being investigated for applications as artificial muscles: ionic gels [Maeda 2010], ionic polymer-metal composites (IPMCs) [Jo 2013, Tiwari 2011], conducting polymer actuators (CPAs) [Baughman 1996] and, more recently, carbon nanomaterial based composites [Baughman 1999, Kong 2014]. Ionic gels could potentially match the force and the energy density of a skeletal muscle at low voltages. But its weak mechanical pro-
1.3. Artificial muscles

Properties need to be improved [Bassil 2014, Imran 2010]. Ionic polymer-metal composites (IPMCs) have potential applications in the underwater robotics (e.g. grippers [Ford 2015], swimming devices [Chen 2011, Kim 2005, Palmre 2013]) and medicine (e.g. microgrippers [Feng 2014], steerable catheters [Ruiz 2015]) due to the low actuation voltage and relatively large bending. But one of their drawbacks is that the actuation is followed by a slow relaxation due to the water diffusion. Moreover, IPMCs are sensitive to dehydration, hydrolysis above 1.23 V and tend to drift in the position or get permanently deformed. Carbon nanotubes, since from the time of its discovery, have found their applications in several fields. These have been recently used as an ionic actuators. When carbon nanotubes (CNTs) and their composites suspended in the electrolytes [Baughman 1999] or ionic liquids (ILs) [Barisci 2004] and the voltage is applied (1–4V), the CNTs surface is charged and electrolytes form an electric double layer around them. The electrostatic repulsion of the charges on the nanotubes causes the elongation of the carbon-carbon bonds, that consequently elongates the nanotube. Due to their stiffness, networks of entangled nanotubes or yarns are needed to cause macroscopic deformations and even then, a very small strain (< 1%) are achievable [Baughman 1999]. Also these CNTs actuators can have good strain rate, high elastic modulus and huge work densities. After the discovery of the Bucky gel, which is a single walled carbon nanotube and ionic liquid gel-like composite, it is considered for ionic actuators. It is due to the possibility of facile fabrication and the fast response time of the actuators. However, so far, the mass production of CNTs and Bucky gel are quite expensive and difficult and so their applications in the design of actuators are limited. [Li 2008, Tunckol 2012]. There is an ongoing effort to look for cheaper alternatives. Carbon black and carbon fibre mixtures with ILs are being investigated [Terasawa 2014]. Also, there is a growing interest in composite material electrodes that would combine advantages and reduce disadvantages of each type, e.g. carbon - conducting polymer composites [Torop 2014, Surana 2015].

Ionic based polymer actuator has shown the great potential to be a good soft actuator for several robotic applications. Hence, we have considered Ion-based actuation for our study. In the laboratory, an Ionic polymer based bending actuator has been developed and various experiments are conducted to characterize the actuator. We will present our work and contribution in this field in latter chapter (Chapter 2).

1.3.2 Pneumatic Artificial Muscles

Pneumatic Artificial Muscles (PAMs) are contractile and linear motion engines operated by gas pressure. Their core element is a flexible reinforced closed membrane attached at both ends to fittings along which mechanical power is transferred to a load. The membrane is inflated or squeezed when gas is filled in or sucked out of it. It creates a radial expansion or contraction of the membrane which in turn contracts axially and thereby exerts a pulling force on its load. The force and motion thus generated by this type of actuator are linear and unidirectional.
The most common driving force for a PAM’s is gas, usually air which is either forced into it or extracted out of it. This way the actuator is powered by the pressure difference of the inside gas with regard to the surroundings. Although, under-pressure operating muscle have been proposed in [Marcincin 1993, Morin 1953], PAMs usually operate at an overpressure. It is easier to generate and supply compressed gas and a lot more energy can be conveyed by over-pressure than by under-pressure.

Various fluid-driven muscle-like actuators have been there now for almost a century. A classification review of PAMs to cover most of the commonly used PAMs in the research have been presented in [Daerden 2002] where these are broadly classified according to their design and operation: (1) pneumatic or hydraulic operation, (2) overpressure or under-pressure operation, (3) braided/netted or embedded membrane and (4) stretching membrane or rearranging membrane. The distinction between PAM designs were done on the basis of structure of the tension carrying element of the muscle and the way membrane inflates. The tension carrying structure can embrace the membrane or can be embedded into the membrane. Also the inflation of membrane can happen in radial direction either by stretching the membrane material or by rearranging the membrane’s surface. Hydraulic operation has been used in humanoid set-up and robotics applications. However, due to the flexibility needed for inflation and deformation, material strength poses a limit and consequently the pressure difference across the inflating element needs to be limited. Hydraulic operations have usually bad power to weight ratio, typical in the range of about 500 kPa to 800 kPa. This makes hydraulic based actuators less viable as actuators for soft robotics. Below presented the most frequently used PAMs which is the Braided Muscles. Also a short description of Pleated Pneumatic Artificial Muscle (PPAM) is presented, which is one of the recent improvement to counter the drawbacks of the braided design. In fact, we present two kinds of pneumatic system in more depth in order to understand their characteristics. These are PPAM and Mckibben muscles. The former study is based on the work of Daerden ([Daerdan 1999, Daerdan 2001, Daerden 2002]) and the latter work is directly inspired from Tondu ([Tondu 1995]) These studies will further help us to propose model for our own Mckibben musclses which are used as an actuator for our experimental set-up.

**Pleated Pneumatic Artificial Muscle (PPAM)** This actuator was developed by Daerden [Daerdan 1999, Daerdan 2001] in which inflation of muscles occurs by the rearrangement of the membrane. This means no material strain is involved when it is inflated. The way this is done is shown in Fig. 1.19.

The muscle membrane has a number of pleats in the axial direction. The contractile motion due to expanding of the muscle membrane is carried out by unfolding these pleats. There is almost no friction involved in this process. Furthermore, membrane stresses in the direction perpendicular to the axis are kept negligibly small and decrease with an increasing number of folds. This results into a very low energy
1.3. Artificial muscles

Figure 1.19 – Pleated Muscle, fully stretched and inflated [Daerden 2002].

demanding expansion of the membrane. One of the great advantages of this kind of
PAM is that there is almost no hysteresis because of the absence of the friction. Since
the membrane’s expansion needs a very small amount of energy, threshold pressure
could be restricted to a low value, e.g. less than 10 kPa for the muscle used in the
experiment [Daerdan 1998].

The characteristics of this type of muscle depend on the ratio of full length
to minimum diameter, on the strain behavior of the membrane’s material, on the
contraction rate and, finally, on the applied pressure. Contraction force can be
derived mathematically [Daerdan 1999] and expressed as

\[ F_t = -pL^2 f_t(\varepsilon, L, a), \] (1.26)

in which \( L \) represents the muscle’s full length, \( R \) its minimum radius and \( a \) is a
dimensionless factor that accounts for the membrane’s elasticity. Please refer 1.19.

From Eq. (1.26), it can be seen that \( f_t \) is a dimensionless function which depends on
contraction rate, geometry and material behavior. Fig. 1.20 shows \( f_t \) for different
values of muscle thickness \( R/L \).

It has been shown by the author that the thick muscles contract less than
thin ones, but generate higher forces at low contraction rates. Although, infinitely
thin muscle has a maximum contraction of about 54%, practically the maximum
contraction of the this type of muscle can reach up to 45%. It is because a minimum
thickness of the muscles has to be ensured in order to be able to assemble the muscle.

A typical Force-contraction characteristic of PPAM type muscles has been iden-
tified experimentally in [Daerdan 2001]. In the experiment, the muscle used was
made of a para-aramid fiber unidirectional fabric made air-tight by a polypropy-
ylene liner. The end fittings are made of aluminium. Its total weight is about 60g.
The maximum contraction of this muscle was experimentally found to be 41.5%.
The pressure was limited to 300kPa and threshold pressure was below 10kPa. In
order to keep the muscle safe, the maximum force was limited to 3500N. Fig. 1.21 shows the measured force diagrams for a range of operating pressures of a muscle of $L = 10cm$ and $R = 1.25cm$ or $(R/L = 0.125)$.

Since the muscles in unidirectional force generator, two muscles are used in antagonistic setup to move a joint [Daerden 1999, Daerden 1998]. In comparison to the similar set-up using Mckibben muscles, it is concluded that PPAM based actuator has better position accuracy of about 0.1° for a motion range of 60°. Also it has lower rise time. Besides positioning, compliance control was performed [Daerden 1998]. Both position and compliance control was achieved just by using classic linear PI-control techniques. This was possible mainly because of the absence of hysteresis. In the case of positioning experiments with the Mckibben muscle [Caldwell 1993, Inoue 1987, D. G. Caldwell 1995, Hesselroth 1994a, Tondu 1995], in spite of using more or less complex control algorithms, e.g. pole placement, feed-
forward, adaptive control, fuzzy control or neural networks, the step response times are in the order of magnitude of 1s and higher and positioning accuracy worse than 1° for similar motion ranges as above. This shows the tremendous impact hysteresis due to friction has on controlling these actuators.

Mckibben Muscle  McKibben muscles show great similarity with biological muscles. They have very good power to weight ratio. Moreover, they can be used in rigorous environment whether it is dusty, humid or even wet. In contrary to conventional electrical or mechanical actuators which require very clean and dry place. Despite of having hysteresis phenomenon and requirement of threshold pressure, Mckibben muscle is the most studied and used as pneumatic artificial muscles. One of the reason is that this kind of muscle is very easy to fabricate, maintain and mass produced. For these reasons, we have considered Mckibben muscles for our actuators in our work. The following section is dedicated to present a review of different modelling attempts of the Mckibben muscle along with its resemblance to the biological muscle. Mckibben muscle is composed of an inner tube surrounded by a double helix braid, characterized by its initial braid angle (α₀) as illustrated in Fig. 1.23.

![Figure 1.22 – Mckibben Muscle](image)

The Mckibben muscle behavior depends largely on the dynamics of the inner tube, surrounding braided sleeve and the pressure supply. In literature, several models of Mckibben muscles can be found. The most prominent are [Chou 1996, Tondu 2000, Colbrunn 2001]. In [Chou 1996, van Ham 1996a], the pneumatics are taken into account in the modelling while the muscle is subjected to a dynamic load. In [Colbrunn 2001], a complex relation of the valve is included in the model of the muscle. In most cases however, the pressure is considered as an input to the system. As indicated in [Schroder 2003], it is interesting to note that these three models, even though they do not use exactly the same parameters, can be transformed into each other. In this section we will present the most referred model which is the
Chou-Hannafof model [Chou 1996] :

\[ F_m = \frac{\pi d_o^2 p_m}{4} \left( \frac{3}{\tan^2 \alpha_o} (1 - \varepsilon^2) - \frac{1}{\sin^2 \alpha_o} \right) \]  \hspace{1cm} (1.27)

with the muscle force \( F_m \), the resting diameter \( d_o \), the muscle pressure \( p_m \), the rest braid angle \( \alpha_o \) and the elongation \( \varepsilon \). The pressure in a McKibben muscle is modelled by Boyle Gay Lussac’s law, while the generated force is defined using a force balance. The parameters \( \alpha_o \) used in Eq. (1.27) is not a well defined parameter, since it is not constant over the length of the muscle and it is hard to measure. The results of this model are good in the high-pressure range typically above 2 bar and it is suitable to model Rubbertuator like Festo’s MAS. However, in this thesis, the model proposed in [Tondu 2000] is taken as the base. This model includes the cylindrical volume error correction and has the close resemblance to biological muscle. It could also be applied in the application of smaller pressure range (1-5 bar). This model is deal in detail in the Chapter 3.

McKibben muscles resemblance with biological muscles has been studied in [Klute 1999] where the experimental based comparison was made between pneumatic and biological muscles. The McKibben muscles are compared to the Hill model, a model describing the behavior of biological muscles in [Tondu 2006]. The Hill model describes the relationship between muscle shortening velocity \( V \) and its corresponding tension, \( F_{Hill} \) which can be mathematically defined as follows

\[ (F_{Hill} + a)V = (F_0 - F_{Hill})b, \]  \hspace{1cm} (1.28)

where \( F_0 \) is the isometric contraction force at zero contraction ratio in given stimulation conditions. \( a \) is a constant having the dimensions of a force and \( b \) is a constant having the dimensions of a velocity.
1.3. Artificial muscles

Figure 1.24 – Characteristics of a typical pneumatic McKibben muscle (of initial length $l_0 = 335\,mm$, initial radius $r_0 = 10\,mm$ and initial braid angle $\alpha_o = 23^\circ$), (a) Tension-Displacement curves at constant pressure 1, 2 and 3 bar, (b) Tension-Velocity curve at constant 2 bar pressure.
2.1 Introduction

As discussed in the Chapter 1 in 'The state of the art' where various types of artificial muscles are presented, conducting polymer actuators (CPAs) are found to have several advantages when compared to other kinds of artificial muscles. They show faster response and require less voltage up to $2V$. Furthermore, they are lightweight and compliant. These advantages make CPAs as one of the best potential choice in biomedical applications. It was shown in Chapter 1 Fig. 1.1a, they can produce large strain and stress and work in electrolytes or biological fluids [Daneshvar 2014, Harlotte 2002]. CPAs can be configured as free-standing or bilayer and trilayer actuators. In the free-standing CPAs, a single film is submerged in liquid electrolyte polymer and the volumetric expansion can be measured directly [Melling 2002]. Such actuator is characterized by out-of-plane strain. However, bending actuators are usually employed for most of the practical applications as they can take advantage of much higher in-plane strains. The bending motion is achieved by laminating an electromechanically active conducting polymer with an inactive substrate creating bi-layer or tri-layer structures. During volumetric expansion of the polymer, stress gradient is generated at the interface subsequently leading
to bending. Most commonly studied configuration is bilayer structures, but their operation requires a counter electrode which motivates the use of trilayer devices for application purposes. In our laboratory at LAASCNRS, PEDOT :PSS trilayer CPAs are extensively studied and reported in [Simaite 2015a]. Various advantages of PEDOT :PSS trilayers CPAs and the challenges are compared to the most commonly used conducting polymer based actuators. In [Simaite 2015a], the author has reported, in detail, about the structure, fabrication, basic functioning and the characterization of the actuators based on PEDOT :PSS triayer CPAs. Since scope of my thesis is to study the dynamical model of such actuators and propose a control strategy for such actuators. For the sake of better understanding and completeness, a very brief introduction of the PEDOT :PSS trilayer CPAs are presented.

2.1.1 PDOT :PSS Ionic liquid actuator

poly(3,4-ethylenedioxythiophene) polystyrene sulfonate (PEDOT :PSS) based actuators are trilayer conducting polymer actuators (CPAs). 2.1 Fig. 5.1 shows the structure of the trilayer actuator. So far, Polypyrrole (PPy) is one of the most used conducting polymer for applications in CPAs. It can produce volumetric swelling of typically 2 – 3% during oxidation. In comparison to others, polypyrrole based actuators produce largest displacements and forces [Gaihre 2013, Temmer 2013] and maximum electrochemical strains of up to 29% [Hara 2004, Hara 2005]. Despite having all these features, electrical conductivity of polypyrrole decreases by 2 - 3 orders of magnitude in the reduced state. This reduces the over all active part of the film which ultimately results into electrochemical creep during actuation [Hara 2011]. Furthermore, PPy films are usually very rigid leading to low ion diffusion speed and slow actuation rates [Otero 2003, Temmer 2013]. Therefore, use of polythiophene derivatives as electrodes is now preferred which motivates the consideration of actuators based on poly(3,4-ethylenedioxythiophene) (PEDOT) and one of its possible counterions - polystyrene sulfonate (PSS). The performance of the actuators based on PEDOT in comparison to PPy are still not so significant. Similar strains and strain rates are expected [Temmer 2013]. However, PEDOT is a well known polymer for its chemical, electrochemical (in doped state) and thermal stability. PEDOT also has high electrical conductivity that could reach up to 2000Scm$^{-1}$ [Mengistie 2014]. Furthermore, it shows faster actuation. It is because of doping with the immobile anions (DBS, PSS, etc.) makes it more soft and porous which lead to a better ion diffusion [Otero 2003, Temmer 2013, Zainudeen 2008]. Therefore, PEDOT could eventually emerge as an advantageous alternative to conventional CPAs electrodes.

2.1.2 Characterization of Ionic actuator

The mechanical work produced by the Ionic actuator is mainly due to the processes involved in the volume changes in conducting polymers during their redox reactions. While polypyrrole (PPy) secondarily doped with immobile anion (DBS)
2.1. Introduction

during its synthesis, is widely studied, the ion transport and volume expansion of the PEDOT:PSS is barely studied. So, in order to explain the behaviour of PEDOT:PSS in ionic liquid, the current understanding of the actuation mechanisms of PPy(DBS) based actuators is used. Characterization measurements were mostly done with trilayer actuator (PEDOT:PSS/mPVDF/PEDOT:PSS) clamped at one end (Please refer to the Fig. 5.2), at one end and supplied with a voltage in $[-2V + 2V]$ range.

The actuators were cycling by applying a potential waveform between two electrodes and the response was recorded by recording the video of the bending or by laser displacement sensor. Detail set-up and explanation could be found in Appendix A. The change in the displacement was then extracted from the video and is shown in Fig. 5.3a. The transferred current was simultaneously measured and was
used for calculations of the dissipated power (Fig. 5.3b).

![Figure 2.3](image)

**Figure 2.3** – Merged images of the actuator at its extremities during actuation applying square wave with frequency of 50mHz and 2.0V amplitude. Blue and red actuators show its maximum and minimum displacement position, green dots show the tip position calculated from recorded videos. Actuator displacement profile in time is shown in the figure below. Actuator is bending towards the negative electrode. (b) Applied voltage, current and power dissipation measured during the actuation. Figure adopted from [Simaite 2015a]

**Strain** The actuator bending is often expressed as strain. The use of displacement and curvature to characterize the performance of the actuator is quite trivial as they do not take into account the dimensions of the actuators. Strain can be defined simply, in the context of artificial muscles, as a displacement normalized by the original material length in the direction of actuation [Madden 2004b]. Measurement of strain can be done by direct means in the case of free-standing polymer films or indirectly using bending beam theory. Sugino et al. in [Sugino 2009] proposed an equation to estimate the difference in strain ($\varepsilon$) during bending of the actuator

$$\varepsilon = \frac{2DW}{L^2 + D^2}, \tag{2.1}$$

where $L, W$ are the length and the thickness of the actuator and $D$ is the measured displacement. The Eq. 5.1 is valid for a simplified geometrical model assuming low displacements, it is still viable for the measurements in the case of PEDOT :PSS based actuators. Due to the mechanisms other than ion transport involved in volume expansion, irreversible expansion (creeping) is often observed as shown in Fig. 5.4a. The term "active strain" is defined as the difference between the maximum peak strain and the following minimum strain of each voltage cycle (shown in Fig. 5.4a as $\delta e_{max}$).
2.1. Introduction

**Strain rate** Strain rate is the measure of the speed of the actuator and thus it is another important characteristic of the actuator. Formally speaking, it is the average change in strain per unit time during an actuator stroke [Madden 2004b] (Please refer Fig. 5.4a. It has been observed that the strain rate expressed in this manner is highly dependent on the actuation frequency. In fact, speed of the actuation is not constant and its bending significantly slows down once 70% (approx) of the maximum strain is reached. Therefore, sometimes for comparison purposes, the maximum speed of expansion is used. It is calculated at each time interval ($\delta \varepsilon / \delta t$ as shown in Fig. 5.4b). PPy based actuators typically have strain rates of approximately 1%/sec. The strain rate is mostly limited by how quickly ions can move through the polymer film. Therefore, size of the ion, the microstructure of the polymer and history of the cycling have large influence on the speed of actuation [Melling 2002, Pytel 2007]. Another implication of the diffusion model is that it takes more time to diffuse deeper into the film and the full depth might not be reachable.

![Figure 2.4](image)

**Figure 2.4** – (a) Actuator bending profile shown as calculated strain versus time. Strain is calculated using Equation 5.1 for every point detected during video processing. Min to max strain ($\Delta \varepsilon_{max}$) is defined as strain difference between extremities during one actuation period ($T$), strain rate is a ratio of ($\Delta \varepsilon_{max}$ and $T/2$). (b) The speed of the actuator is calculated at every point as $\delta \varepsilon / \delta t$. Figure adopted from [Simaite 2015a]

2.1.3 Control reviews of Electroactive polymer actuators

Closed-loop control of artificial muscle is a difficult challenge due to the general non-linear character of the artificial muscle dynamic contraction but also due to its associated feeding requirement. Among possible energy choices, electric tension is particularly relevant as a clean, simple supply mode easy to put into work, especially when a quick contraction can be got from low voltage and low electric energy. Ionic polymer bending artificial muscles belong to this class of low energy electroactive polymeric actuators. While, in their earlier development, such bending strips needed a liquid environment for contracting, the recent use of non-evaporable ionic liquid
made possible their use in open air [Lu 2002, Bennett 2004] and so expanded their application field. Although the positioning of this kind of actuator can be controlled in open-loop with an input voltage, the typical "drift"-phenomenon of the actuator under a constant input voltage - i.e. the fact that the actuator continues to slowly bends without giving the impression to converge towards a steady-state position - makes necessary the need of a closed-loop control. Several attempts have been made for developing closed-loop control for the accurate positioning of this bending artificial muscle including linear PID-control [Yao 2008], feed-forward control [John 2010], sliding mode control [Wang 2013] or fuzzy and neuro-fuzzy control [Druitt 2014]. The highly non-linear character of the bending phenomenon would actually leads to give priority to sophisticated control approaches as done by Druitt and Alici in their paper [Druitt 2014]. Alternatively, in this preliminary work on soft actuators, we would like to analyze the relevance to come back to simpler control approaches. The motivation for such approach comes from our work made on the control of robots actuated with the pneumatic McKibben muscle. Due to its highly non-linear nature, several sophisticated control approaches have been tested such as sliding mode control, fuzzy control or biomimetic control. Although interesting results were obtained for various trajectories, all these approaches actually suffer a degree of complexity due to the relatively high number of parameters or rules to tune without to be sure to keep the same level of performances in a large field of experimental conditions. More recently, we attempted to control a single artificial muscle and a joint made of two antagonist pneumatic McKibben muscles by considering a simple I-controller taking advantage of the own stiffness and damping of any artificial muscle [Tondu 2016]. The electroactive polymers considered in our work contracts by bending while the McKibben fluidic muscle contracts along its long axis. A linear closed-loop control approach with a limited number of parameters are proposed to apply to a tri-layer PEDOT :PSS/PVDF/ionic liquid sample [Simaite 2015b]. Carbon nano-tubes [Simaite 2016] have been added in order to increase its resistance to delamination in the full working range $[-2\,V, +2\,V]$, as illustrated in Fig. 2.2. In a broad sense, the originality of our approach is based on the intuitive idea that the classic PID can be especially adapt to the peculiar nature of any artificial muscle. Such an approach finds its place, according to us, in current thinking about redefinition of PID gains tuning rules as done, for example, by Fruehauf et al. [Fruehauf 1994] — mentioned in [Druitt 2014]. The choice of a PI control, as proposed in this thesis, is motivated by the identified model developed in section 5.2. Before we attempt to apply it for steps and sine-wave trajectories in the next section, by means of the classical experimental set-up shown in Fig. 2.5. The sample tip positioning is measured using a laser with respect to a zero horizontal position, and the feedback control combines a NI-card with the LabView software.
2.2 Non-linear Identification of the Artificial Muscle

In a recent article [Tondu 2015], we attempted to propose a general definition of any artificial muscle as an open-loop stable system when input is the muscle activation variable and output is one positioning dimension. In the case of a tri-layer bending polymeric sample, the input is an electrical voltage while the output is generally specified as a vertical distance measured at the tip of the sample. The open-loop stable character of the artificial muscle points the way towards open-loop identification, especially from step recording of its positioning dimension in response to various step amplitude. Such an identification problem can be tackled by using various methods as the ANFIS-NARX paradigm, recently applied to IPMC (Ionic Polymer Metal Composite) [Annabestani 2015] for getting an advanced non-linear model of the full bending actuator or, in a more conventional way, classical techniques of linear system identification applied to the time variation of the sample: in [John 2010], the authors are proposing a sixth-order transfer function with a constant gain for identifying their polypyrrole tri-layer actuator.

2.2.1 Non-linear model derivation from the first order linear model

Our approach is a bit different in the sense it is based on a preliminary observation of two characteristics of any open-loop step-response of the type of bending actuator we try to control: whatever the u-control voltage, no overshoot occurs and the slope at the origin is never close to zero. In the framework of linear systems, these two points are characterizing a first-order system. If, for low voltage open-loop steps, a linear first-order system can give a satisfying model, as illustrated in Fig. 2.6a for +0.25V and 0.5V-steps, this is not the case for upper voltage open-loop steps due, in particular, to the "drift"-phenomenon which makes the convergence to the steady-state slower than expected for a linear system. This is the reason why we propose the following non-linear model directly derived from the expression of a first-linear model, as follows:

\[ x(t) = k(1 - e^{-\frac{t}{\tau}})u \]  \hspace{1cm} (2.2)

where \( u \) is the step amplitude, \( x \) is the artificial muscle tip position, and \( k \) is a...
Table 2.1 – Identified parameters of the proposed non-linear model

<table>
<thead>
<tr>
<th>u (V)</th>
<th>k (mm/V)</th>
<th>T (s)</th>
<th>r</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.25</td>
<td>2.5</td>
<td>6</td>
<td>1</td>
</tr>
<tr>
<td>0.5</td>
<td>2.5</td>
<td>5.5</td>
<td>1</td>
</tr>
<tr>
<td>0.75</td>
<td>2.45</td>
<td>4</td>
<td>0.8</td>
</tr>
<tr>
<td>1</td>
<td>2.5</td>
<td>3</td>
<td>0.7</td>
</tr>
<tr>
<td>1.25</td>
<td>2.5</td>
<td>2.5</td>
<td>0.6</td>
</tr>
<tr>
<td>1.5</td>
<td>2.0</td>
<td>2.15</td>
<td>0.475</td>
</tr>
<tr>
<td>1.75</td>
<td>1.8</td>
<td>2.15</td>
<td>0.45</td>
</tr>
<tr>
<td>2</td>
<td>1.75</td>
<td>2.1</td>
<td>0.4</td>
</tr>
</tbody>
</table>

gain, T a time constant-like parameter and r a positive coefficient lower than 1, without dimension. If r = 1, the system behaves like a first order linear system. For each considered open-loop u-step, k was identified as the ratio between steady-state position over u, and the T and r parameters were identified by successive trials, T being chosen for matching rising slope while r was chosen for matching the final convergence speed. Fig. 2.6a gives the result of this identification in the case of positive u-steps whose corresponding estimated values for k, T and r are given in Table 1. A linear interpolation between identified parameter values for getting continuous change for k, T and r is proposed in Fig. 2.6b. It can be noted that we voluntarily limited the interpolation to the range [+0.25V, +2V] : if it is clear from identified step responses at low voltage, that the assumption of a linear behaviour of the bending artificial muscle at very low voltage is relevant, data are however missing about k and T parameters in this voltage-range. We see little problem with this situation due to the fact that control voltage close to zero is rarely used in practice.

![Figure 2.6](image)

Figure 2.6 – Nonlinear open-loop identification of the actuator: (a) Comparison between x-position in response to u-voltage steps (full line) — only positive u-steps are considered — and the proposed non-linear model (dashed line), (b) Variation of the parameters (T, k, r) of the proposed non-linear first-order for a u-control voltage varying in the range [+0.25V, +2V]
2.3. PI-closed loop control

2.3.1 Linear tuning and non-linear effects

It is well known that a first linear system can be controlled in closed-loop by a PI-controller whose proportional and integral gains can be determined from a direct comparison between the resulting characteristic polynomial and this of a standard second order system. Let us write the PI-control as follows:

\[ u = k_P(x_d - x) + k_I \int_0^t (x_d - x)(\tau)d\tau \quad (2.3) \]

where \( u \) is now the closed-loop control voltage, \( x_d \) the desired output, \( x \) the real output and \( k_P, k_I \) are constant gains. For a linear first order, open-loop system, in the form of the transfer function \( \frac{k}{1+Ts} \), the characteristic equation resulting from the PI-controller is given by:

\[ 1 + \left[ \frac{1 + kk_P}{kk_I} \right] s + \left[ \frac{T}{kk_I} \right] s^2 = 0 \quad (2.4) \]

whose terms can be identified with those of the classical form: \( 1 + 2z\omega_n s + (1/\omega_n^2)s^2 = 0 \), where \( z \) is the damping factor and \( \omega_n \) the undamped pulsation of the corresponding linear second order. Because it is also well known that response time of a linear second-order system without zero is, for a given \( z \), inversely proportional to \( \omega_n \), it is then possible to choose \( z \) and a given response time \( T_r \) — for example, the time beyond which the response keeps inside the 0.95/1.05 desired position-range — for deriving the gains \( k_P \) and \( k_I \) as follows:

\[ k_P = \frac{1}{k} \left[ \frac{2z(\omega_n T_r)T}{T_r} - 1 \right] \quad (2.5) \]
\[ k_I = \left[ \frac{(\omega_n T_r)^2 T}{k T_r^2} \right] \quad (2.6) \]

In the limit-case \( z = 1 \) — corresponding to the quickest step-response before overshooting — the \((\omega_n T_r)\)-term is equal to about 5 and we can so compute \( k_P \) and \( k_I \) for any given \( T_r \). This approach has, however, a severe limitation: the presence of a zero in the closed-loop transfer function equal to \((-k_I/k_P)\) whose effect can be an overshoot impacting also the response time. If we apply this approach to the linear version of the identified model of our sample developed in section 5.2 by considering \( r = 1 \), constant \( k \) and \( T \) parameters respectively equal to the mean value of identified \( k \) and \( T \) parameters of Table 2.1, we get, for \( z = 1 \) and \( T_r = 2s \), the result shown in Fig. 2.7a in the case of a 1mm desired step position — we get \( k_P \) equal to about 8.1V/mm and \( k_I \) to about 10.65V/mm.s\(^1\), while \( k \) is about equal to 2.2mm/V and \( T \) is equal 2 to about 3.7s. The response time is a bit greater than the expected 2 seconds with, however, a slight overshoot exceeding a bit 5%. If we now apply the same values for \( k_P \) and \( k_I \) to the non-linear model proposed, it is interesting to remark that the overshoot is now negligible with, as
a consequence, a reduced response time divided by more than 2. Such a way for tuning the controller gains is however not able to take a strong constraint peculiar to the considered artificial muscle: control voltage control must be lower than $+2V$, in absolute value, which is clearly not satisfied as shown in Fig. 2.6b.

![Figure 2.7 – Simulation of a closed-loop PI-linear control applied to a mean linear model of the artificial muscle and to the proposed non-linear model : (a) Simulation of step responses — circles correspond to the time beyond which response belongs to the 0.95/1.05 desired position-range, (b) Corresponding control voltage.](image)

### 2.3.2 Taking into account voltage constraints

Theoretically, closed-loop control should avoid to reach the bounds of the permitted control range but, in the case of our tri-layer sample, the consequence would need to adapt the controller gains — or rules if a logics-based controller is considered — to the desired position. The consequence can be a great complexity as already mentioned in the case of the recent study by Druitt and Alici [Druitt 2014].

Our alternative approach proposes to consider the $[−2V, +2V]$ voltage range as a practical range whose $−2V/ +2V$ bounds can be reached without damage for the artificial muscle at the condition that the steady-state position does not require to indefinitely stay at one of these bounds. From open-loop identification developed in section 5.2, this condition is satisfied by limiting the desired position in the range $[−3mm, +3mm]$. If we admit that closed-loop control can be performed with saturation periods, it is clear that classical rules for tuning a PID-type controller cannot be applied anymore. Our approach for tuning the PI-gains is based on the fact that, on the one hand, only two gains are considered and, on the other hand, on the knowledge of the identified non-linear model. In the case of steps, the following two-stage strategy is proposed, where $u_{lim}$ designates the maximum value for a safe control:

1. A reference $x_{ref}$-position is chosen, typically at the middle of the positive, or negative, admissible range. The gain $k_P$ is then tuned according to the following
2.3. PI-closed loop control

relationship:

\[ k_P = \frac{u_{lim}}{x_{ref}} \]  

(2.7)

Such a \( k_P \)-gain leads to a control value equal to \( u_{lim} \) at \( t = 0^+ \) just before the integral action starts to play its role:

2. For the same reference position, the gain \( k_I \) is then tuned by simulation of the PI closed-loop controller applied to the proposed non-linear model with, as an aim, a limited overshoot combined to the lowest possible response time. The obtained \((k_P, k_I)\) couple can then be applied to lower and upper desired positions.

Let us consider, in our case, a reference equal to \( 1 \)mm and \( u_{lim} = +2V \). We deduce : \( k_P = 2V/mm \). As shown in Fig. 2.8a, a choice of \( k_I = 1V/mm.s \) leads to a response time of about \( 2s \) with no overshoot. As expected, the control voltage is saturated at \( t = 0^+ \) and then tends to a non-saturated value. On the same plot, we considered the simulated step-response for \( x_d = 0.5 \)mm : no overshoot occurs and response time is still close to \( 2s \). On the same plot, the corresponding real step responses are also given. There is some discrepancy between simulated and real responses. This is, especially due, according to us, to the way the non-linear differential equation has been solved : we used Matlab software and its ode113-solver which, in the case of our problem, generated solution with a mean sampling time of about \( 300ms \) when the Labview control program was sampled at \( 10 \) ms.

It is, however, interesting to check that the real step response both for \( 1 \)mm and \( 0.5 \)mm exhibit no overshoot, as expected. We give in Table. 2.2 the performances in step response time and overshoot for steps between \( -3 \)mm and \( +3 \)mm whose corresponding position and control versus time are respectively shown in Figs. 2.9a and 2.9b. In every case, the same \((k_P, k_I)\)-couple equal to \((1V/mm, 2V/mm.s)\) was used. For any desired position greater, in absolute value, than \( 1 \)mm, the control is initially saturated to \( +2 \) or \( -2 \) volts before almost instantaneously leaving this value limit. In the case of bounds \(-3/ +3 \)mm, the control value is initially maintained to the voltage limit during several seconds. This limitation of our actual electroactive artificial muscle makes impossible to get short time responses for desired positions in the lower and upper-range between \(-3 \) and \(-2 \)mm and \(+2 \) and \(+3 \)mm. It is worthy to note that for steps less than \( 1 \)mm, in absolute value, another tuning of the gains would make possible to get a faster contraction but our first aim in the reported experiments was to analyze the possibility of keeping the same gains whatever the step-value and, especially, to check the very limited overshoot resulting of such an approach, as verified in Table. 2.22. We also give in Fig. 2.9c the steady-state error for positive steps \( 0.5, 1, 2 \) and \( 3 \)mm : in every case, the steady-state error belongs to the \([-0.02, +0.02 \)mm]-range which exhibits the very positive role of the integral action.

2.3.3 Stability of the PI-controller

A linear first-order system with a PI-feedback control is always stable whatever the choice of the positive \( k_P \) and \( k_I \) gains because its characteristic polynomial is
Chapitre 2. Identification and control of Electroactive polymer

Figure 2.8 – Simulation of the closed-loop positioning of the bending actuator by means of a PI-controller with constant \((k_P, k_I)\)-gains: (a) Comparison between real (full line) and simulated (dashed line) step-responses for a desired +0.5\,mm position and a desired +1\,mm position, (b) Corresponding real and simulated controls.

Table 2.2 – Estimated response time and overshoot for desired steps in the range \([-3\,mm, +3\,mm]\)

<table>
<thead>
<tr>
<th>(X_d(\text{mm}))</th>
<th>-3</th>
<th>-2</th>
<th>-1</th>
<th>-0.5</th>
<th>+0.5</th>
<th>+1</th>
<th>+2</th>
<th>+3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Response time(s)(95%)</td>
<td>24.2</td>
<td>6.71</td>
<td>2.01</td>
<td>2.05</td>
<td>1.99</td>
<td>1.97</td>
<td>7.22</td>
<td>20.05</td>
</tr>
</tbody>
</table>

a second-order one with positive coefficients. At the opposite, the same first order system with a three-term PID-feedback control is unstable for a \(k_I\)-gain whose value limit is given by the Runge-Kutta criterion. In the case of our non-linear artificial muscle model, let us assume that the artificial muscle has been put in the equilibrium position \(x_{equ}\) by means of a control voltage equal to \(u_{equ}\) which must verify the steady-state relationship: \(x_{equ} = k u_{equ}\). Let us assume that we move the system from this equilibrium position, briefly and within a short distance, in order that we can assume that the parameters \(k, r\) and \(T\) keep constant. As a consequence, the PI generates a closed-loop control voltage given by Eq. 2.3 where \(x_{equ}\) has to be written instead of \(x_d\). By deriving Eq. 2.2, we get:

\[
\dot{x} = k(1 - e^{-\frac{r}{T}})\dot{u} + (\frac{r}{T}) t^{r-1}(e^{-\frac{r}{T}})u
\]  

(2.8)

By putting into Eq. 2.8 the expression of resulting from the time derivative of the control equation imposed by the PI as follows: \(\dot{u} = -k_P \dot{x} + k_I (x_{equ} - x)\), the following differential equation of the closed-loop system results:

\[
\dot{x} \left[ 1 + kk_P(1 - e^{-\frac{r}{T}}) \right] = kk_I(x_{equ} - x)(1 - e^{-\frac{r}{T}}) + (\frac{kr}{T}) t^{r-1}(e^{-\frac{r}{T}})u
\]  

(2.9)
2.3. PI-closed loop control

![Figure 2.9 – Closed-loop positioning of the bending actuator by means of a linear PI control with the same constant \((k_P, k_I)\)-gains: (a) Step responses in the range \([-3\text{mm}, +3\text{mm}]\), (b) Corresponding variation of control voltage for positive desired positions, (c) Corresponding steady-state errors.](image)

where \(k, r,\) and \(T\) depend on \(u\) according to the relationship expressed in Eq. 2.3. In the neighbourhood of infinite for time \(t\), due to the fact that, for \(0 < r \leq 1, e^{-t/r}\) and \(t^{-1}e^{-t/r}\) tend to zero when \(t\) tends to infinite, Eq. 2.9 is reduced to:

\[
\dot{x}(1 + kk_P) = kk_I(x_{equ} - x) \tag{2.10}
\]

This last equation is similar to the one resulting from the closed-loop control by a PI of a first-order linear system in the form : \(\dot{x} = k(1 - e^{-t/T})u\). We can so conclude from the accurate knowledge of the proposed actuator model that the considered PI-controller makes the closed-loop system stable. A very interesting practical consequence is that any blind tuning of the two considered gains cannot put the closed-loop system into instability, whereas a blind tuning of the three gains of a PID could do it.

2.3.4 Tracking performances

The method for tuning the \((k_P, k_I)\)-gains proposed in section 2.3.2 is not applicable to the choice of a trajectory to be tracked due to the fact that the \(k_P\)-gain
cannot be derived from a simple saturation constraint as expressed in Eq. 2.7. An alternative way for tuning the two gains can however be proposed in this case after having remarked that, in steady-state, the considered actuator model behaves like a first order whose only gain $k$ and time constant $T$ are depending on control $u$. We can indeed write the following equivalence in the neighbourhood of infinite time, for $0 < r \leq 1$ and whatever $T$:

\[
(1 - e^{-\frac{tr}{T}}) \approx (1 - e^{-t/T})
\]

\[
t = + \inf 
\]

(2.11)

(2.12)

eq 9 because, when $t$ tends to inf, $(1 - e^{t/T})(1 - e^{t/T})$ tends to 1. As a consequence, and considering mean constant values for $k$ and $T$, we can deduce, from classical results on tracking errors of first linear order systems in closed-loop with a PI, the following estimation of the tracking error $\varepsilon_V$ in response to a constant slope:

\[
\varepsilon_V = \frac{V}{k_{\text{mean}}k_I}
\]

(2.13)

where $V$ is the value of the slope, $k_{\text{mean}}$ is the mean value for $k$, either in positive or negative $u$-range and $k_I$ is the already defined integral gain. We give in Fig. 2.10 tracking results obtained for various sine-waves. In the case of the tracking of a sine-wave of $\pm 2 \text{mm}$, with a period of 20s, a near constant tracking error can be observed in a large portion between sinus-wave extrema, as shown in Fig. 2.10f and on the close-up view of the first $\frac{3}{4}$ period of Fig. 2.11a : from time equal to about $8s$ to a time equal to about $12s$, the tracking error $(x_d - x)$ varies, in absolute value, between about $0.06 \text{mm}$ and $0.08 \text{mm}$. By estimating the corresponding slope, in absolute value, to about $0.6 \text{mm/s}$ and considering a mean value $k_{\text{mean}}$ roughly equal to about $2.1 \text{mm/V}$, and because a $k_I = 5$ was considered in the reported experiment, from Eq. 3.13, $\varepsilon_V$ can then be estimated, in absolute value, to about $0.57 \text{mm}$, which is in relative good accordance with the reported experimental values. This emphasizes the relevance of our approach. Another fact is also a direct consequence of the interpretation of the simple dynamic behaviour as a first order system and its PI-control in steady-state : the deviation of the real trajectory from the desired one when curvature is increasing or decreasing. It is indeed well known that, in the case of a first-order system with PI-closed loop, for input time-signals in the form $t^r, r > 1$, the tracking error tends to be infinite with, as a consequence, a maximum tracking error occurring just after each sinus-wave extremum as this can be verified in Figs. 2.10b and 2.10d.

We can now better understand the respective roles of $k_P$ and $k_I$ of our PI-control applied to our bending actuator in trajectory tracking : $k_I$ is the sole gain responsible for the tracking error, when $k_P$ is an additional gain for controlling the transitory state. From conclusion of section 2.3.3, there is no instability risk of increasing $k_I$ to get a better tracking error for constant slope and to limit deviation.
2.3. PI-closed loop control

increasing during non straight-line parts of the trajectory to be tracked, expect that we are limited by the imposed control range \([-u_{lim}, +u_{lim}]\). We show in Fig. 2.10e, and on the close-up view of Fig. 2.11a, the effect of a control saturation imposed, in our case, to \(\pm 2V\). As shown on Fig. 2.11b, the control is saturated just before the system reaches the top of the sine-wave: as a consequence, the system behaves as an open-loop system and cannot continue to efficiently track the sine-wave. At the opposite of the case without saturation, the real trajectory is now below the desired one and the shape of the sine-wave is no more preserved. From all these remarks and because we wanted in this paper to analyze the possibility of a PI-controller with same constant gains for a set of desired trajectories, we considered the following strategy applied to a family of given sine-waves:

— Because \(k_P\) is essentially devoted to transitory state dynamics, it is proposed to choose its value equal to this determined in step gain tuning,

— Considering a sine-wave of the maximum desired amplitude \(k_I\) is chosen equal to the value in order that \(\pm u_{lim}\) is reached at sine-wave top/bottom.

We applied this strategy to sine-wave tracking whose amplitude is between \(\pm 0.5mm\) and \(\pm 2mm\); three examples are reported for which amplitudes and associated time period were chosen as follows: \(\pm 0.5mm\) with a time period of \(5s\), \(\pm 0.1mm\) with a time period of \(10s\) and \(\pm 2mm\) with a time period of \(20s\). Keeping \(k_P\) equal to 2, a \(k_I\) equal to 5 was practically chosen from the observation of a control saturated respectively to \(+2V\) and \(-2V\) when the sine-wave of \(\pm 2mm\) reaches respectively the neighbourhood of its maximum and minimum. From the reading of Figs. 2.10a, 2.10b, 2.10d, 2.10f, it can be seen that the tracking errors are respectively in the ranges \([-0.2mm, +0.2mm]\), \([-0.2mm, +0.15mm]\] and \([-0.35mm, +0.3mm]\) for the three considered examples. It is interesting to remark that the error obtained in the third example (amplitude of \(\pm 2mm\) at a \(0.05Hz\) frequency) is not so far from the result reported by Yao, Alici and Spinks [Yao 2008] with a much faster tri-layer bending actuator — see especially the figure 6 of the mentioned paper.

Conclusion and future work The proposed PI-controller for closed-loop position control of bending actuators was motivated by an original identification of the actuator under the form of a kind of non-linear first-order system as follows:

\[x(t) = k(1 - e^{-\frac{t}{T}})u,\]

where the three parameters \(k, r\) and \(T\) vary with the \(u\)-control voltage. This simple non-linear identified model leads us to justify the relevance of a simple PI-controller for an efficient and stable closed-loop control of the actuator. In the case of a step-response, a simple tuning methodology for the two gains is proposed: it is based on the specification of a safe control voltage range \([-u_{lim}, +u_{lim}]\) and on the possibility given to the control to reach such safe working limits. Given a reference position \(x_{ref}\), belonging to the admissible position range derived from the specification of the control voltage-range, the \(k_P\)-gain is given by the simple relationship \(k_P = \frac{u_{lim}}{x_{ref}}\); the \(k_I\)-gain can then be tuned in order to get the best compromise between no overshoot and quickest response time. As reported, a
Figure 2.10 – Tracking of a sine-wave trajectory by means of a PI closed-loop control with constant gains ($k_P = 2$, $k_I = 5$): (a), (b) Case of a $[-5\text{mm}, +0.5\text{mm}]$-range sine-wave with a time period of $5s$ and corresponding tracking error, (c), (d) Case of a $[-1\text{mm}, +1\text{mm}]$-range sine-wave with a time period of $10s$ and corresponding tracking error, (e), (f) Case of a $[-2\text{mm}, +2\text{mm}]$-range sine-wave with a time period of $20s$ and corresponding tracking error.

Fine tuning for $k_I$ can be done by simulating the PI-controller with the proposed non-linear bending artificial muscle model. Reported results show the relevance of this approach for getting a same couple of gains in the full position range leading to a maximum overshoot of 5% and a response time taking advantage of the imposed safe voltage limits. The PI-controller is also applied to sine-wave trajectory tracking. In this case, we tried to highlight the analogous behaviour of the studied artificial muscle with a linear first-order system when steady state is established and, as a consequence, the fundamental role of the $k_I$-gain for limiting the tracking error. Such a similarity also emphasizes the limitation of our PI-control when sharp trajectory curvature changes occur. Future work will focus on improvements in trajectory tracking, especially, with studying the relevance of variable $P$ and $I$-gains to tackle both with sharp curvature changes and voltage saturation constraints.
Figure 2.11 – Close-up of the tracking performance (a) and associated control (b) in the case of the $\pm 2\text{mm}$ amplitude sine-wave shown on the first $\frac{3}{4}$ period equal to $15s$ — every gradation in time is equal to $0.5s$ (see text).
Chapitre 3

Modeling of the system

3.1 Robotic experimental set-up

In this chapter we describe the kinematic structure of the 7Dof anthropomorphic arm, a presentation of the hardware on which is based the control architecture, and then we provide a detailed original model of the pneumatic actuation system.

3.1.1 Kinematic structure of the arm

The robot has 7 degrees of freedom (Dof) with three Dofs are at the shoulder and three are at the wrist. One extra Dof is at the elbow. Due to its kinematic structural analogy to human arm, the physiological joint terminology is used rather than the roll-pitch-yaw type mechanical terminology. The External-internal rotation is the rotation of the link along its longest axis. Flexion-extension is the decrease and increase of joint angle. Abduction-adduction is moving away and towards the body sagittal plane. The sequence of Dofs in the arm is described in Fig. 3.1 and Fig. 3.3.

3.1.2 Hardware components

Intensity-Pressure converter (IP) : The arm is pressurized by air supply through servo-valves controlled by Intensity-Pressure converter. The product used in our setup is a Samson I/P 6111 manufactured by Samson Corporation, Frankfurt,
Electropneumatic Converter. This IP is rapid in action producing output pressure in range 0 to 5 bar. The bandwidth of IP is volume dependent and can be as high as 5Hz for volume of $75cm^3$. There are seven joints and a gripper. Each joint and gripper is actuated by a pair of Mckibben muscles and each muscle is controlled by one IP converter and so there are 16 IP converters.

**Encoders/Potentiometers**: There are seven potentiometers at each joint or Dofs to get the joint angle measurement. These analogue potentiometers could be
3.1. Robotic experimental set-up

Figure 3.2 – The 7 Dofs robotic arm

replaced by digital encoders in near future.

Data Acquisition device: CompactRIO from National Instruments (NI) is used for this purpose. This is a reconfigurable and embeddable chassis, integrating an intelligent real-time controller. According to the customer needs, up to 8 different modules can be plugged into the chassis. Depending on our needs 3 kinds of modules are added:

- NI9205: It is an Analog-to-Digital-Converter (ADC) with up to 32 channels, selectable acquisition range (±200mV, ±1v, ±5v and 0v) and a max sampling frequency of 250kS/s. This device will sample the seven potentiometers dedicated to the positioning of the arm.

- NI9265: There are 3 modules which are Digital-to-Analog-Converters (DAC). They have the particularity to provide analog current outputs. The SAMSON’s 6111 electropneumatic converters use this kind of signal. Each module is able to manage up to 4 channels in the 0 to 20mA range at 100kS/s.

- NI9401: Finally the 4 last modules drive bidirectional digital IOs. Theses IOs connected to relatives quadrature encoders will be able to replace more accurately the current analog potentiometers. Up to 12 quadrature encoders can be acquired. The aim of the CompactRIO is to do the link between the computer managing high level control and the actuators of the 7Dof arm. It means that simple functions such as sampling and encapsulation into standard network protocol (UDP), extraction
from standard network protocol (UDP) and signal generation will be performed.

**Development computer**: This is the main computer where modeling, simulation and finally control for the robot arm will be implemented. The computer bi-directionally communicates to the NI module via Ethernet cable for sending control command and receives sensory feedback. Figure 5 shows the overall experimental setup at our laboratory.

![Figure 3.3 – Overall experimental setup](image)

**Linux kernel**: The resulting system is composed of Linux and small co-kernel running side by side on the same hardware. Xenomai co-kernel exclusively controls the real-time applications and real-time interfaces either to kernel-space modules or to user-space applications. These interfaces called skins can mimic pSOS+, VRTX, VxWorks, POSIX, uITRON and RTAI API. Due to this feature, Xenomai is considered as the RTOS chameleon. It is designed to enable smooth migration from a traditional RTOS to Linux without having to rewrite the entire application. Fig. 3.4 illustrates the Xenomai skins architecture. Previously a software was written to control the robot arm manually by using joystick. The software was running under vxworks real time controller. Moving towards open source and linux platform, we have chosen to use Xenomai. Some of the important functions used in previous software have been integrated in the new software architecture by using Xenomai’s vxworks skin.

### 3.2 Modeling of the pneumatic system

There have been several attempts to model the McKibben artificial muscle [Tassa 2013, Tondu 2012, Kothera 2009, Tondu 2006, Daerden 2001]. The difficulty for getting an accurate model is due to a combination of complex phenomena during static and dynamic contraction: shape changing at the muscle tip which lose their initial cylindrical shape for a conical one, mobility and flexibility of the braided sleeve, elasticity of the inner rubber tube, exotic friction in the textile braided sleeve without forgetting, for the pneumatic version of the McKibben muscle, dynamic fluidic phenomena resulting from the artificial muscle volume variation during contraction. When we want to include such a physical model into the closed-loop control of a McKibben muscle actuator, a compromise must be found between the
3.2. Modeling of the pneumatic system

3.2.1 Muscles side dynamics

The following model was considered for relating the dynamic contraction force \( F \) of the artificial muscle to its control pressure \( P \) and contraction ratio.

\[
F(\varepsilon, P) = (\pi r_0^2)P[a(1 - k\varepsilon)^2 - b]
\]  

(3.1)
Figure 3.5 – Muscle geometric parameters: \( l_0 \) initial length, \( r_0 \) radius and \( \alpha_0 \) braid angle

Where,

\[
\varepsilon = \frac{l_0 - l}{l_0}, \\
a = \frac{3}{\tan^2 \alpha_0}, \\
b = \frac{1}{\sin^2(\alpha_0)},
\]

\( l \) being the current muscle length and \( l_0, r_0, \alpha_0 \) are the muscle geometric parameters corresponding to its initial length, radius and braid angle respectively (see [Tondu 2012] for more details). \( \varepsilon \) is the contraction ratio. The parameter \( k \), slightly greater than 1, is empirically chosen for taking into account the conic shape at muscle tips. The viscous coefficient is also experimentally estimated for expressing the naturally damped behavior of the artificial muscle contraction due to the complex kinetic friction inside the braided sleeve. Although hysteresis phenomenon due to dry friction is not included in this model, we think it captures most of the static and dynamic behaviour of the artificial muscle.

3.2.2 Pressure side dynamics

As previously introduced, control pressure in a muscle is provided by an Intensity-Pressure (I/P) converter which translates a current value into a desired pressure value that has to be fed to the muscle. In literature, see [Kelasidi 2011] for a survey, there exist several models of pressure generated in a muscle in terms of the mass of air injected, volume of the muscle and some parameters related to servo valves or the I/P converter (for an example see [Vanderborght 2006]). These models are highly non-linear and eventually become too cumbersome for devising control strategies. We propose a somewhat simpler empirical model to cover the dynamics of the pressure generation from the I/P converter. It is derived from SAMSON I/P converters reported in [Boitier 1996]. Following this model the instantaneous pres-
sure $p$ inside a muscle is represented by a damped second order differential function with a control pressure as input as follows:

$$\ddot{p} + 2w_n \dot{p} + w_n^2 p = w_n^2 p_{des} \quad (3.2)$$

Note that the input of the intensity converter is a current value which is then scaled to the corresponding pressure control input $p_{des}$ in the pressure unit. The above equation is also non-linear as the natural frequency $w_n$ has been empirically identified as a function of the volume of the muscle, $V$.

$$w_n = 2\pi f_v (1/V) \quad (3.3)$$

$f_v$ is the empirically found parameter. The volume of a McKibben artificial muscle can be approached by the following cylindrical volume: $V = \pi r^2 l$, where $r$ and $l$ are respectively the current radius and length of the artificial muscle. By using the relationship Eq.(3.4) as reported in [Tondu 1995], we deduce an expression for the volume of the muscle.

$$r/r_0 = \left(1/\sin(\alpha_0)\right)\sqrt{(1-\varepsilon)^2} \quad (3.4)$$

$$V = \frac{\pi r_0^2 l}{\sin^2(\alpha_0)} (1-\cos^2(\alpha_0)(1-\varepsilon)^2) \quad (3.5)$$

For a second order system, the rise time is inversely proportional to its natural frequency and in the case of our pressure dynamic model, the natural frequency is inversely proportional to the volume. It implies that the bigger the muscle, the larger the rise time. Fig. 3.6 depicts a typical variation of $w_n$ with the joint angle at one of the manipulator joints. If the range of operation for a joint is small i.e range of

\[ \theta \text{ is small, then the corresponding changes in the volume of the muscles as } \theta \text{ varies,} \]
would be small at that joint. In such case, a constant value for \( w_n \) could be chosen for the muscles corresponding to their mean volumes. Here, another interesting point to notice is that for different muscles, pressure dynamics of a larger volume muscle will be slower. The above two points help in trading off between the operating range of the joint and the corresponding easiness of the control strategy.

### 3.2.3 Modeling of Agonistic-antagonistic joint actuator: Symmetric case

Skeletal artificial muscle usually can generate forces in only one direction i.e. they can only pull and not push. When they are applied to the actuation of anthropomorphic limbs, they cannot work alone and hence configured in agonist-antagonist fashion. The similar attempt had been made by the Washington’s Biorobotics Laboratory in the upper limb case [Hannaford 1995] to mimic the complex organization of human musculature. The more recent development in this field using pneumatic muscles can be seen in [B. Verrelst 2005] and [Kurumaya 2016] (Fig. 3.7). However, such an arrangement is not trivial. In order to incorporate a linear skeletal artificial muscle to a revolute joint structure, a basic muscular organization seems to be necessary which is described as follows: the revolute actuator made of two antagonistic artificial muscles illustrated in Figure 9. The two antagonistic muscles are assumed to be identical and attached by means of a non-extensible pulley-chain system, where \( R \) denotes the pulley radius. Both muscles are having an initial \( l_0 \) active length. In the general case, agonistic muscle is controlled by \( u_1 \) and antagonistic muscle is controlled by \( u_2 \), and the resulting actuator angle is \( \theta \). The case of

![Figure 3.7](image)

**Figure 3.7** – From Left to right: Antagonistic biomimetic arm developed at Washington Biorobotic laboratory [Hannaford 1995]. Biped Lucy [B. Verrelst 2005]. Humanoid skeleton powered by artificial muscles [Kurumaya 2016]

symmetric model where both muscles are identical is discussed here first and then the generic model will be presented later. It is assumed that there is no passive tension in the artificial muscles and the joint rest angular position is \( \theta = 0 \). In this initial state both muscles are equally contracted with a same control \( u_0 \) allowing the \( \varepsilon_0 \) initial contraction. Therefore in any particular joint position \( \theta \) the agonist
and antagonist contraction ratios are respectively given by

\[ \varepsilon_1 = \varepsilon_0 + \frac{R\theta}{l_0} \]
\[ \varepsilon_2 = \varepsilon_0 - \frac{R\theta}{l_0}, \]

where, \( \varepsilon_1 \) is the contraction ratio for the agonist muscle and \( \varepsilon_2 \) is that for the antagonist muscle. The actuator torque \( T \) can be written as follows

\[ T = R(F_1 - F_2) \]

where, \( F_1 \) is the agonistic force and \( F_2 \) is the antagonistic force. The application of the fundamental model of equation (4) leads to the following expression:

\[ T = K_1(u_1 - u_2) - K_2(u_1 + u_2)\theta - T_{damp}(u_1, u_2, \theta, \dot{\theta}) \]

with

\[ K_1 = RF_{\text{max}}(1 - \frac{\varepsilon_o}{\varepsilon_{\text{max}}}) \]
\[ K_2 = \frac{R^2F_{\text{max}}}{l_0\varepsilon_{\text{max}}} \]
\[ T_{damp} = R(F_{1-damp}(u_1, \varepsilon_1, \dot{\varepsilon}_1) - F_{2-damp}(u_2, \varepsilon_2, \dot{\varepsilon}_2)) \]

The static component of the actuation torque as expressed in Eq. 3.13

\[ T_{\text{stat}} = K_1(u_1 - u_2) - K_2(u_1 + u_2)\theta \]

has resemblance to the simplified Hogan’s model of the biceps/triceps system [Hogan, 1984] [Hogan 1984]. Inspired from this comparison, three fundamental properties of the artificial muscle antagonistic actuator in analogy with the fundamental biceps-triceps natural muscular system can be highlighted.
**Stable open loop** The equilibrium position $\theta_{equ}$ corresponding to a null static torque can be defined as follows:

$$\theta_{equ} = \frac{K_1(u_1 - u_2)}{K_2(u_1 + u_2)}$$ (3.14)

In this equilibrium position, the stiffness of the actuator $S$ defined as follows:

$$S = K_2(u_1 + u_2)$$ (3.15)

**Two output actuator: torque and stiffness** The actuator can be considered as a double input-output system whose $(u_1, u_2)$ are the inputs and $(T_{stat}, S)$ are the outputs defined as follows:

$$\begin{bmatrix} T_{stat} \\ S \end{bmatrix} = \begin{bmatrix} K_1 & -K_1 \\ K_2 & K_2 \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} \Rightarrow \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} = \frac{1}{2K_1K_2} \begin{bmatrix} K_2 & K_1 + K_2 \theta \\ -K_2 & K_1 - K_2 \theta \end{bmatrix} \begin{bmatrix} T_{stat} \\ S \end{bmatrix}$$ (3.16)

**Maximum actuator torque decreases continuously from an actuator angle limit to the other one** Here we try to establish the actuator angle limit to the maximum contraction of the muscles assuming that each actuator muscle can fully contract to its maximum contraction ratio $\varepsilon_{max}$. If the two muscles are identical, the two actuator angle limits can be defined as follows:

$$[\theta_{min}, \theta_{max}] = [- (\varepsilon_{max} - \varepsilon_o)l_o/R, + (\varepsilon_{max} - \varepsilon_o)l_o/R]$$ (3.17)

Assuming that the inputs $(u_1, u_2)$ are the normalized command and so for every actuator angle $\theta$ belonging to this range (Eq. 3.17), the following expression of the maximum torque can be obtained, corresponding to a maximum control of the agonistic muscle $(u_1 = 1)$ and a null control of the antagonistic muscle $(u_2 = 0)$:

$$T_{max}(\theta) = K_1 - K_2 \theta$$ (3.18)

As clear from the Eq. 3.18, the maximum torque decreases from $\theta_{min}$ to $\theta_{max}$ with the $-K_2$ slope. In contrast to the classical actuators, the presence of the restoring torque term ‘$K_2(u_1 + u_2)\theta$’ gives to the biomimetic actuator a natural compliance which can be actively controlled independently from the actuator position. However, this angular position-actuator torque dependence induces a specific sensitivity of the actuator to gravity.

### 3.2.4 Modeling of agonistic-antagonistic joint actuator: Generic case

Following the human arm model, a pair of artificial muscles can be set up in antagonistic fashion to drive a chained wheel of radius $R$. According to Fig. 3.9, the
resulting actuator torque $T$ can be written as follows:

$$T = R[F_1(\varepsilon_1, P_1) - F_2(\varepsilon_2, P_2)],$$  

(3.19)

where $F_1$ and $F_2$ are the forces of muscles 1 and 2 respectively, defining the antagonist muscle pair. As illustrated in Fig. 3.9, the relationship between $\theta$, the actuator angle and the contraction ratios for each muscle can be expressed as follows:

$$\varepsilon_1 = \varepsilon_{10} + \frac{Rq}{l_0}$$  

and

$$\varepsilon_2 = \varepsilon_{20} - \frac{Rq}{l_0},$$

where $\varepsilon_{10}$ and $\varepsilon_{20}$ are the initial contraction ratios for muscle 1 and muscle 2 respectively corresponding to the zero-angular position. Moreover, we propose to specify the pressures in muscle 1 and muscle 2 as follows:

$$P_1 = P_{10} + \Delta P_1$$  

and

$$P_2 = P_{20} + \Delta P_2,$$

where $P_{10}$ and $P_{20}$ are respectively the initial pressure in the agonist-antagonist muscle and related to zero positioning of the joint. $\Delta P_1$ and $\Delta P_2$, are the control pressures.

Using Eq.(3.1), and neglecting the terms $\varepsilon_1^2$ and $\varepsilon_2^2$, the torque at the joint can be expressed as

$$T = K_1 \Delta P_1 - K_2 \Delta P_2 - K_3 (P_1 + P_2)\theta - K_4 \dot{\theta} + K_5,$$

(3.20)

where,

$$K_1 = (\pi r_o^2)R[a(1 - 2k\varepsilon_{10}) - b],$$

$$K_2 = (\pi r_o^2)R[a(1 - 2k\varepsilon_{20}) - b],$$

$$K_3 = 2(\pi r_o^2)R^2 ka/l_o,$$

$$K_4 = (\pi r_o^2)R^2 f_v/l_o,$$

$$K_5 = (\pi r_o^2)R[(a - b)(P_{10} - P_{20}) - 2ka(P_{10}\varepsilon_{10} - P_{20}\varepsilon_{20})].$$

Figure 3.9 – Pulley-chain driven antagonist muscle actuator made of two identical McKibben artificial muscles. It has the possibility to adapt initial torque at initial zero $\theta$-position by means of $P_{10}$, $P_{20}$, $\varepsilon_{10}$ and $\varepsilon_{20}$.
If $P_{10} = P_{20}$ and $\varepsilon_{10} = \varepsilon_{20}$, $K_5$ is equal to zero. The details of our robot-arm including the dimensions of muscles are given in [B. Tondu 2005] and also given in Appendix B. The antagonist muscle actuator is now considered as a MIMO-system whose inputs are the control pressures $\Delta P_1$, $\Delta P_2$, and outputs are both $\theta$ and the actuator stiffness which is defined as the instantaneous ratio between the current torque variation and the current angular position variation (see Eq.(3.22)). When no gravity effect is considered, the static equilibrium position of the actuator can be directly derived from Eq.(3.20) with zero angular velocity.

$$\theta_{equ} = \frac{(K_1 \Delta P_1 - K_2 \Delta P_2 + K_5)}{(K_3(P_1 + P_2))}$$ \hspace{1cm} (3.21)

With associated stiffness $\sigma_{equ}$ expressed as

$$\sigma_{equ} = -\frac{\partial T}{\partial \theta} = K_3(P_1 + P_2)$$ \hspace{1cm} (3.22)

From Eq.(3.21) and Eq.(3.22), it is possible to remark that the equilibrium position can be changed while keeping the same stiffness by modulating $\Delta P_1$ and $\Delta P_2$ with a constant $\Delta P_1 + \Delta P_2$. In the case of a symmetrical pressure variation in both muscles : $\Delta P_1 = -\Delta P_2 = \Delta P$, the actuator becomes a SISO-system whose corresponding torque $T_{SISO}$, is now given by the following relationship :

$$T = (K_1 + K_2)\Delta P - K_3(P_{10} + P_{20})\theta - K_4\dot{\theta} + K_5$$ \hspace{1cm} (3.23)

where stiffness at equilibrium position is now constant and equal to $K_3(P_{10} + P_{20})$. When the joint angle $\theta$ varies, and assuming that the actuator chain is inextensible, the contraction ratio of each muscle is known and, consequently, the pressure dynamic model, proposed in 3.2.2, can be applied to each muscle. It is important to note that, in the case of relatively small joint muscles, the effect of volume variation with joint angle on pressure dynamics could be negligible. If the range of operation is small, a constant $w_n$ could be chosen for that joint. As previously noted, pressure dynamics of a larger volume muscle will be slower which is, especially, the case of the muscles at the shoulder joint compared to the muscles at the elbow joint.

### 3.2.5 Model of the multi Dof pneumatic arm

This section presents the robot model formally, including the rigid body model of the robot with its pressure dynamics. Let us consider a $n$ degrees of freedom robot with generalized joint angle coordinates $q \in \mathbb{R}^n$. Each joint is actuated by 2 pneumatic muscles, so there will be $2n$ muscles, each one with a pressure $P_i \in \mathbb{R}^{2n}$. The robot dynamics can be represented in standard form as below :

$$M(q)\ddot{q} + C(q, \dot{q}) + G(q) = T(q, P),$$ \hspace{1cm} (3.24)

$$\dot{P} + 2C_p \dot{P} + G_p P = G_p P_{des},$$ \hspace{1cm} (3.25)
where, \( M(q) \in \mathbb{R}^{n \times n} \) is the inertia matrix of the robot, \( C(q, \dot{q}) \in \mathbb{R}^{n \times 1} \) is the coriolis and centrifugal terms, \( G(q) \in \mathbb{R}^n \) is the gravity related terms, \( T(q, P) \in \mathbb{R}^n \) is the torque generated by pneumatic muscles as described in Eq.(3.19). \( C_p = \text{diag}[w_{n_1}, w_{n_2}, ... w_{n_{2n}}] \) and \( G_p = \text{diag}[w_1^2, w_2^2, ... w_{2n}^2] \) are the collection of coefficients of the pressure dynamics of each muscle and \( w_n \) is the natural frequency of the pressure dynamics at the \( i^{th} \) muscle. \( P = [P_1, P_2, ..., P_{2n}]^T \in \mathbb{R}^{2n} \) is the vector of current muscle pressure and \( P_{\text{des}} = [P_{\text{des}_1}, P_{\text{des}_2}, ..., P_{\text{des}_{2n}}]^T \in \mathbb{R}^{2n} \), is the vector of desired pressure \( P_{\text{des}_i} \), the control input in pressure unit given to the I/P converter of the \( i^{th} \) muscle. Any reference trajectory in \( q \) given to the robot has to respect the pressure dynamics whose bandwidth depends on \( w_n \). As discussed in the previous section, if the joint is actuated by larger muscles (having smaller bandwidth) and higher rise time, rapidly varying trajectory would be difficult to track and pose a limiting factor in performing explosive tasks. Limits to the operating range of the joints are obviously decided by the maximum contraction of the spanning muscles. In addition to that, \( w_n \) could be reasonably considered as constant in a limited operating range, removing in this way the non-linearity in pressure dynamics. Apart from this, due to hardware limitation of I/P converter, the control input \( P_{\text{des}} \) is bounded as follows:
\[
U = P_{\text{des}} \in \mathbb{R}^{2n} : P_{\text{des}} \in [P_{\text{min}}, P_{\text{max}}]
\]
(3.26)
Where, \( P_{\text{min}}, P_{\text{max}} \) are the lower and upper bound on control input \( P_{\text{des}} \).

### 3.3 Conclusion

The problem of modeling a robot manipulator actuated by the pneumatic McKibben muscles is addressed here. Each module of the actuator and the robot is considered one by one and their behaviour are studied. Based on this studies and empirical experiments, suitable models are proposed. While the model of McKibben muscles are based on the previous work of B. Tondu [Tondu 1995], the first contribution of this thesis is to propose a model which encapsulates the pressure dynamics in an efficient way. It is done by using a second order differential function whose bandwidth is dependent on the instantaneous volume of the muscles. Even though, the model does not include the effect of dry friction and hysteresis, it covers most of the static and the dynamic behavior. Also a combined model of the entire robotic anthropomorphic manipulator is presented. It is interesting to show the analogy of such kind of robotic manipulators with the conventional electrically driven manipulators. The motor side dynamics are replaced by pressure side dynamics while keeping the structure of the standard manipulator equation (Refer to Eq. 3.24). This model will be used in later chapters for different control strategies while performing different tasks.
This chapter provides an overview of the control techniques that have been so far applied to control pneumatic systems. Then we describe the approaches that we have developed and applied to control our 7 DoF anthropomorphic arm.

4.1 Introduction

The major advantage of the Mckibben muscles is their inherent compliance but that comes at the cost of complications in control strategies. The force generated or transferred to the load by the muscle depends in a non-linear fashion on the actual muscle length and the supplied pressure. Similarly, the stiffness (variation of the force with respect to the contraction of the muscle) is a non-linear function of the contraction and the input pressure. In addition to this, Mckibben muscles suffer from hysteresis. It is mainly due to the friction between the tube and the braid and between the fibres of the braid. Many researchers had tried to address this problem and proposed several control strategies. A very brief overview of such control strategies is presented here.

Overview of control strategies In a very broad sense, it can be observed that most of the authors had used one of the models presented in [Chou 1996, Tondu 2000, Colbrunn 2001]. Capabilities of controlling the Mckibben muscles are explored by means of neural network control [Hesselroth 1994b, Tian 2014, Thanh 2006], fuzzy logic-based control [Thongchai 2001, Ahn 2011],

In the work presented in [Pack 1994], a comparison was made between three different control strategies namely PID, PID tuned by a fuzzy supervisor and non-linear state feedback controller. The Chou-Hannaford ([Chou 1996]) muscle model was chosen for the model and applied to a joint powered by two muscles in an antagonist setup. The conclusion drawn from the simulation results was that the PID controller gives a slow response and the non-linear state feedback controller has the best response. Using the similar experimental set-up, a double loop PI controller is used in [Schroder 2003]. In this work, the torque generated by the muscles, the joint angle and the pressure difference between the muscles were in consideration instead of the force. A double loop of two PI controllers is to control the torque with one loop and the pressure with the other. The torque is estimated by a variation of the classic Chou-Hannaford model by fitting a damping relation.

[Petrovi 2002b] proposed a predictive fuzzy control approach. The predictive fuzzy model is based on their previous work [Petrovi 2002a]. This control approach is applied to a single muscle in simulation. In [van der Smagt 1996], a neural network based feedback controller is used to simulate a robotic arm model. The Chou-Hannaford model was used for the muscle dynamics. Experiments were also performed to verify the control strategy. An adaptive control strategy is proposed by Caldwell [Caldwell 1994], [Caldwell 1995] and verified experimentally. The robot model parameters are embedded in the controller polynomial and the reconstruction of the robot is done by updating an s-domain polynomial in every sample.

[P. Carbonell 2001] has compared the three nonlinear control strategies by simulation in MATLAB. These are robust back-stepping controller, a sliding mode controller and a gain scheduling controller. In this approach, simulation of the controller were performed on a muscle model which was derived by data fitting. Whereas the sliding mode and the back-stepping controller has shown the best error tracking, the sliding mode controller gives a chattered response. Sliding mode controller for tracking has also been used for an antagonist setup [Lilly 2005].

In the literature, one can find some control approaches applied to the multi-link anthropomorphic arm. [Tuijthof 2000] presents the design and control of a 4DoF anthropomorphic arm which is driven by changes in muscle stiffness. Open loop stiffness control is applied on one joint with two muscles. Equilibrium points are derived by a fixed combination of joint angle and rotation stiffness (pressure). The approach was experimentally verified.

Whereas most of the above mentioned experiments used Mckibben muscles, [van Ham 1996b] has used a pleated pneumatic artificial muscle. It is done to overcome the hysteresis problem in a more efficient way. This is discussed in the literature review in Chapter 1. The experiments were conducted on a robotic arm driven by pleated artificial muscles. These muscles are fed by binary valves. A bang-bang algorithm which uses the sign of the error as valve signal and a PWM algorithm were used to control the valves. Later such system had also been used in humanoid
walking application [Vanderborght 2006].

Although relevant results were reported from various control approaches, these generally complex strategies need to tune a relatively large number of parameters and their performances in a large class of movements is rarely discussed. Woods et al. [Woods 2013] proved that it is possible to control a McKibben artificial muscle actuator using a fairly simple method that does not require a system model and nor any tuning of parameters.

In our work, we have considered model based PI controller, model free PID controller and more advanced control strategies of iterative LQR. These developments are discussed in detail in the following sections.

### 4.2 PID control of the pneumatic system

From the review of different control strategies, it is evident that controlling pneumatically actuated anthropomorphic arm is not trivial. However, a simple but reliable model could facilitate the control strategies. Relying on our model presented in Chapter 3, we proposed two control strategies. One is the conventional PID controller while the other method is model-based predictive controller which is comparatively modern. These strategies will be discussed in detail in this section. But before that, we tried to investigate the possibility of model-free control. This approach is based on the work presented in [Tondu 2013] and continued on the same line. The following section presents the discussion and the results of applying a single Integral action on the Mckibben muscle.

#### 4.2.1 Model free single Integral action controller

Since modelling the Mckibben muscle is difficult, it is desirable to find a fairly simple control method to servo it without the requirement of the exact model and without the need of tuning several control parameters as in [Woods 2013]. In a similar spirit, the relevance of a one-parameter linear integral action is analyzed for accurately controlling in closed-loop the contraction of any artificial muscle characterized by its own stiffness and damping. The motivation behind this approach is to propose that the natural stiffness and natural damping of any artificial muscle could play the role, in its closed-loop positioning control, of the P and D-actions of a classic PID. However, comparing the performance of this I-controller approach with that of a full PID controller is not in the consideration. It is possible that, in some particular case, a PI or a PID controller is able to generate a faster response than the simple proposed I-controller, but the primary goal of this work is to highlight the possibility to control the artificial muscle with a one gain I-action with robustness properties. Although artificial muscles are non-linear complex systems, they globally behave like damped ‘active’ springs whose stiffness can be controlled by some variable mimicking the neural activation. This is this fundamental non-linear specificity of any artificial muscle which makes possible the use of a single I-action for which it is well known that it cannot be used for closing the loop of a linear
Now with the assumption that the P and D-actions are now internal to the actuator itself, only an internal I-action is necessary to make equal to zero the steady-state error due to friction and gravity. It is important to note that, as for a classic PID-approach, no dynamic model is required in this approach. It is even expected to manually tune the single integral gain, assuming that increasing it increases the system quickness as long as stability is verified. Our approach, in this framework, is to first analyze the relevance and efficiency of this idea in a theoretical way from a rectilinear artificial muscle model for which we simulate its closed-loop control with a single linear integral action and then report some experimental results performed on the McKibben muscle. Experiments were performed both in step response and sinus-wave tracking, with various embedded load. N. Hogan proposed in his classical 1984’s paper [Hogan 1984] a very simple and elegant model of the active tension of the skeletal muscle as a linear relationship with current length muscle, whose constant slope is proportional to a normalized control variable noted $u$ varying between 0 and 1 and representing the neural activation. We consider that a rectilinear artificial muscle deprived of any passive elongation - which will be particularly the case of the McKibben muscle - and let us define its x-contraction length as the always positive difference between its initial length $l_0$ and its current length $l$. If we assume that the artificial muscle x-contraction length can vary, independently of $u$, from 0 to a maximum value denoted $x_{max}$ at which contraction force is equal to zero, we can consider, in Hogan’s spirit, the following relationship between the static force $F_{stat}$ and length $x$:

$$F_{stat} = uF_{max} \left( 1 - \frac{x}{x_{max}} \right),$$

(4.1) where $F_{max}$ represents the maximum isometric muscle force corresponding to a zero-contraction and a unit-normalized control value. However, such a model driving a given inertia is not asymptotically stable: a damping-factor is indeed necessary to give stability to the system. Let us call this damping force ($F_{damp}$) whose nature depends on the artificial muscle physics. The full artificial muscle model force $F_{dyn}$ versus length $x$ can now be defined as follows:

$$F_{dyn} = uF_{max} \left( 1 - \frac{x}{x_{max}} \right) - F_{damp}(u, x, \dot{x}) \text{ with } 0 \leq u \leq 1; \ 0 \leq x \leq x_{max}$$

(4.2)

Here, the assumption is made that the artificial muscle drives a given load $M$ against gravity and that during contraction its own mobile weight is equal to $m$. The following dynamic equation of the artificial muscle with the load can be deduced:

$$uF_{max} \left( 1 - \frac{x}{x_{max}} \right) - F_{damp}(u, x, \dot{x}) - Mg = (M + m)\dot{x}$$

(4.3)

This equation can be normalized by dividing all terms by $F_{max}$; we deduce the follo-
4.2. PID control of the pneumatic system

wing equation in which \( r_m = mg/F_{\text{max}} \), \( r_M = Mg/F_{\text{max}} \) and \( r_{\text{damp}} = F_{\text{damp}}/F_{\text{max}} \):

\[
u \left(1 - \frac{x}{x_{\text{max}}} \right) - r_{\text{damp}} - r_M = (r_M + r_m)(\ddot{x}/g)
\] (4.4)

Specifying the damping force can be particularly complex due to the soft character of the artificial muscle and to shape changing of materials during muscle contraction. In the framework of our study, a simplified model is considered corresponding to a linear viscous friction force whose constant coefficient will be noted by \( f_v \):

\[F_{\text{damp}}(\dot{x}) = f_v \dot{x}\] (4.5)

However linear or nonlinear may be the damping component, this dynamic model is essentially nonlinear due to the presence of the term in \( u'x' \). The fundamental idea of our approach consists in considering this term as a kind of nonlinear proportional action term and to close the positioning loop by a pure integral action term of constant \( k_I \)-parameter. Considering a desired \( x_d \)-position (constant or variable) and substituting the corresponding closed-loop \( u \)-control into Eq. (4.4) leads to:

\[
K_I \left[ \int_0^t (x_d - x)dt \right] \left[1 - \frac{x}{x_{\text{max}}} \right] - r_{\text{damp}} - r_M = (r_M + r_m)(\ddot{x}/g)
\] (4.6)

Time derivative of this equation (Eq. (4.6)) with respect to time will give:

\[
K_I \left[ \int_0^t (x_d - x)dt \right] \left[-\frac{\dot{x}}{x_{\text{max}}} \right] + K_I (x_d - x) \left(1 - \frac{x}{x_{\text{max}}} \right) - \frac{dr_{\text{damp}}}{dt} = (r_M + r_m)(\ddot{x}/g)
\] (4.7)

Let us assume that the closed-loop system is stable and that, during contraction, \( u \) remains lower than 1 and \( x \) lower than \( x_{\text{max}} \) : when \( t \) tends to infinite, \( x \) tends to some \( x_\infty \) - with all derivatives equal to zero - given by following equation:

\[
K_I (x_d - x_\infty) \left(1 - \frac{x_\infty}{x_{\text{max}}} \right) = 0 \rightarrow x_\infty = x_d
\] (4.8)

In order to check the possibility to converge towards the desired \( x_d \)-position and to analyze the performances of the I-controller during the transient phase, the artificial muscle model with the linear viscous damping is simulated in response to a desired position step from zero to \( x_d = 7\,\text{cm} \), while \( x_{\text{max}} = 10\,\text{cm} \), by considering a viscous ratio \( (f_v/F_{\text{max}}) = 0.5s/m \). Moreover, in order to take into account the signal transmission during the initial setting up of the control, a first order term \((1 - e^{-t/T})\) with \( T = 0.05s \) was added to it. Fig. 4.1 shows the results obtained for a load/maximum force-ratio \( r_M = 0.1 \) while \( r_m = 0.05 \) and various values of the \( k_I \)-parameter. The system appears to be largely stable. \( k_I = 10m^{-1}s^{-1} \) appears as a good compromise to have a faster response with no overshoot. The stability analysis and the method used for finding proper gains are discussed in the appendix C. Fig. 4.2 shows the effect of load-variation for this imposed \( k_I \)-parameter : response time and overshooting depend on the load but no instability appeared.
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Figure 4.1 – Simulation of the closed-loop control of the muscle model with a $k_I$-single integral action for a 7 cm-position step. The plots show the effect of $k_I$-variation in the case of the linear viscous friction model.

The above experiments and simulations constitute an attempt to see the possibilities of proposing a simple and generic control method for a wide range of McKibben muscles. These experiments were done for demonstration purpose rather than actual implementation on our real robot. It is also important to note that this model cannot be considered as an accurate dynamic model of the McKibben artificial pneumatic muscle, due to the fact that the static relationship of Eq. (4.1) is too far away from the real tension-length curve of a McKibben muscle. But, according to us, this model is sufficient to put into light the dynamic performances of the artificial muscle contraction resulting from the proposed friction model. For the implementation of the controller on our real robot, we have used the model proposed in Chapter 3. In the next section, PID controllers using the model of the muscle and the model of the entire robotic arm are presented.

4.2.2 Model based PI controller

Open loop At any joint, a pressure supply to the muscles ($\Delta P$ in the case of SISO model of the joint) generates the torque $\tau$ which ultimately actuates the joint. Considering that the pressure increment $\Delta P$ is the input and the joint angle $\theta$ is the output, a simple schematic of an open loop robot model can be shown as in Fig. 4.3. With the knowledge of the model of the muscles and structure of the manipulator, it is possible to express the inverse position-pressure relationship
4.2. PID control of the pneumatic system

Figure 4.2 – The plots show the effect of load variation in the linear viscous friction case for $k_I = 10 \text{m}^{-1}\text{s}^{-1}$.

Figure 4.3 – Schematic of an open-loop anthropomorphic arm which encapsulates the muscle dynamics and the rigid manipulator dynamics.

which can be schematically presented in Fig. 4.4. In all of our control strategies, position control is preferred. It is well known that a torque control loop with real torque feedback could improve the control quality. In this case, exact modeling describing the behavior of the actuator can be avoided and also the hysteresis and non-linearity could be controlled. But these benefits will come at the cost of the additional torque/force sensors, their IO interfaces with computer and effort of placing wires and sensors into the robotics structure. Therefore, position control is preferred in all our control strategies instead of torque feedback loop. The torque
is estimated using our actuator model. In fact, this model-based estimated torque is embedded inside the inverse position-pressure block in Fig. 4.4.

The controller for a robot such as the one used in our work, is expected to be fast and robust. A conventional PI controller is investigated to deploy for this task. The PID controller can be implemented simply by summing the positional error (deviation from of the measured position from the reference), its derivative and integral (See Fig. 4.5). It is observed that this method is able to control the robot when the motion is very slow, for an example: tracking a ramp with a very small slope. But it is failed to track any rapidly varying trajectories. Moreover, any small disturbance can blow off the system. So, a simple PI controller is not robust and finding a stable controller with good margin is not an easy task. To resolve this problem, a feed-forward PI controller is proposed. The feed-forward term is calculated using the inverse position-pressure block. The block will give a reference pressure with respect to a desired position which is given to the block as an input. The proposed PI controller structure is shown in Fig. 4.7 and expressed mathematically by Eq. 4.9

\[
    u(t) = \Delta P_{des} + K_p(e(t)) + K_i \int_0^t (e(t))dt, \tag{4.9}
\]

where, \(e(t) = q_{des} - q(t)\), \(K_p\) and \(K_i\) are proportional and integral gains respectively.

This method makes use of the knowledge of the model through its feed-forward
4.2. PID control of the pneumatic system

Figure 4.6 – This inverse model block generates desired command pressure from the desired joint position for each joint using inverse position-pressure relationship.

Figure 4.7 – Schematic of close loop PI position controller with $\Delta P_{des}$ as feedforward term.

Block. Then a PID controller designed in this way was found to be much more robust and stable. However, an overshoot can be easily observed in step response. Also the PID controller seems to be stiff and fails to capitalize the benefits of inherent compliance in the muscles.

On the other hand, iLQR approach is known to have the capability to perform predictive control and to tackle the non-linearity in the model [Li 2007], [Tassa 2013]. Moreover, the optimization framework within the iLQR approach could enable the robot to optimize the trajectory in order to make good use of the inherent compliance of the muscles to perform various explosive movements [D.Braun 2013]. Since our goal is to show the capabilities of a pneumatic actuators based robot to perform highly explosive motion like throwing or kicking a ball, the iLQR approach is preferred. The fundamental principle and the basic algorithm is described in the next section.
4.3 iLQR control of the anthropomorphic pneumatic arm

This section presents the optimal control framework used to find the control sequences to perform a desired task. The optimal control problem is the minimization or maximization of a performance criterion with respect to the control under a set of constraints that arise from the physical limitation of the control action and from the plant dynamics.

4.3.1 State space representation

Let us represent the dynamics stated in Eq.(3.24) and Eq.(3.25) in state space form considering the state vector as $x = [q, \dot{q}, P, \dot{P}]^T$.

$$\dot{x} = f(x, u) = \begin{bmatrix} \dot{q} \\ M^{-1}(-C(q, \dot{q}) - G(q) + T(q, P)) \\ -C_p \dot{P} - G_p P + G_p u, \end{bmatrix}$$ (4.10)

where, $f$ is the non-linear function given by Eq.(4.10) in state $x$ and control $u$ that gathers Eq.(3.24) and Eq.(3.25). In the present work, we consider the constraints on the state in the optimal control formulation. There exists a mechanical limit to each degree of freedom of the arm. For the operation to be safe, we have introduced these limits as constraints on the state space inside the cost function of the optimal control formulation. The chosen cost function for the state space constraints is expressed by the following equation :

$$C_s = e^{\lambda_{max}} + e^{\lambda_{min}}$$ (4.11)

where,

$$\max = 1 - \lambda(x_{max} - x),$$
$$\min = 1 - \lambda(x - x_{min}),$$

$x_{min}, x_{max}$ are lower and upper limits on the state and $\lambda$ is a constant. The above consideration for the cost function will ensure that the cost near the limits will be very high and hence the optimal solution will keep the system within the operating limits.

Also, the control action has to be admissible, i.e $u \in U = [P_{min}, P_{max}]$. The control problem formulation is then expressed as determining an open-loop control input $u = u(t, x) \in U$ which can minimize or maximize a cost function along a given time interval $t \in [0, T]$ and with initial state $x(0) = x_0$. For a non-linear dynamics and non-quadratic cost, optimal control solution can be obtained using full DDP. However, as DDP is computationally expensive, an iterative LQR (iLQR) approach is considered [Li 2007]. The iLQR method relies on linearizing the dynamics and
approximating the cost function to quadratic form along the $x$ trajectory. This control approach is briefly summarized in the next section.

### 4.3.2 Iterative Linear Quadratic Regulator (iLQR)

The iterative Linear Quadratic Regulator method (iLQR) is an extension of LQR control. Here, the basic idea is to optimize a whole control sequence starting from any initial state unlike the LQR approach where the optimal control signal is found for the current point in time without any consideration of the future steps. There are basically four steps in this algorithm: Initialization, forward pass, backward pass and control updating. These steps are described in detail after formally defining a generic discrete time dynamical model.

$$x_{t+1} = f(x_t, u_t), \quad (4.12)$$

where $x_t \in X = (x_0, x_1, x_2, ..., x_N)$ and $u_t \in U = (u_0, u_1, u_2, ..., u_{N-1})$. The trajectory $X$ is obtained by the application of $U$ on the system with initial state $x_0$. In order to consider the future consequences, the total cost function ($J$) is defined by taking into account the sum of the immediate cost ($l$) from each state in the trajectory plus the final cost ($l_f$),

$$J(x_0, U) = \sum_{t=0}^{N-1} l(x_t, u_t) + l_f(x_N) \quad (4.13)$$
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The cost-to-go function is the sum of the costs from time $t$ to $N$ and is defined as:

$$J_t(x,U_t) = \sum_{i=t}^{N-1} l(x_i, u_i) + l_f(x_N)$$  \hspace{1cm} (4.14)

The value function $V$ at time $t$ is the optimal cost-to-go from a given state:

$$V_t(X) = \min_{U_t} J_t(x,U_t)$$  \hspace{1cm} (4.15)

From the above equation, it can be said that the optimal cost-to-go is found by using the control sequence $U_t$ that minimizes $J_t$.

The value function $V$ at the final step is actually the final cost.

$$V(x_N) = l_f(x_N)$$  \hspace{1cm} (4.16)

At any previous steps, the value function can be split and expressed as a function of the current cost and the value function at the next time step:

$$V(X) = \min_u [l(x,u) + V(f(x,u))]$$  \hspace{1cm} (4.17)

Having established the definition of various terms used in the algorithm, we can now elaborate the four steps of it.

**Forward pass**  Forward pass means simulating the system from an initial state $x_0$ by applying the control sequence $U$ to obtain the trajectory $(X)$ through state space. From the trajectory $(X,U)$, the overall cost of the trajectory can be evaluated. Also in this pass, partial derivatives of the system and the cost function are calculated in order to linearize the dynamics and quadratize the cost function. At each point $(x_t, u_t)$ on the trajectory $(X,U)$, the partial derivation of the function $f(x_t, u_t)$ is performed with respect to $x_t$ and $u_t$. Similarly, the first and second partial derivatives of the value functions $l(x_t, u_t)$ and $l_f(x_t, u_t)$ are obtained with respect to $x_t$ and $u_t$. All of these partial derivative terms are obtained to facilitate the next step of backward pass.

**Backward pass**  Backward pass computes a local solution to the value function Eq. (4.15) using a quadratic Taylor expansion. Let’s assume that $(\delta x, \delta u)$ is the perturbation given to the system at $(x, u)$ which results into $Q(\delta x, \delta u)$ as a change in the value function. Thus $Q(\delta x, \delta u)$ can be expressed as in (4.18).

$$Q(\delta x, \delta u) = l(x + \delta x, u + \delta u) + V(f(x + \delta x, u + \delta u))$$  \hspace{1cm} (4.18)
So the second order taylor expansion of $Q$ written as:

$$Q_x = l_x + f^T_x V'_x,$$

$$Q_u = l_u + f^T_u V'_x,$$

$$Q_{xx} = l_{xx} + f^T_x V'_{xx}f_x + V'_xf_{xx},$$

$$Q_{ux} = l_{ux} + f^T_u V'_{xx}f_x + V'_xf_{ux},$$

$$Q_{uu} = l_{uu} + f^T_u V'_{xx}f_u + V'_uf_{uu}. \quad (4.19)$$

$V'$ is the value function at the next time step. With the given taylor expansion of $Q$, the optimal control modification $\delta u^*$ for the state perturbation $\delta x$ is obtained by minimizing the quadratic model:

$$\delta u^*(\delta x) = \min_{\delta u} Q(\delta x, \delta u) = k + K\delta x. \quad (4.20)$$

This results into a local linear feedback policy with two terms. The first term $k$ is the feed-forward term and the second term $K\delta x$ is the state feedback whose gains are expressed in (4.21).

$$k = -Q^{-1}_{uu}Q_u \text{ and } K = -Q^{-1}_{uu}Q_{ux} \quad (4.21)$$

Substituting this policy back into Eq. (4.19) with some mathematical manipulation will give the quadratic model of $V$, which can be expressed in Eq. (4.22) as follows:

$$V_x = Q_x - K^T Q_{uu}k,$$

$$V_{xx} = Q_{xx} - K^T Q_{uu}K. \quad (4.22)$$

The backward pass proceeds with the initialization of the Value function with the terminal cost and its derivatives $V(x_N) = I_f(x_N)$ and then Eq. (4.20) and Eq. (4.22) are recursively computed.

**Updating the control signal** After the backward pass, $k$ and $K$ can be obtained which will give the optimal control value. Whether this update will be accepted, rejected or modified depends on the evaluation of the resulting new trajectory denoted by $(\hat{X}, \hat{U})$. So a forward pass is done and the cost is recorded.

$$\hat{x} = x_0$$

$$\hat{u}_t = u_t + \alpha k_t + K_t(\hat{x}_t - x_t)$$

$$x_{t+1} = f(\hat{x}_t, \hat{u}_t). \quad (4.23)$$

where $\alpha$ is a backtracking search parameter. It is set to 1 initially and then iteratively reduced. If the cost of the new trajectory $(\hat{X}, \hat{U})$ is less than that of the previous trajectory $(X, U)$ then the control is updated to $U = \hat{U}$. The backward-forward process is repeated until the new cost is below a certain threshold and then it will be assumed that the final trajectory converges to the locally optimal trajectory. Also
in order to ensure a good descent direction in all cases even while inverting \( Q_{uu} \), a regularization term is usually embedded. This regularization and backtracking terms are determined by the Levenberg-Marquardt heuristic. The summary of this algorithm is presented in Algorithm 1.

**Algorithm 1 ILQR \((u_t, x_i, x_N, Q_N, Q, R, dt, n_{Iter})\)**

```plaintext
cost_{curr} ← ILQRCost \((u_t, x_i, x_N, Q_N, Q, R, dt)\)
for \(j = 1, \ldots, n_{Iter}\) do
    \(\delta u \leftarrow ILQRIterate \((u_t, x_i, x_N, Q_N, Q, R, dt)\)\)
    \(u_t' \leftarrow u_t + \alpha \delta u_t\)
    \(cost_{new} \leftarrow ILQRCost \((u_t', x_i, x_N, Q_N, Q, R, dt)\)\)
    if \(cost_{new} - cost_{curr} < cost_{threshold}\) then
        TerminateIteration
    end if
end for
\(cost_{curr} \leftarrow cost_{new}\)
\(u_t \leftarrow u_t'\)
return \((u_t^{opt}, cost^{opt})\)
```

### 4.4 Conclusion

In this chapter, our goal was to introduce the relevant control strategies that are considered in our work. We have presented a very brief review of several methods to control pneumatic systems and the difficulty faced by all of those methods due to the highly nonlinear nature of the system. It was then interesting to see the possibility of a generic control method independent of the model, so that it can be used for a wide range of the McKibben muscles. The proposed method using a single Integral action is appealing theoretically and can even be verified experimentally on a single McKibben muscle but the response is comparatively slower when it is compared with a full three gains PID controller. We then come up with a PI controller with a feed-forward term which encapsulates the model of the muscles and the robotic arm. This approach, so far, gives the better result but it comes at the cost of overshooting and stiff movement. Finally, the iLQR approach is presented which is known to deal with the non-linear model by linearizing the dynamics and cost function along the trajectory. In Chapter 5, various simulation and experimentation results using these control strategies will be presented.
Simulation and Experiments

The experimental set up considered here is the manipulator of LAAS CNRS which is an anthropomorphic arm of seven degrees of freedom (DoF), where each joint is pneumatically actuated by a pair of Mckibben muscles. In the experiment presented in this paper, only two joints are controlled. These joints are the flexion $\theta_1$ at the shoulder and the flexion $\theta_2$ at the elbow (see Fig. 5.1). So, for the experiments, the robot can be viewed as a 2 DoF manipulator with state defined by

$$x = [\theta_1, \dot{\theta}_1, \theta_2, \dot{\theta}_2]^T.$$  

Each muscle is pressurized by an I/P converter which converts a current command to a reference pressure value. The chapter is dedicated to report various results obtained by performing several experiments on the real robot and simulations using the robot model. These experiments are carried out to understand the robot behavior, evaluating the accuracy and the significance of the proposed model and evaluating different control strategies used to control the system.

5.1 Open loop simulation of the robot

The first experiment is done by supplying a constant pressure as a step input. It is tested on the robot with only one link (the elbow joint). The typical response of the joint is shown in Fig. 5.2.
Figure 5.1 – Picture of the robot-arm showing the two pairs of muscles, in shoulder and elbow flexion.

Figure 5.2 – A typical step response of a joint when both agonist-antagonist muscles actuating this joint are fed with $\Delta P = 1.5\text{bar}$ pressure as a step input.

The pressure dynamics as mentioned in the modelling chapter. The model used here for a single link can be expresses as:

$$\tau_{ext} - f_v\dot{\theta} - G(\theta) = I_M\ddot{\theta} \quad (5.1)$$
5.2. Close loop control with PI controller

In this section, some important results are reported to show the effectiveness of a feed-forward PI controller. The experiments are done on the elbow joint of the robot. The joint is subjected to track two different trajectories: Trapezoidal trajectory and sine wave trajectory.

5.2.1 Trapezoidal trajectory tracking

A reference trajectory in the form of a trapezoid (in a position-time plot) is given to the joint. Based on the model of the actuator, feed-forward term generates a desired $\Delta P$ pressure trajectory corresponding to the reference position trajectory. The PI controller then uses the position feedback to compensate the model error. We have got a very good results with this approach as shown in Fig. 5.4.

The parameters used in the experiments are either estimated or measured. For the elbow joint, $f_v$ is found to be 0.8. The estimation of the inertia of the link and viscous parameters are obtained through CAD model and least square estimation.
5.2.2 Sine wave trajectory tracking

A sine wave trajectory is given as a reference to be followed by the elbow joint. Since this joint cannot move backward i.e. the angular position $\theta$ cannot be negative, the proposed sine trajectory is $30 + 20 \sin(2\pi ft)$ with amplitude of 20 deg and 0.1 Hz frequency.

It is evident from Fig. 5.5 that the tracking result is quite promising at this frequency. However, it is observed that the tracking performance deteriorates with high frequency. It is probably due to the effect of hysteresis which is not considered in the model. So, as long as the frequency is low and the trajectory is slowly varying (less velocity), the effect of hysteresis would be less and the model would be more accurate. The hysteresis effect will be dealt in detail in the future work. But for now, we are able to track a slowly varying trajectory (up to 0.5 Hz) very well using feedforward PI controller. Having a simple model of the pneumatic arm which provides us the capability of predicting the future steps, a local optimal control framework (iLQR) is investigated. iLQR control is then used to perform several tasks which are usually embedded in the cost function of the optimal problem. The method is described in detail in Chapter 4. In the next section, various experiments to perform different tasks and their results are presented.
5.3. Application of iLQR in performing explosive motion

The objective of the experiments is to evaluate the performance of the iLQR control to achieve the following tasks with our multi-link pneumatic robot.

1) Final position control: We aim to compare the quality of the positioning control in the presence of different loads with the iLQR approach and with the feed-forward proportional control. 2) Capability to execute explosive movements by maximizing the link speed at a given time. For this second task we compare simulation results with the results of experiment executed with the real robot. For each task, we analyze the stiffness modulation and we show that the optimal control approach enhances the explosive motion capabilities by simultaneous modulation of position and stiffness. In order to do that, two cases of simulations and experiments are considered:

1) Case-I: When the sum of the pressure in the agonist-antagonist pair of muscles at each joint is kept constant, i.e. $P_1 + P_2 = Constant$.

2) Case-II: When $P_1$ and $P_2$ are left independent. In this case, there will be two inputs for each joint.

Figure 5.5 – Close loop response of the elbow joint (Green) while tracking a reference trajectory (Red).

5.3 Application of iLQR in performing explosive motion
It is important to mention here that the experiments on the real robot are done in open loop. It is possible that the iLQR framework could be used to generate a reference trajectory in position and control and then a feed-forward PI controller could be used to close the loop. However, in order to understand and validate our proposed model, we have preferred to continue the experiments by directly feeding the control generated by the iLQR controller.

5.3.1 Task 1 : Position control

The manipulator is given a final position with a load mass of \( m_l = 0.1 \text{kg} \) at the end effector. iLQR is used here to find the optimal path to reach the final goal \((\theta_1, \theta_2) = (28.8, 57.6)\) degrees. The same task is repeated with different load masses of \( m_l = 0.1 \text{kg} \) and \( m_l = 1.0 \text{kg} \) which is shown in Fig. 5.6.

The following cost function is considered for this task.

\[
C_f = Q_f (x_{ref}(T) - x(t))^2; \\
C_r = Q \int_0^T ((x_{ref}(T) - x(t))^2 + u^2(t)) dt,
\]

where, \( x_{ref} \) is the final position for the two joints. The iLQR control uses Eq. 3.10 and Eq.(5.2) to solve for the optimal control sequence \( u^* \). This optimal control sequence in forward application to Eq. 3.10 will yield the needed trajectory. To compare the effectiveness of the iLQR approach, the task is executed using a Proportional-Integral controller with a feed-forward term. The feed-forward term gives a desired pressure for each muscle at the joint needed to maintain a desired joint angle. Thus, the control action of the feed-forward PI controller can be defined as follows:

\[
u(t) = P_{feed} + K_p(e(t)) + K_i \int_0^t (e(t)) dt
\]

where, \( e(t) = x_{ref} - x(t) \), and \( K_p \) and \( K_i \) are proportional and integral gains respectively. The simulation results are shown in Fig. 5.7. The response of the feed-forward PI controller is shown in black dashed line is compared with the responses of optimal position control in Case-I when \( P_1 + P_2 = \text{Constant} \) (blue lines) and in Case-II when \( P_1 \) and \( P_2 \) are independent (magenta lines)(See Fig. 5.7).

From the position plots in Fig. 5.7, it appears that the iLQR approach gives a good compromise between keeping the stiffness low and minimizing the oscillations which results into a smooth motion. However, the feed-forward PI controller makes joint 1 very stiff and joint 2 very flexible leading to an overshoot and oscillations.

As discussed in section Chapter 3, the stiffness can be adjusted for the same equilibrium position by changing the sum of pressures in the agonist-antagonist pair of muscles. As the sum increases, stiffness at the equilibrium increases which can be observed at each joint (blue and brown lines in stiffness plots).

In order to find the most compliant position trajectory, i.e to find the best sum of pressure in the agonist-antagonist pair, \( P_1, P_2 \) are left independent and Eq.(3.20) has two independent inputs for each joint. In this case, the optimal solution gives
5.3. Application of iLQR in performing explosive motion

Figure 5.6 – Figures on the left side represent the position response and stiffness variation at joint 1 and figures on the right side represent the same for joint 2 in order to reach the target \((\theta_1, \theta_2) = (28.8^\circ, 57.6^\circ)\). The plots compare the response of the joints and the stiffness profile when the end effector is loaded with mass 0.1kg (solid line) and 1.0kg (dashed line). For the heavier load, optimal control gives a stiffer stiffness profile.

Figure 5.7 – Figures on the left side represent the position response and stiffness variation at joint 1 and figures on the right side represent the same for joint 2.
the similar optimal position trajectory but with better stiffness profile (magenta line in stiffness plot in Fig. 5.7). Here, the better stiffness profile is not too stiff to lose the inherent compliance nature of the Mckibben muscle actuated joint and not too highly compliant in order to avoid oscillation and poor position control.

5.3.2 Task 2 : Maximizing the link speed

The objective is to execute some explosive motions with the aim to perform, in the future, tasks such as ball throwing, kicking or hammering a nail. Such motions would require either maximizing the joint/link speed or end-effector speed [Garabini 2011], [D.Braun 2013]. Here, two sub-tasks are presented:

1) Maximizing the angular speed of the elbow joint. The task is first simulated and then executed by the real robot. A comparison between simulation and the experimental results are shown in Fig. 5.8.

2) Maximizing the end effector speed: The objective of this task is to achieve maximum end-effector speed at terminal time $T$. Simulations are done for both Case-I ($P_1 + P_2 = Constant$) and Case-II ($P_1$ and $P_2$ are independent).

5.3.2.1 Maximizing the angular speed

For maximizing the elbow joint’s angular speed at final time $T = 1$, the task requires only the terminal cost, $C_f$. But to minimize the control effort, a running cost $C_r$ involving only control pressures is used.

$$C_f = -Q_f (x_4(T))^2,$$

$$C_r = Q_u \int_0^T u^2(t) dt,$$

(5.4)

where, $x_4 = \dot{\theta}_2$ is the angular velocity of the elbow joint which constitutes the fourth state variable. $Q_f$ and $Q_u$ are weights for the terminal cost and the running cost respectively. The simulation results are shown in Fig. 5.8

In simulation, the maximum joint velocity which is around -15 rad/sec, is reached at terminal time (See Fig. 5.8). The robot response and the simulation response in position and speed show a good match. However, some discrepancies can be observed. Apart from some modeling error, this difference is probably due to the fact that the constraints on the state vector are not considered in the optimal control problem formulation. This is an improvement that we implemented in the subsequent experiments. Snapshots of the video of the experiment are presented in Fig. 5.9

5.3.3 Task 3 : Maximizing the end effector speed

The objective is to maximize the end-effector speed of the manipulator at terminal time. The cost function, thus, comprises the terminal cost $C_f$ involving the
end-effector velocity and the running cost $C_r$ involving only control efforts.

\[
C_f = -Q_f(f_{vel}(x(T))^2, \\
C_r = Q_u \int_0^T u^2(t) dt, \tag{5.5}
\]

where, $f_{vel}(x(t))$ is the function which computes end effector velocity from the robot kinematics. Simulations are done for the following two cases. In Case-I, the sum of pressures in the agonist-antagonistic pair is kept constant. This value is equal to 3 bars at joint 1 and to 4 bars at joint 2 (Fig. 5.10).

In this second simulation (Case-II), we let $P_1, P_2$ independent (Fig. 5.11).

Comparing the velocity plots and the corresponding stiffness plots in Fig. 5.12, it can be seen that the maximum end-effector velocity has increased from 3.8m/s in Case-I to 4.1m/s in Case-II. This is due to the fact that in Case-II, the optimal control has the freedom to modulate the compliance with two inputs at each joint and hence it was able to achieve higher speed.

5.3.4 Task 4 : Ball throwing and kicking

The objective is to throw a ball to a maximum distance. The distance to be reached is related to the kinematics of the arm and hence is a function of the state of the arm. The cost function, thus, comprises the terminal cost $C_f$ involving the distance and the running cost $C_r$ involving only control efforts. Also the final time
Figure 5.9 – The pneumatic manipulator arm executing the task of maximizing the angular speed of the elbow.

Figure 5.10 – Case-I: $P_1 + P_2 = \text{Const}$. Plots on the top show the simulated position response of joint 1 (blue line) and Joint 2 (black line). Control effort is shown in the bottom plots. The control inputs, Input 1 and Input 2 are applied on joint 1 and joint 2 respectively.

of the motion is fixed at $T = 4$ seconds.

\[ C_f = d = kf(x) \]

\[ C_r = Q_u \int_0^T u^2(t)dt, \tag{5.6} \]
5.3. Application of iLQR in performing explosive motion

Figure 5.11 – Case-II: $P_1, P_2$ are independent. Plots on the top show the simulated position response of joint 1 (blue line) and joint 2 (black line). Control effort is shown in the bottom plots. The control inputs, Input 1 and Input 3 are inputs to the agonist-antagonist pair at joint 1. The control inputs, Input 2 and Input 4 are inputs to the agonist-antagonist pair at joint 2.

where, $k_f(x(t))$ is the function which computes the maximum distance to which the ball will be thrown. This function relates the motion of the ball with the robot kinematics. We used the same cost function in a second experiment for the task of kicking a ball stationed at a point. Snapshots of the video of both the experiments are presented in Fig. 5.13.

Simulations are done for the case where the sum of pressures in the agonist-antagonistic pair is kept equal to 4 bars at the joint 1 and to 4 bars at the joint 2. We present the simulation results when there are no constraints on the state of the robot (Fig. 5.14). However, the robot has limits at its joints which is typically between $[-28.5^\circ, 114.6^\circ]$ in degrees. It is evident from Fig. 5.14 that it is necessary to include the constraints in order to make the real robot execute the task.

Plots in Fig. 5.15 compare the response of the real robot with the simulated response of the model when optimal control inputs are applied in the open-loop. It is interesting to note that the optimal solution given by the iLQR control is somewhat intuitive to the human behaviour. It takes few swings to attain the maximum speed of the end effector before launching the ball. The maximum distance achieved by the ball was 2.3m against 3m predicted by the simulation. The observed discrepancies between simulated and real robot response can be justified by the fact that the system is controlled in open-loop without feedback. Also we have no model of the various effects of hysteresis and dry friction. Moreover, the model of the gripper is not available, so the exact time of opening of the gripper is not known. It has
Figure 5.12 – Comparison of the stiffness profile of each joint (joint 1: blue lines, joint 2: red lines) in Case-I when $P_1 + P_2 = \text{Const}$ (dashed lines) and Case-II when $P_1, P_2$ are independent (solid lines). It is evident from the plots that the motion in Case-II is indeed slightly more compliant than the motion in Case-I.

been roughly estimated by observation for the ball throwing experiment. Since modeling all the aspects of pneumatic muscles actuators seem to be difficult, it will be interesting in the future to rely on close loop control.

5.4 Conclusion

The various simulations and experiments are carried out in open loop and then in closed loop. From the open loop simulation and its comparison with the real experiment, it can be said that the model is good enough to capture the static and the dynamic behavior of the actuator. Based on this model, an inverse mapping leads to a feed-forward term. A PI controller with this feed-forward term is very effective in tracking trajectories like line, trapezoid or sine wave. Though, the tracking performance could be enhanced with a better understanding of the physical phenomenon occurring inside the Mckibben muscles and the pressure generating valves. Specially, hysteresis modeling is crucial to track trajectories with high velocities. The simplified model, however, makes the iLQR approach feasible for application on the robot. In view of the experiments with the real robot and the comparison with the simulation results, it can be claimed that the model is reliable enough to predict the future steps to be used in the iLQR kind of controllers. This results into smoother tracking and enable the anthropomorphic arm to execute high per-
5.4. Conclusion

Figure 5.13 – Two experiments have been performed. Left picture is the set-up for the task of kicking the ball while the picture in right is the set-up for throwing the ball.

formance motion which would be very difficult otherwise (with PI controller). Also, experiments are done with both SISO system ($\Delta P$ input) and MIMO system (independent $P_1$, $P_2$). Simulations have shown that the iLQR approach has utilized the two inputs to generate a better optimized trajectory with respect to energy and hence is capable to improve the performance of the explosive motion by increasing the throwing speed.

It can be concluded from this chapter that our proposed model is valid enough and can be used in the control of the anthropomorphic arm actuated by the Mckibben muscles. The robot can thus be controlled either by feed-forward control or by means of a more sophisticated receding horizon model predictive controller can also be used.
Figure 5.14 – Plots on the top show the simulated position response of joint 1 (blue line) and Joint 2 (red line) under no constraints and the plot below presents the same after applying the state constraints. Brown lines are the limits on the state.

Figure 5.15 – Plots on the top show the simulated position response of joint 1 (blue line) and Joint 2 (red line). Control effort is shown in the bottom plots. The control inputs, Input 1 and Input 2 are applied on joint 1 and joint 2 respectively.
Our interest in the scope of this thesis was to explore the potential of alternative actuators than the traditional electric motors. This is in particularly inspired from the human musculoskeletal design. It is well known that human utilize the inherent elasticity in the muscle-tendon linking to store energy for later use or optimize the energy to perform tasks efficiently. Also this energy storing capability makes such system shock absorber. From robotics perspective, all of these properties are very interesting. On one hand, energy storage capability will make the robot safe for both the human, the environment and the robot itself while on the other hand it empowers the robot with the capability to perform extreme movements which would be impossible for a rigid robot to do. In the literature various electro-mechanical designs are proposed to acquire such a behaviour. Several different designs have been presented in the state of the art of this thesis. Usually this is achieved by placing an elastic component between the links and the motors. Moreover, in order to even actively control the level of stiffness, additional motors are deployed. These class of actuators (VSAs and AWAS, AMSC etc.), though capable of controlling position and compliance simultaneously, are usually very bulky and complex to be integrated in a full size robot. Its a challenging task to find a best compromise in terms of having variable compliance actuator with simpler and lighter design. The scope of our study also covered a futuristic electroactive polymers based actuator which bends on the application of voltage and thus generates motion. These are very light and may be best suited for micro or nano robots. Finally, the Mckibben muscle based pneumatic actuator is considered in the study due to its similarity with the human muscles and having a very good power to weight ratio. The Mckibben muscles actuate each joint of our anthropomorphic arm in agonist-antagonist set-up. However, modelling such system is not trivial. In fact, this is the problem which has been addressed in depth in our work. A mathematical model was proposed to encompass all the different components of a pneumatic actuator based robots. Simulations and experiments were used to validate the proposed model. The main points that can be concluded from this modeling as the following ones:

- It is possible to model such a non-linear system with quite simple model.

- Pressure generation inside the muscle is approximated by second order differential equation. However, the non-linearity in this model which arises as the natural frequency of the second order differential function is dependent on the instantaneous volume of the muscle, which in turn depends on the instantaneous joint angle.

- The model does not include hysteresis effects due to dry friction in the present study but still, it covers most of the static and the dynamic behavior.

Some of the parameters in the model (usually coefficients in the torque function) are identified using gray box modeling with the knowledge of the dynamics of the system. A combined model of the entire anthropomorphic manipulator is presented as an analogy to the robotic manipulators with conventional electrical motors. The
motor side dynamics are replaced by pressure side dynamics while keeping the structure of the standard manipulator equation (Refer to Eq. 3.24).

A generic model free single-I controller is tested in simulation. Though the results were promising, it is not relevant for practical purposes because of the over simplification of the McKibben system. Moreover, it results into very slower response in comparison to a full three gains PID controller. A PI controller with a feed-forward term which encapsulates the model of the muscles and the robotic arm is used. Although, it has shown overshoot and stiff response, it can be considered as the better option for tracking a reference trajectory (specially when the trajectory is slowly varying). The iLQR controller is used to enable the robot to perform various tasks while utilizing the inherent compliance and energy storing capabilities.

One of the objective of our work was to empower the robot with the capability of performing high performance motion. In order to do so, various simulation and experiments are carried out in open loop and then in closed loop. Following points can be clearly deduced from these experiments:

- Comparison of the simulation of the model and the real robot response confirm that the model is good enough to capture the static and the dynamic behaviour of the actuator.
- A PI controller with this feed-forward term is very effective in tracking trajectories like line, trapezoid or sine wave.
- The iLQR controller application on the robot is made possible by the simplified model. It results into smoother tracking and enable the anthropomorphic arm to execute high performance motions like kicking or throwing a ball. The solution given by iLQR in ball kicking or throwing experiments is very interesting because the kind of trajectory given by the iLQR is quite intuitive to human. A human would most probably chose the similar trajectory for his arm to throw a ball to a maximum distance if he is constrained to optimize the energy as in the case of our robot.

Encouraged by these successful experiments, we are planning to continue our experiments to perform more difficult task like hammering a nail. Also it will be of our interest to consider an improvement of the model by including an hysteresis effect. All of the experiments have been done in open loop. The iLQR generates an optimal control sequence that is fed directly to the robot. In the near future, an MPC scheme would be engaged to use the real time feedback from the robot.

The thesis also present our proposed non-linear model for the dynamic behaviour of the ionic polymer bending actuator. The model is based on the identification of the actuator under the form of a kind of non-linear first-order system with parameters varying with the control voltage. A PI controller was found to be efficient and stable to control the system. The tuning for the two gains of the PI controller was also proposed based on the specification of a safe control voltage range and on the possibility given to the control to reach such safe working limits. Reported results show the relevance of this approach for getting a same couple of gains in the full position range leading to a maximum overshoot of 5% and a response time taking advantage of the imposed safe voltage limits. The limitation of our PI-control
are reached when sharp trajectory curvature changes occur. Future work will focus on improvements in trajectory tracking, especially, with studying the relevance of variable $P$ and $I$-gains to tackle both with sharp curvature changes and voltage saturation constraints.

I would like to write my thesis in English. The work done in my research could be interesting for various other institutions working on similar topics. In order to reach wider and international audience, this thesis is considered to be written in English. Also, We are inviting jury from different country (Belgium). In addition to that, my french level is not fluent yet and I may not be able to express all my arguments very well in French.
Characterization of PEDOT :PSS Ionic actuator actuators

One can refer the thesis of Simate [Simaite 2015a] in which fabrication and characterization of PEDOT :PSS Ionic actuator is reported in very much detail. Here is presented the different sensors and the experimental set-up used in characterization of the actuator.

The thickness of dry and soaked actuators was measured by digimatic indicator (Mitutoyo Absolute) and also estimated from the SEM pictures. SEM images of membranes and actuators were obtained using a Hitachi S−4800 field emission scanning electron microscope (acceleration voltage 800 V, working distance of about 5 mm).

Resistance and conductivity of PEDOT :PSS was measured between two extremities of each electrode and between two electrodes, by applying 0.1−0.5 V voltage (with 0.01 V increment) and measuring current, using Suss PA200 probe station and Agilent 4142B tester. Conductivity was then calculated assuming dimensions of 2 mm x 1.5 cm and the thickness measured by SEM not taking into account the PEDOT :PSS in the membrane.

For all bending characterization measurements, actuators were placed between two copper electrodes clamped at 1−2 mm from one end of the actuator. For bending measurements actuators were placed under Leica MZ-12 microscope (Leica Microsystems) with Digital Sight camera system (Nikon) as shown in Fig. A.1. The square voltage wave with various amplitudes and frequencies was generated with Keithley 2450 sourcemeter. Bending was recorded at 100 frames per second, 640x480 resolution. After recording it was converted from raw to 5 frames per second ‘mpeg4’ encoded video in order to reduce its size. Videos there processed using Matlab Image processing toolbox to track the displacement of actuators tip. The strain was then calculated from tip displacement using formulas proposed by Sugino et al [Sugino 2009] :

\[
\varepsilon = \frac{2hd}{L^2 + d^2} \times 100\%
\]  

(A.1)

where \( \varepsilon \) is strain in %, \( h \), \( L \) and \( d \) are thickness, free length and displacement of the actuator respectively. Thickness of dry actuator, estimated by SEM, was used for calculations.
Cyclic voltammetry (CV) measurements were performed using Autolab potentiostat PGSTAT30 (Metrohm Autolab) coupled with NOVA 1.8 Software at room temperature \((23\pm1)\). Two electrode configuration was adopted (equivalent to the one used for bending characterization), in which two surfaces of PEDOT :PSS were working and reference electrodes. CV measurements were performed at various voltages and scan rates as indicated in the labels of the figures.

Actuator bending for lifetime measurements was recorded by laser displacement sensor (optoNCDT 1302, MicroEpsilon) at the position of about 2 mm from the end of the actuator. All measurements were performed in the room temperature and humidity that were slightly varying. Actuation voltage was generated by Keithley 6221 waveform generator.

For bending characterization, laser displacement sensor (optoNCDT 1700, MicroEpsilon) was used connected to Ni-DAQmx card as shown in Fig. A.2. Ni-DAQmx was also used for signal generation and current measurements. Displacement measured by laser was used as a feed-back in order to switch actuators position to 1 mm above or below the initial by changing polarity of applied voltage \((\pm1.5 \, V)\). The time needed to reach the set position was calculated for each cycle.
Figure A.2 –

Figure A.3 – Tracking bending using laser displacement meter.
Annexe B

Geometrical parameter of the robot

B.1 Kinematics of the robot

For this thesis, we have actuated only two joints (the elbow and the shoulder). So for all the kinematic equations, we have used the 2 Dof model and did all the calculation manually similar to the work presented in [D.Braun 2013].

B.2 Cad model of the robot

The total mass of the mobile part of the arm is \( m_1 + m_2 + m_3 + m_4 = 5.138 \text{kg} \). This does not include mass of the shoulder joint and mass of the muscles, chains, wires and air tubes.

<table>
<thead>
<tr>
<th>Joints</th>
<th>( l_o (\text{cm}) )</th>
<th>( \alpha_o (\text{degrees}) )</th>
<th>( k )</th>
<th>( r_o (\text{cm}) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Shoulder Joint</td>
<td>23</td>
<td>20</td>
<td>1.1</td>
<td>1.2</td>
</tr>
<tr>
<td>Elbow Joint</td>
<td>18.5</td>
<td>20</td>
<td>1.2</td>
<td>0.85</td>
</tr>
</tbody>
</table>
Annexe B. Geometrical parameter of the robot

Figure B.2 – Kinematic diagram and calculation for parameters in dynamical equation of the manipulator.

\[
\mathbf{M} = \begin{bmatrix}
I_1 + m_1 l_1^2 + l_2 + m_2 (l_2^2 + 2l_1 l_2 \cos(q_2) + l_3^2) + m_3 (l_1^2 + 2l_1 l_2 \cos(q_2) + l_3^2) \\
I_2 + m_2 (l_2^2 + l_1 l_2 \cos(q_2)) + m_3 (l_3^2 + l_1 l_2 \cos(q_2)) \\
I_2 + m_2 l_1^2 + m_3 l_3^2
\end{bmatrix}
\times
\begin{bmatrix}
l_2 \\
l_3
\end{bmatrix},
\quad \mathbf{C} = \begin{bmatrix}
-(m_2 l_1 l_2 l_1 \sin(q_2)(2\dot{q}_1 \dot{q}_2 + \dot{q}_2^2)) \\
(m_2 l_1 + m_3 l_2) l_1 \sin(q_2) \dot{q}_2^2
\end{bmatrix},
\quad \mathbf{D} = \begin{bmatrix}
b_1 \dot{q}_1 \\
b_2 \dot{q}_2
\end{bmatrix},
\quad \mathbf{G} = \begin{bmatrix}
g(m_1 l_1 + m_2 l_1 + m_3 l_1) \cos(q_1) + g(m_2 l_2 + m_3 l_2) \cos(q_1 + q_2) \\
g(m_2 l_2 + m_3 l_2) \cos(q_1 + q_2)
\end{bmatrix}.
\]

Table B.2 – Joint parameters

<table>
<thead>
<tr>
<th>Joints</th>
<th>R(m)</th>
<th>m(kg)</th>
<th>l(cm)</th>
<th>l_c(cm)</th>
<th>I(kgm^2)</th>
<th>f_v</th>
</tr>
</thead>
<tbody>
<tr>
<td>Shoulder Joint</td>
<td>0.009</td>
<td>2.7</td>
<td>351</td>
<td>125</td>
<td>0.02</td>
<td>3.0</td>
</tr>
<tr>
<td>Elbow Joint</td>
<td>0.015</td>
<td>2.6</td>
<td>307</td>
<td>178</td>
<td>0.0144</td>
<td>0.8</td>
</tr>
</tbody>
</table>

Inertial property of the arm in G-frame (center of gravity frame with 1, 2 and 3 as principal axes as shown in the Fig. B.4):

\[
\mathbf{I}_G = \begin{bmatrix}
4.93593 & 0 & 0 \\
0 & 328.749 & 0 \\
0 & 0 & 330.924
\end{bmatrix} & \overrightarrow{OG} = \begin{bmatrix}
1.58 \\
-0.84 \\
-309
\end{bmatrix} \quad (B.1)
\]

Distances are in mm and so the inertia is in kg – mm^2.
B.2. Cad model of the robot

**Figure B.3** – Different parts of the robot arm

**Figure B.4** – Solid model of the entire integrated robot arm
In order to better understand closed-loop stability, we propose to apply to our nonlinear system a classic linearization around the desired position considered as system’s equilibrium point. We will limit, in a first step, our analysis to the linear viscous friction case. From Eqn. (3) Eq. (4.3) we derive:

\[
\dot{u}_{\text{Fmax}} \left[1 - \frac{x}{x_{\text{max}}} \right] - u_{\text{Fmax}} \left(\frac{\dot{x}}{x_{\text{max}}} \right) - f_v \ddot{x} = (M + m)\ddot{x} \tag{C.1}
\]

Let us define the state variables as follows:

\[
x_1 = \ddot{x}, x_2 = \dot{x}, x_3 = x - x_d
\]

As a consequence, the linearization will be realized around a zero-equilibrium point:

\[
x_{1d} = x_{2d} = x_{3d} = 0
\]

Let us define the following integral term:

\[
\text{Int}(x_3) = \int_0^t (x_d - x) dt = -\int_0^t x_3 dt \tag{C.2}
\]

From Eq. (C.1) Eqn. (10) the following state representation is deduced in which the term in \(x_3\) corresponding to a \(\varepsilon_3\)-term was neglected:

\[
\dot{x}_1 = \left(\frac{1}{m + M}\right)[-f_v x_1 - \frac{k_I \text{Int}(x_3) F_{\text{max}}}{(m + M)x_{\text{max}}} x_2 - k_I F_{\text{max}} (1 - \frac{x_d}{x_{\text{max}}}) x_3]
\]

\[
\dot{x}_2 = x_1
\]

\[
\dot{x}_3 = x_2 \tag{C.3}
\]

In a classic way, we can deduce the matrix relationship \(\dot{\varepsilon} = J\varepsilon\) in which \(\varepsilon = [\varepsilon_1, \varepsilon_2, \varepsilon_3]^T\) and the characteristic polynomial corresponding to \(\text{det}(J - \lambda I_3)\) where \(I_3\) is the 3x3 unit-matrix and \(\lambda\) a complex variable. We get:

\[
\lambda^3 + \frac{f_v}{(m + M)} \lambda^2 + \frac{k_I \text{Int}(x_3) F_{\text{max}}}{(m + M)x_{\text{max}}} \lambda + \frac{k_I F_{\text{max}}}{(m + M)} (1 - \frac{x_d}{x_{\text{max}}}) = 0 \tag{C.4}
\]

Analyzing the system stability from this equation has however a meaning only if all coefficients are constant. This can be made from a simple physical interpretation of \(\text{Int}(x_3)\) : let us assume that the system transitory state takes a finite time to put the system from its initial position to the neighborhood of \(x_d\) with the \(\varepsilon\)-accuracy, and that this time is long enough in order that its change resulting from the \(\varepsilon\)-vector is
negligible. In this case we can write:

\[ \text{Int}(x_3) \approx u_d/k_I, \]  

where \( u_d \) is the unique closed-loop control value corresponding to the equilibrium \( x_d \)-position and given by:

\[ u_d F_{\text{max}} \left(1 - \frac{x_d}{x_{\text{max}}}\right) = Mg \]  

(C.6)

By reporting Eq. (C.5) and Eq. (C.6) into Eq. (C.4) we get:

\[ \lambda^3 + \frac{f_v}{(m + M)} \lambda^2 + \frac{Mg}{(m + M)(x_{\text{max}} - x_d)} \lambda + k_I \frac{F_{\text{max}}}{(m + M)} \left(1 - \frac{x_d}{x_{\text{max}}}\right) = 0 \]  

(C.7)

It is now possible to apply the classic Routh-Hurwitz stability criterion peculiar to a third order system in the form \( \lambda^3 + A\lambda^2 + B\lambda + C = 0 \): the system is stable if and only if \( A > 0, B > 0, C > 0 \) and \( AB > C \). In our case these conditions can be gathered in the following relationship:

\[ k_I < \frac{f_v g x_{\text{max}}}{(1 + m/M) F_{\text{max}} (x_{\text{max}} - x_d)^2} \]  

(C.8)

Two important facts can be deduced from this stability condition: the higher the load \( M \) is, the more stable the system is and the closer the desired position is to \( x_{\text{max}} \), the more stable the system is. If we apply this formula to the numerical values used in previous simulations, a limit \( k_I \)-value of about \( 363 m^{-1}s^{-1} \) is deduced; in fact this parameter induces some intermediate \( x \)-values exceeding the maximum of \( 10 \) cm, leading to saturate the muscle contraction position, which is not taken into account in our model. Moreover, it is also possible to underestimate this stability condition to get one \( k_I \)-parameter bound value which is now independent on load and desired position. On the one hand, we can write \( (x_{\text{max}} - x_d) < x_{\text{max}} \) and, on the other hand, we can consider that \( m < M \) i.e. the mobile muscle mass is low and so \( (1 + m/M) < 2 \); as a consequence, we derive the following expression of \( k_I \)-bound parameter now independent on load and desired position:

\[ k_{I,\text{im}} < \frac{f_v g}{2 F_{\text{max}} x_{\text{max}}} \]  

(C.9)

Its value, in the case of our simulations, is equal to about \( 24.5 m^{-1}s^{-1} \) and is still greater than the chosen value of \( 10 \) associated to a load \( Mg \) equal to \( 10\% \) the maximum force. It is possible to apply such analysis to our non-linear kinetic friction model if we assume that, when the system is removed from its equilibrium position, its restoring velocity can be considered to be constant and equal to the initial slope of the kinetic friction versus speed relationship i.e. in accordance with our previously
introduced notations:

\[
k_l < \frac{f_v g}{2F_{\text{max}}x_{\text{max}}} \frac{dF_{\text{damp}}}{dx}(u_d, \dot{x} = 0) = u_d \frac{(F_k - F_s)}{x_k}
\]  

(C.10)

where \(u_d\) is now the control value corresponding to the following equilibrium positioning equation:

\[
u_d F_{\text{max}} \left(1 - \frac{x_d}{x_{\text{max}}} \right) = Mg + F_s
\]  

(C.11)

By using this new expression of \(u_d\) in Eq. (C.4) and substituting initial slope of Eq. (C.10) for \(f_v\), we get the following stability condition for \(k_l\) parameter:

\[
k_l < \frac{(Mg + F_s)^2 x_{\text{max}}^2 (F_k - F_s)}{(m + M) F_{\text{max}}^2 (x_{\text{max}} - x_d)^3 \dot{x}_k}
\]  

(C.12)

As earlier, increasing load or desired position are stability factors but also a large difference \((F_k - F_s)\) which, according to us, is particularly well realized in the case of the double helix braided sleeve used in McKibben artificial muscle technology.

To derive from Eq. (C.13) a bound-value independent of load and desired position can be made if we assume, as previously, that \((x_{\text{max}} - x_d) < x_{\text{max}}\) and \(m < M\); we get the following bound-expression for \(k_l\):

\[
k_{l,\text{im}} < \left( \frac{mg}{F_{\text{max}}} \frac{F_k - F_s}{F_{\text{max}}} \right) \frac{g}{2x_{\text{max}} x_k}
\]  

(C.13)

which is equal to about to \(9.8m^{-1}s^{-1}\) in the case of numerical values used for our simulation, very close to the empirically chosen \(10m^{-1}s^{-1}\). Although questionable due to its very simplifying assumptions, this stability analysis suggests that a closed-loop stable control by means of a single linear integral action is feasible for the McKibben muscle without adding any supplementary damping device, as experimentally checked in further reported experiments.
D.1 Intensity-Pressure converter

To provide pressure to the muscles, Intensity-Pressure converter are used on our robot. It is a Samson I/P 6111 manufactured by Samson Corporation, Frankfurt, Electropneumatic Converter. The current to pressure conversion done by the IP converter is shown in its datasheet.

This IP is rapid in action producing output pressure in range 0 to 5 bar. The bandwidth of IP is volume dependent and can be as high as 5Hz for volume of 75cm³. There are seven joints and a gripper. Each joint and gripper is actuated by a pair of Mckibben muscles and each muscle is controlled by one IP converter and so there are 16 IP converters.
D.2 NI module

The electronics of the 7 Dofs anthropomorphic arm is upgraded. Previous solutions based on the old and obsolete ISA bus were not adapted to these new evolutions. Finally, CompactRIO from National Instruments was selected. This is a reconfigurable and embeddable chassis, integrating an intelligent real-time controller. According to the customer needs, up to 8 different modules can be plugged into the chassis. Depending of our needs 3 kinds of modules are added:

- 1x NI9205. It is an Analog-to-Digital-Converter (ADC) with up to 32 channels, selectable acquisition range (±200mV, ±1V, ±5V ± 0V) and a max sampling frequency of 250kS/s. This device will sample the potentiometers (7 in numbers) dedicated to the positioning of the arm.

- 3x NI9265. These 3 modules are Digital-to-Analog-Converters (DAC). They have the particularity to provide analog current outputs. The SAMSON’s 6111 electropneumatic converters use this kind of signal. Each module is able to manage up to 4 channels in the 0 to 20mA range at 100kS/s.

- 4x NI9401. Finally the 4 last modules drive bidirectional digital IOs. Theses IOs connected to relatives quadrature encoders will be able to replace more accurately the current analog potentiometers. Up to 12 quadrature encoders can be acquired. The aim of the CompactRIO is to make the link between the computer managing high level control and the actuators of the 7DOF arm. It means that simple functions such as sampling and encapsulation into standard network protocol (UDP), extraction from standard network protocol (UDP) and signal generation will be performed.

D.2.1 From Host computer to NI module

**Initialization of the communication** Before broadcasting data, NI module requests that a host initialize the communication, defining numbers of useful data in all the others messages:

- "ADC channels to be transmitted" : Between 0x00 and 0x20 on an unsigned char. It corresponds to the total of analog-to-digital inputs transmitted by the NI 9205 converter. Up to 32 channels are available.

- "Counters to be transmitted" : Between 0x00 and 0xC on an unsigned char. It corresponds to the number of counters transmitted on the 3 NI9401 digital IO controllers. Up to 12 counters can be acquired.

- "Errors to be transmitted" : Between 0x00 and 0x04 on an unsigned char. It corresponds to the errors broadcasted by the four NI 9265 digital-to-analog currents converters. As the four modules are connected, all of them can send its status.

- "Sampling Period" : Between 0x0001 and 0xFFFF on an unsigned short. It corresponds to the sampling period expressed in milliseconds. Every N sampling period ADC values and NI9401 status errors are sampled and send to the host computer.
Electrical current commands for the electropneumatic converters A 1D array composed of 16 unsigned shorts words (24 bytes or 16 bits long) is sent up to one millisecond.

- "0" corresponds to a 4mA
- "216-1 = 65535" to a 20.6mA on the output of the NI module. According to the datasheet of the SAMSON’s 6111 electropneumatic converter, 4/20mA signal is used, it has to be confirmed. Likewise, pressure to current conversion will have to be evaluated. Endianness will have to be verified too. The frame is composed as shown in Fig. D.3:

Counters Reset A 2 states unsigned byte (0x00 or 0x01) can be sent to reset synchronously the values of the 12 counters recording the encoders. Take care, that an 'enable' command as to be performed after a 'reset' in order to start counting otherwise counters will be maintained in reset state. The frame is shown in Fig. D.4:

Digital output control A digital output is available on the NI9205 module. A 2 states unsigned byte (0x00 or 0x01) can be sent to set or reset the output. The frame is shown in Fig. D.5:
D.2.2 From NI module to Host computer

**Potentiometers values** A 1D array of single float words (4 bytes or 32 bits long) + 1 unsigned long word (4 bytes or 32 bits long) of label (increased every millisecond) is sent every millisecond. The number of elements contained into the 1D array is initialized at start-up (varying from 0 up to 32). The 7 first values correspond to the tension available on the potentiometers, others inputs are free and can be used in future. Conversions have to be done between tensions and positions. Endianness will have to be verified. The frame is shown in Fig. D.6 (in case all 32 ADC channels are requested):

**Counters values** A 1D array of 12 signed integer words (4 bytes or 32 bits long) + 1 unsigned long word (4 bytes or 32 bits long) of label (increased every millisecond) is sent every millisecond. The number of elements contained into the 1D array is initialized at start-up (varying from 0 up to 12). The values correspond to counters associated to incremental encoders. Endianness will have to be verified. The frame is composed as in Fig. D.7 (in case all 12 counters are requested):
Current module error  Each NI9265 Digital-to-Analog-Converter can provide a diagnostic of its state. 4 bytes (because of the 4 stacked modules) + 1 identification byte + 1 unsigned long word (4 bytes or 32 bits long) of label (increased every millisecond) are sent every millisecond. Each of the 4 bytes is a bits field.

- Bit 0 : NI9265 module is working normally or is in fault state.
- Bit 1 : NI9265 is not supplied externally. In order to provide current, an external supply must be connected in the 9 to 36Vdc range.
- Bit 2 - 5 : Each of the 4 channels can diagnostic a 'current open loop'.
- Bit 6 - 7 : ’0’ padding. The frame is shown in Fig. D.8 :

![Data frame for Current module error](image-url)

**Figure D.8 – Data frame for Current module error**
Figure D.9 – The complete experimental set-up
Bibliographie


[Daerden 2001] F. Daerden et D. Lefeber. The concept and design of pleated pneumatic artificial muscles. International Journal of


Key words : Pneumatic systems, Mckibben muscles, iLQR control, non-linear control, agonist-antagonist actuation, bio-inspired robots, anthropomorphic systems, mots, clefs