

Dimensionality reduction and pathway network analysis of transcriptome data: Application to T-cell characterization

Soutenance de Thèse de Christophe Bécavin
6 Décembre 2010

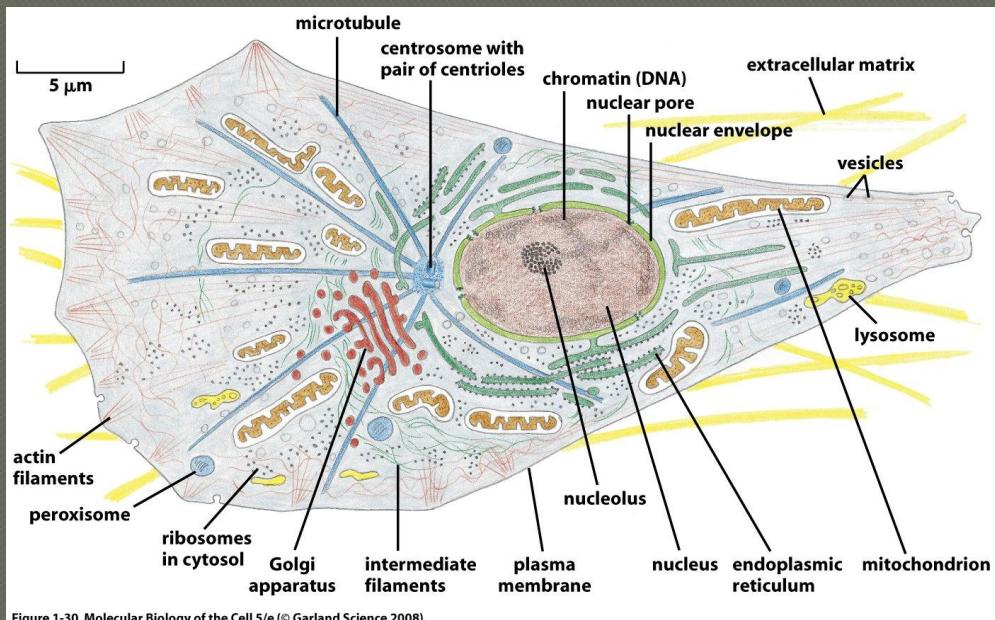
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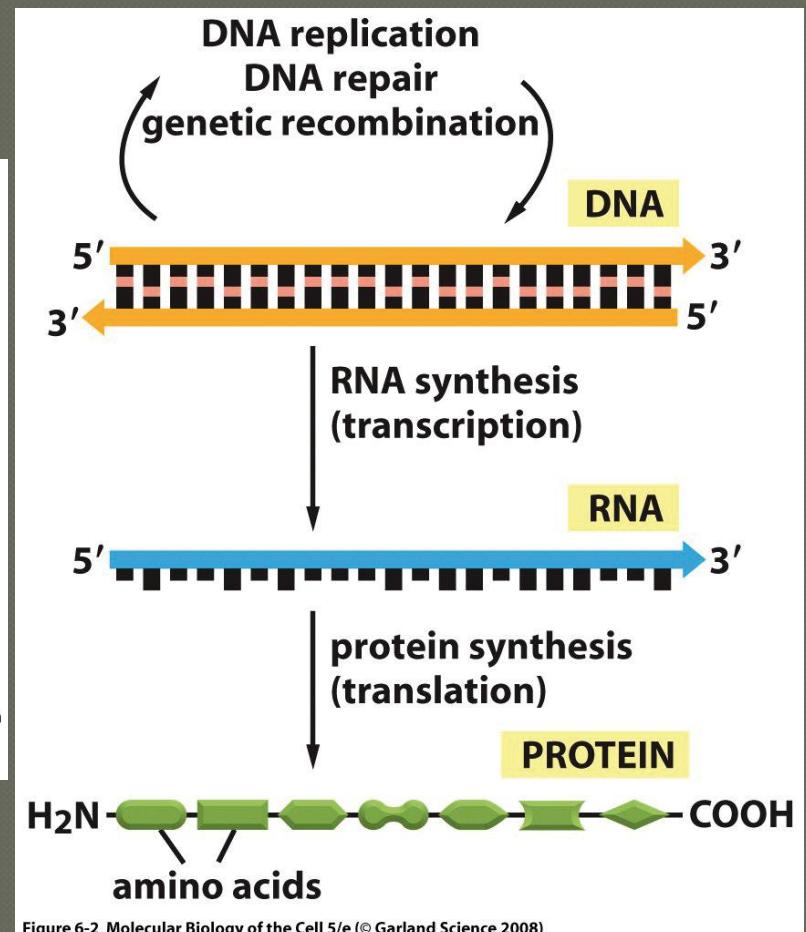
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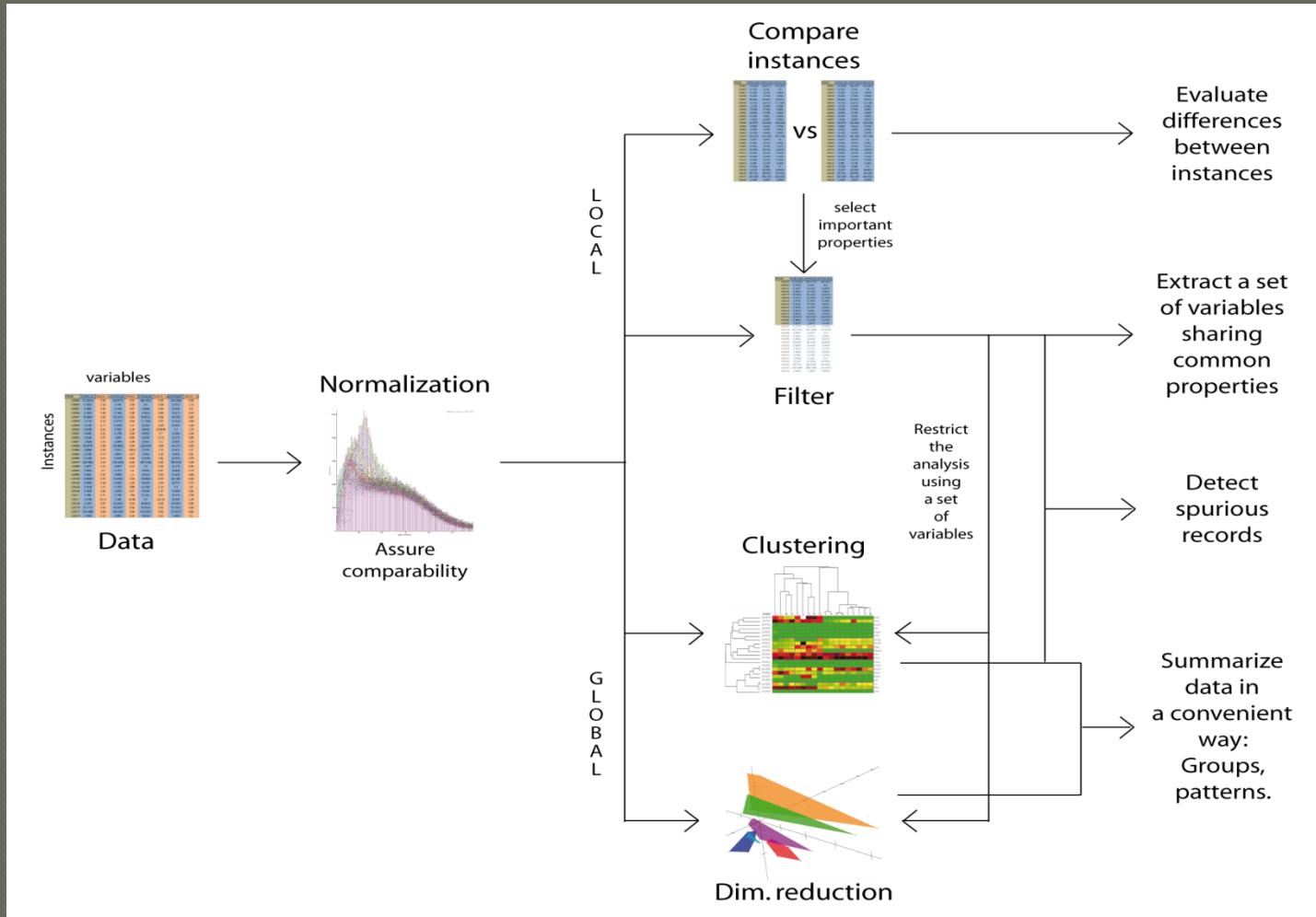
Transcriptome



Albert et al., Molecular Biology of the Cell, 4th Ed



Typical work-flow in data analysis



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- Review of dimensionality reduction techniques
- SVD-MDS
- Pathway network analysis software
- 1st Application: Cerebral Malaria characterization
- 2nd Application: Treg characterization

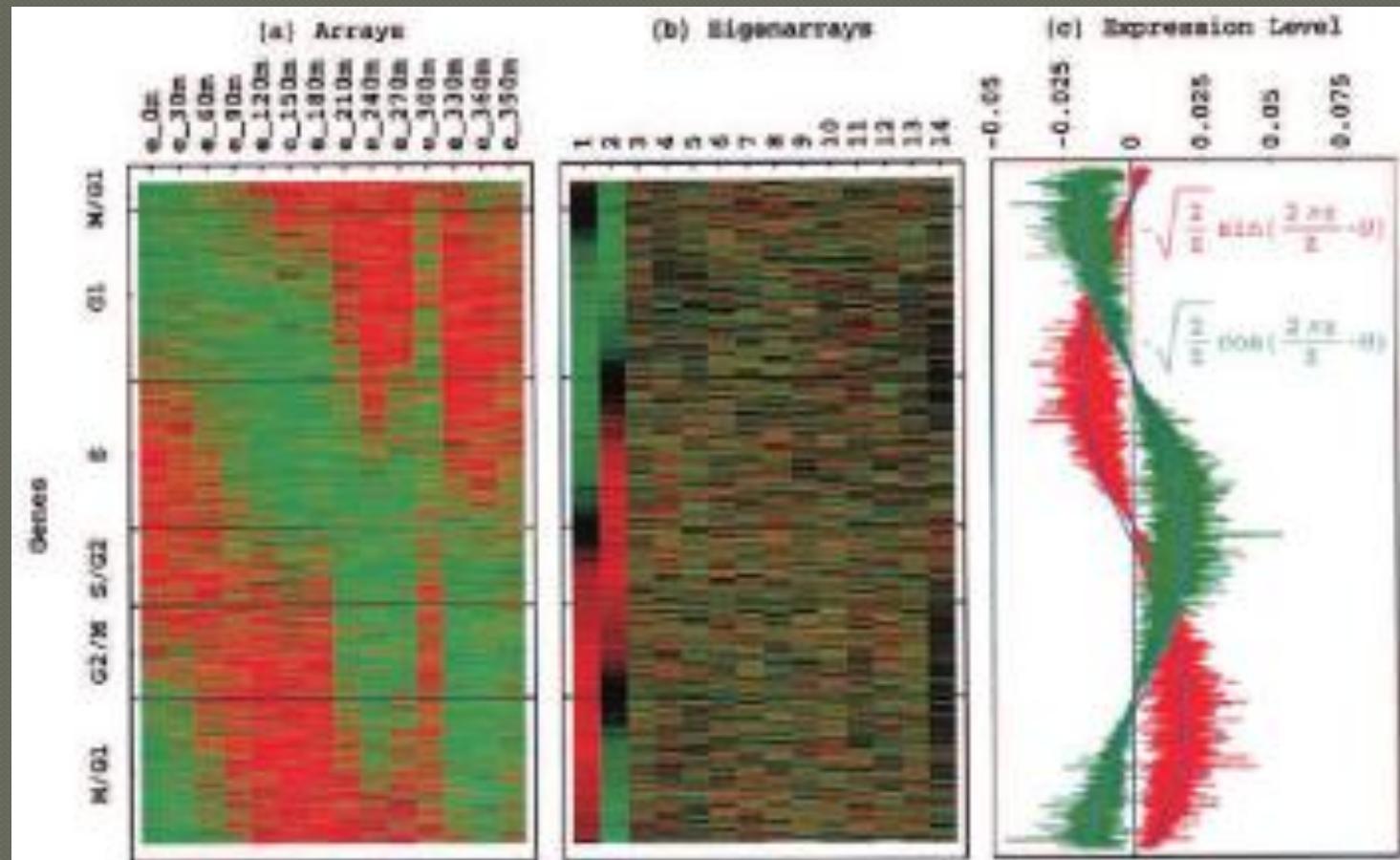
Dimensionality reduction

PROBE	SIGNAL[D1]	VAR[D1_Tcc]	SIGNAL[D2]	VAR[D2_T]	SIGNAL[D4]	VAR[D4_Tcc]	SIGNAL[D5]	VAR[D5_Tcc]
100002	172.8246	0.06	295.0775	0.04	263.3923	0.05	215.4909	0.05
100003	0.7632	2.19	0.155	2.04	0.8	0.29	0.0727	1.15
100027	0.1667	5.39	0.1163	3.47	0.3846	0.54	0.3545	0.2
100036	0.4035	4.86	0.7364	1.36	0.5846	0.89	0.6273	0.44
100037	36.6842	0.06	58.1473	0.04	29.8231	0.06	18.5091	0.05
100039	3.2719	0.14	12.0775	0.04	11.7308	0.07	14.3636	0.04
100044	1.5702	1.77	0.1938	0.4	0.2385	0.58	0.1091	1.59
100045	0.6228	5.52	0.7054	1.16	0.6462	1228.36	0.3	1.73
100051	0.6491	1.01	0.1783	3.26	0.0923	0.7	0.1364	1.04
100052	0.2544	1.07	0.093	0.96	0.2692	11.31	0.2273	0.83
100057	1.0526	1.13	2.2093	0.29	3.5615	0.1	2.0091	0.24
100058	60.6579	0.06	165.8062	0.04	126.6538	0.06	24.1727	0.05
100060	0.8684	0.46	0.2016	149.6	0.2769	1.73	0.1455	2.51
100062	2.0702	0.75	1.6047	6.37	1.4462	3.23	0.4091	0.91
100064	0.2193	3.72	0.2248	0.26	0.2538	1.81	0.2545	0.75
100079	209.4561	0.04	540.1938	0.04	487.0308	0.05	769.0546	0.04
100089	2.0877	0.22	3.6977	0.12	2.0	0.26	4.1273	0.05
100093	0.4825	0.9	0.1473	1.3	0.3462	0.47	0.0818	0.75
100095	0.9561	0.52	0.5659	1.1	0.5231	0.52	0.1455	0.64
100100	18.8509	0.05	36.4264	0.04	28.6846	0.05	44.3182	0.04
100102	0.9035	0.26	0.2326	1.03	0.3538	1.34	0.0727	0.72
100103	0.2018	4.24	0.1705	0.89	0.1769	2.14	0.1	0.5
100105	0.4035	3.64	0.3023	0.57	0.0538	1.37	0.1909	0.55
100111	0.386	0.71	0.1783	1.84	0.1462	0.91	0.1273	0.56
100117	0.3158	19.15	0.186	24.56	0.3	152.31	0.0909	1.24
100120	12.307	0.07	32.2403	0.04	26.5615	0.05	24.8364	0.05
100130	35.7719	0.04	68.5039	0.04	54.9154	0.05	32.5818	0.04
100137	256.4386	0.06	568.1396	0.04	414.0923	0.05	173.9273	0.05
100145	1.4035	0.22	1.0853	0.16	0.6308	0.21	1.4909	0.1

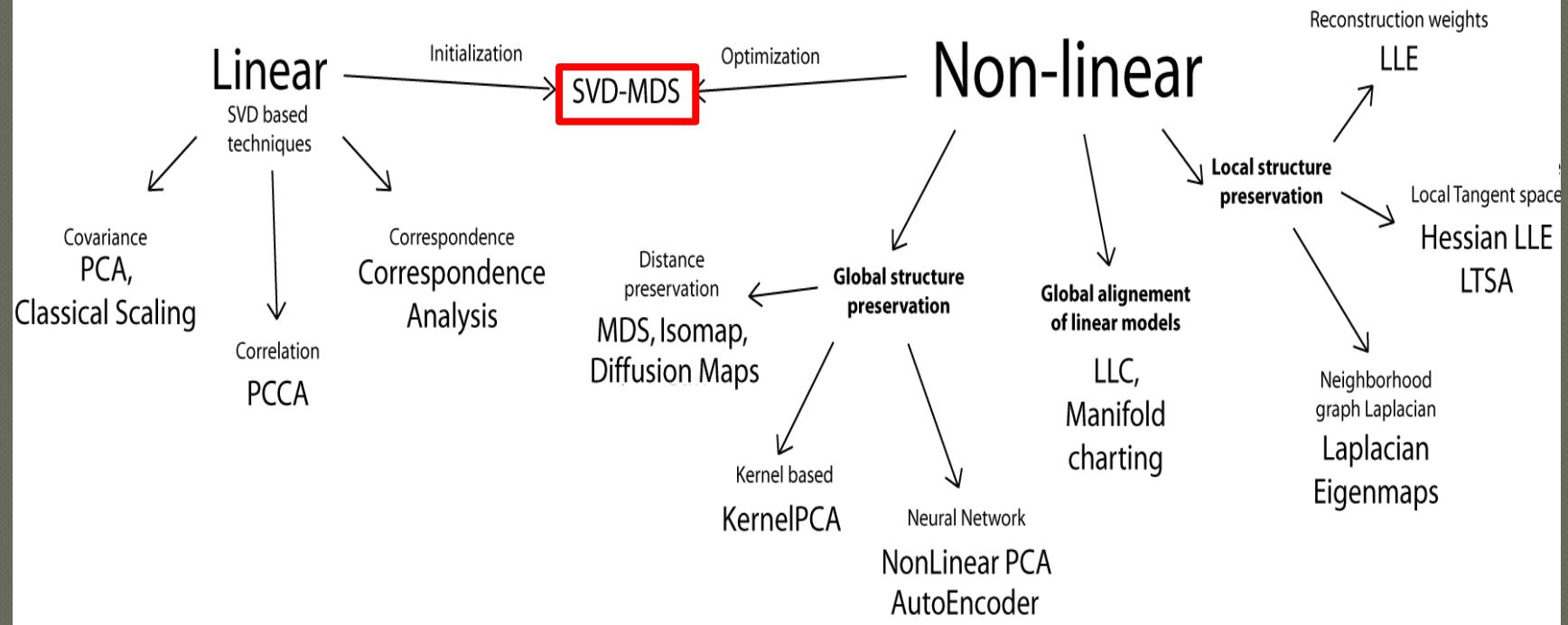


PROBE	axe 1	axe 2	axe 3
100002	-0,005761155	-0,0196512	0,0119491
100003	3,33E-06	-7,64E-06	-3,41E-05
100027	1,56E-05	1,68E-05	-1,35E-05
100036	-2,15E-05	5,47E-05	7,82E-05
100037	-6,07E-04	-0,0032565	-3,98E-04
100039	-1,81E-04	-8,52E-04	7,59E-04
100044	-7,69E-06	1,92E-05	-4,63E-05
100045	-1,48E-06	2,01E-05	-1,08E-05
100051	2,72E-05	1,03E-05	-1,29E-05
100052	2,45E-05	2,98E-05	-4,44E-07
100057	-3,12E-05	9,81E-06	8,40E-05
100058	-0,005544852	-0,0014884	3,56E-05
100060	-4,28E-06	2,66E-05	-2,50E-05
100062	-1,87E-05	1,36E-04	8,07E-05
100064	1,16E-05	1,48E-05	-1,36E-06
100079	-0,008017877	-0,052928	0,0132812
100089	-3,44E-05	-7,79E-05	-6,46E-05
100093	1,21E-05	1,12E-05	-3,78E-05
100095	-2,46E-06	2,76E-05	-4,02E-05
100100	-4,15E-04	-1,19E-04	2,03E-04
100102	4,28E-06	1,75E-05	-3,19E-05
100103	8,46E-06	1,68E-05	1,43E-05
100105	3,09E-05	5,10E-05	5,02E-05
100111	8,07E-06	1,77E-05	-6,58E-06
100117	9,05E-06	3,10E-05	-5,17E-05
100120	-8,48E-04	-0,0027472	5,07E-04
100130	-0,001304086	-0,0035659	3,79E-04
100137	-0,018473712	3,53E-04	0,015201
100145	1,55E-05	-7,17E-06	-3,92E-05

Applications of dimensionality reduction techniques



Alter et al., PNAS, 2000

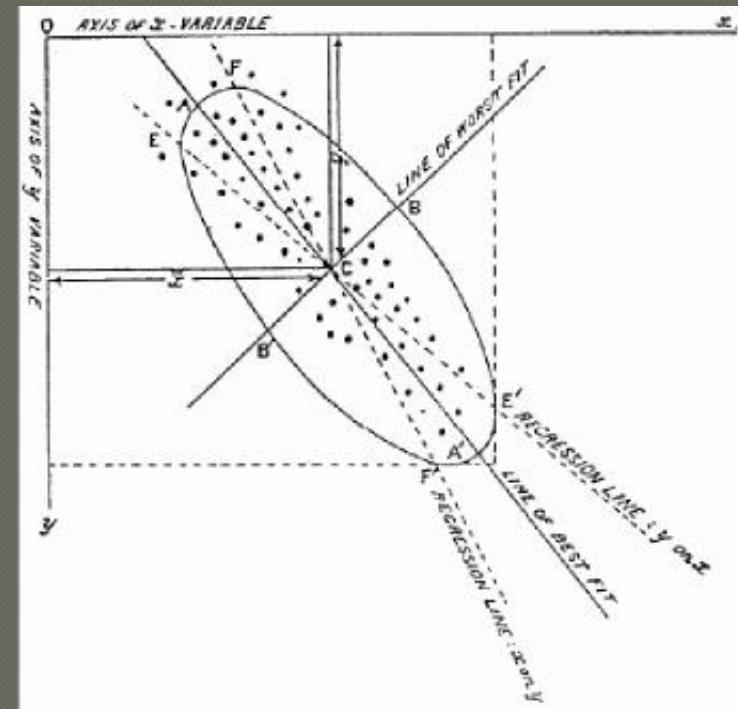
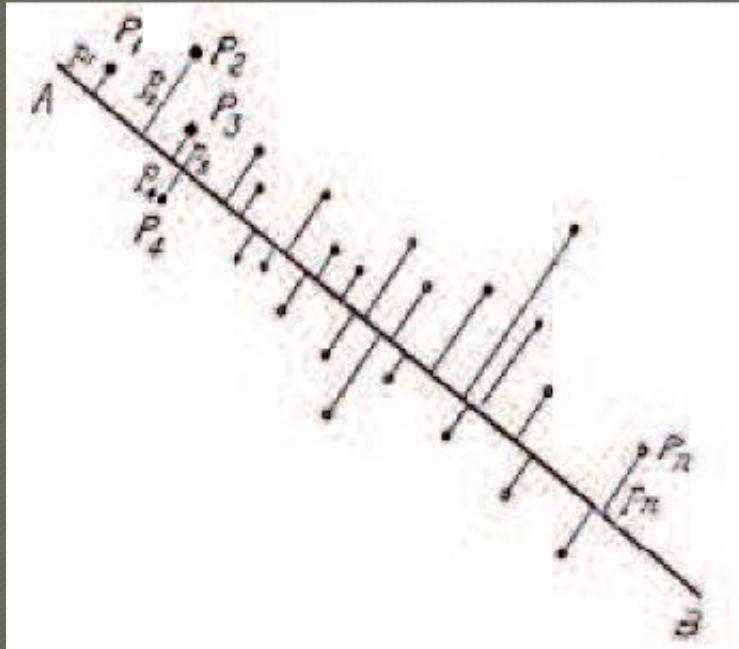


Bécavin et al., Expert Review of Molecular Diagnostics, 2011

Principal Component Analysis

In many physical, statistical, and biological investigations it is desirable to represent a system of points in a plan, three, or higher dimensioned space by the "best-fitting" straight line or plane

K. Pearson, Philosophical Magazine, 1901



Different measures for different linear dimensionality reduction techniques

Covariance (PCA):

$$Cov(x_i, x_j) = E[(x_i - E[x_i])(x_j - E[x_j])]$$

$$Cov(x_i, x_j) = \frac{1}{n} \sum_{k=1}^n x_i^k x_j^k$$

$$CovMatrix = \frac{1}{n} X^t X$$

Correlation (PCCA):

$$Cov(x_i, x_j) = \frac{\frac{1}{n} \sum_{k=1}^n x_i^k x_j^k}{\sigma(x_i)\sigma(x_j)}$$

$$\tilde{X} = \begin{pmatrix} x_{i,j} \\ \sigma(j) \end{pmatrix}$$

Euclidean distance (Classical scaling):

$$d(x^i, x^j)^2 = \sum_k (x_k^i - x_k^j)^2$$

$$XX^t = -\frac{1}{2} H \begin{pmatrix} {d_{11}}^2 & {d_{12}}^2 & \vdots \\ {d_{21}}^2 & \ddots & \vdots \\ \dots & \dots & {d_{nn}}^2 \end{pmatrix} H$$

$$\text{with } H = I - \frac{1}{n} \mathbf{1} \mathbf{1}^t, \text{ and } \mathbf{1} = (1, 1, \dots, 1)^t$$

Chi-square distance
(correspondence analysis):

$$\chi^2(x^i, x^j)^2 = \sum_k \left(\frac{x_k^i}{\sqrt{W \sum_l x_k^l} \cdot \sum_l x_l^i} - \frac{x_k^j}{\sqrt{W \sum_l x_k^l} \cdot \sum_l x_l^j} \right)^2$$

$$\text{with } W = \sum_k \sum_l x_l^k$$

Singular Value Decomposition

$$n \times p = n \times n \times n \times p$$

The diagram illustrates the decomposition of an $n \times p$ matrix into three components. On the left, there is a large rectangle labeled $n \times p$. To its right is an equals sign. Following the equals sign are three smaller rectangles: one labeled $n \times n$, one labeled $n \times p$ containing a red diagonal line, and one labeled $n \times p$ on the far right.

$$X = U S V^t \quad \text{with} \quad s_1 > s_2 > \dots > s_{n-1} > 0$$

Inner product matrix

$$XX^t = U\lambda U^t$$

Outer product matrix

$$X^t X = V\lambda V^t$$

It is easy to demonstrate that inner and outer product matrices have the same eigenvalues, which are linked to singular values

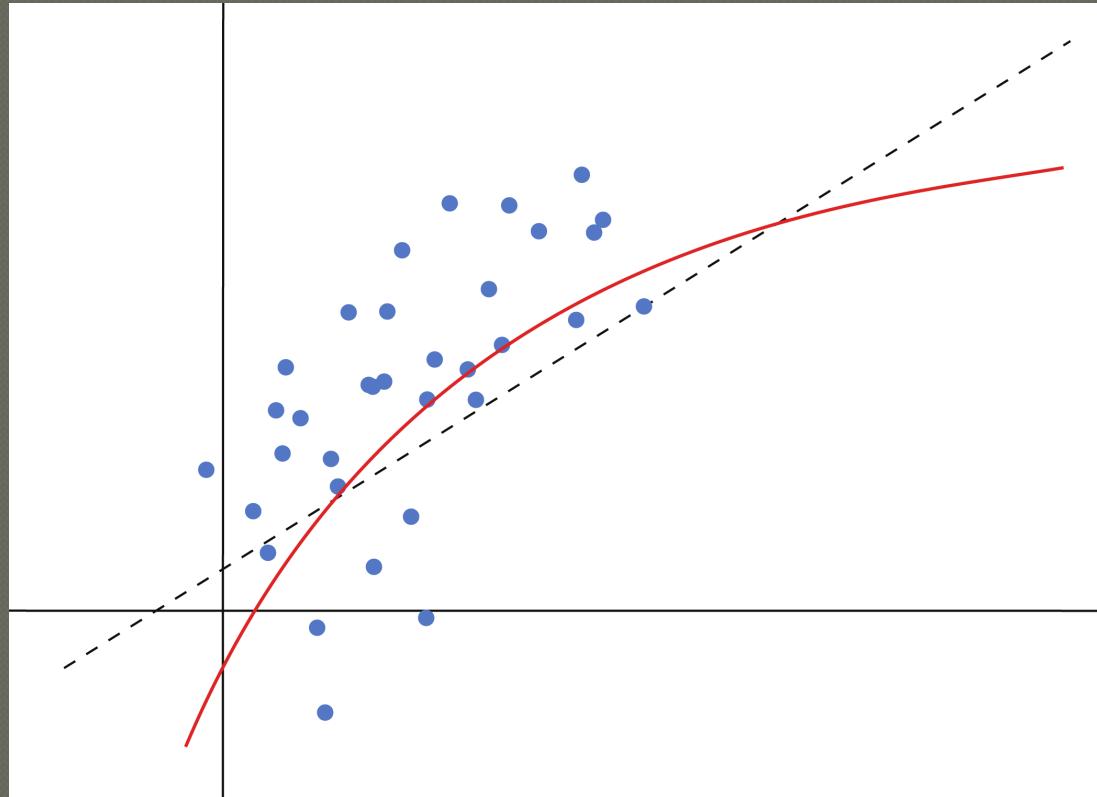
$$s_i^2 = \lambda_i$$

From line to curve: Non-linear PCA

PCA
search for the “best-fitting” line

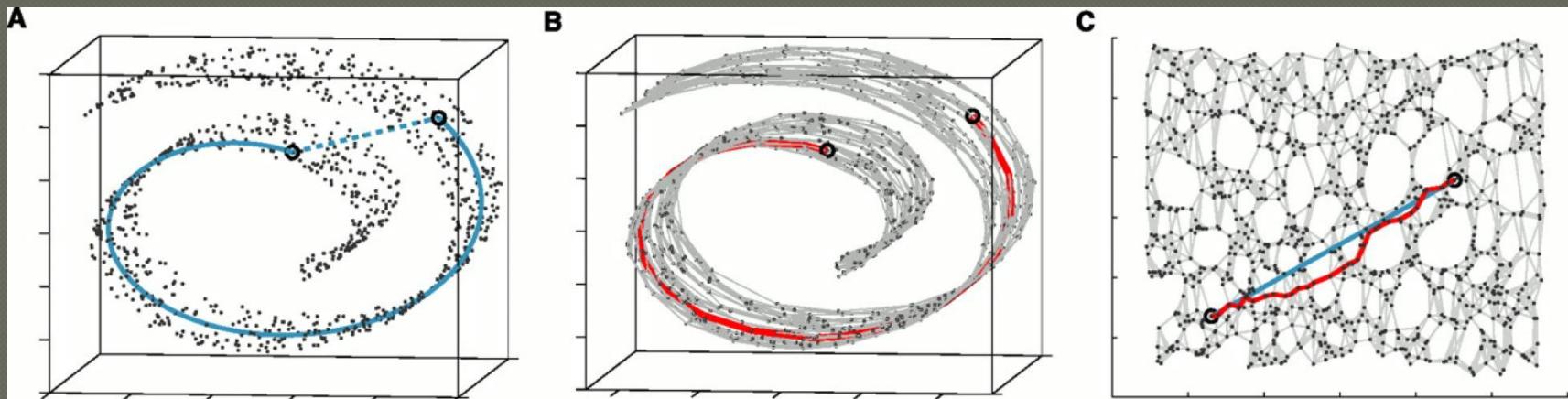


Non-linear PCA
search for the principal curve



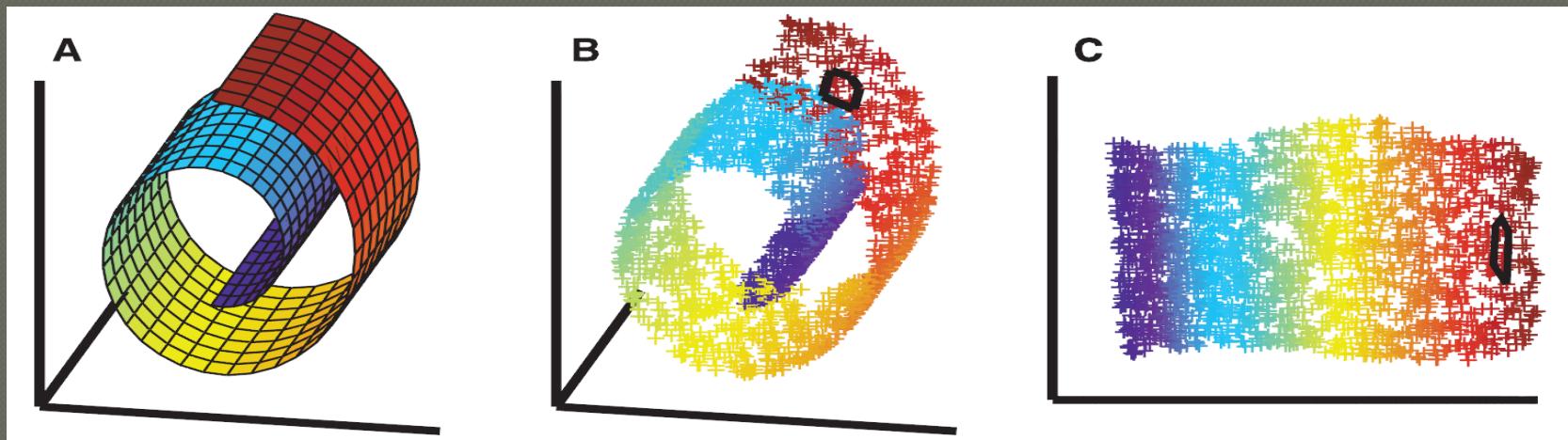
Isomap

Tenenbaum et al. , Science, 2000

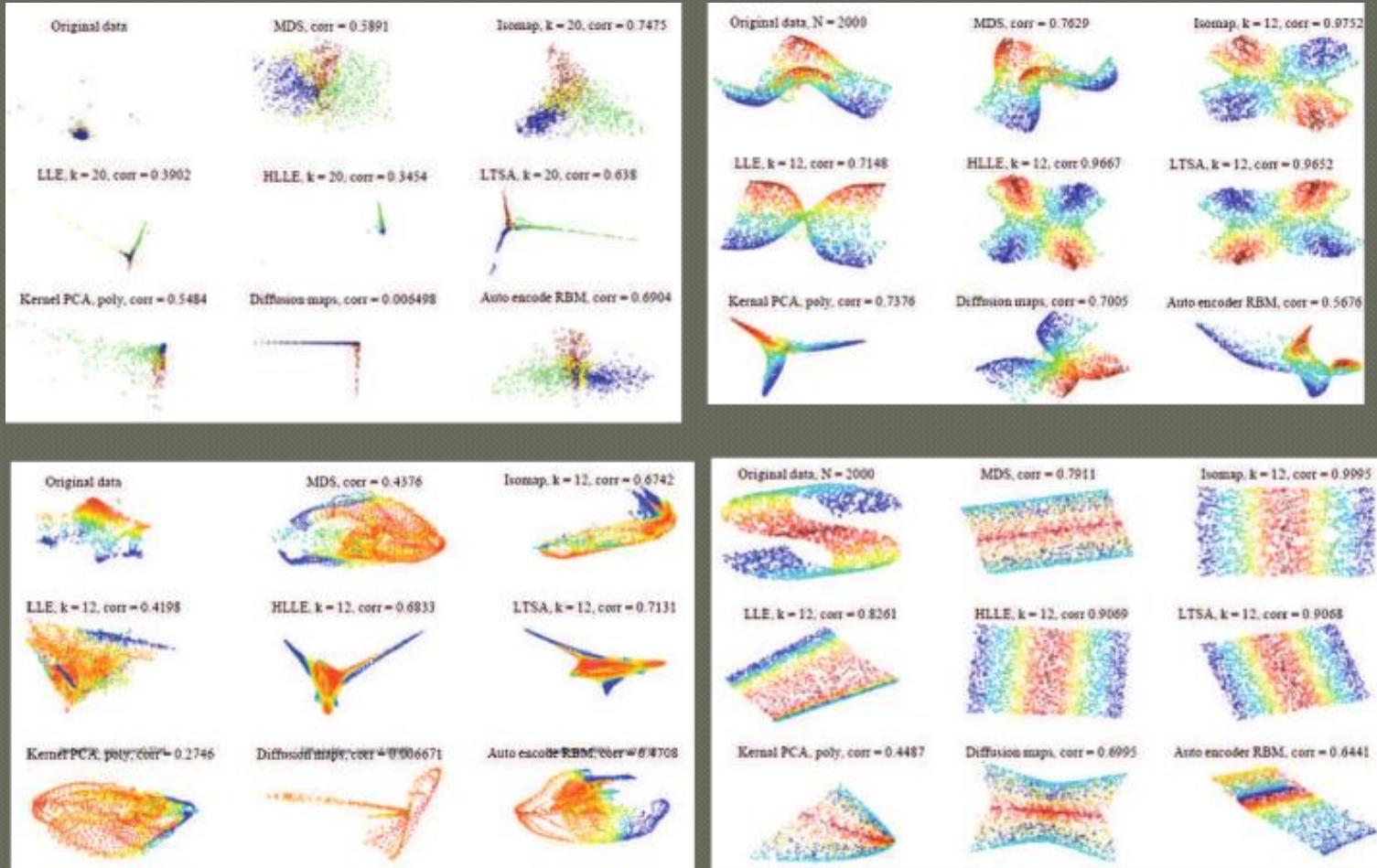


Locally Linear Embedding

Roweis et al. , Science, 2000



A great diversity of results given by each dimensionality reduction technique



Tsai F., Journal of Artificial Intelligence, 2010

Soutenance de thèse de Christophe Bécavin 6 Décembre 2010

Multidimensional Scaling

using Molecular Dynamics approach

- Each pair of points connected by a spring:

$$F_{spring}(x^i, x^j) = -K(\delta(x^i, x^j) - d(x^i, x^j))^2$$

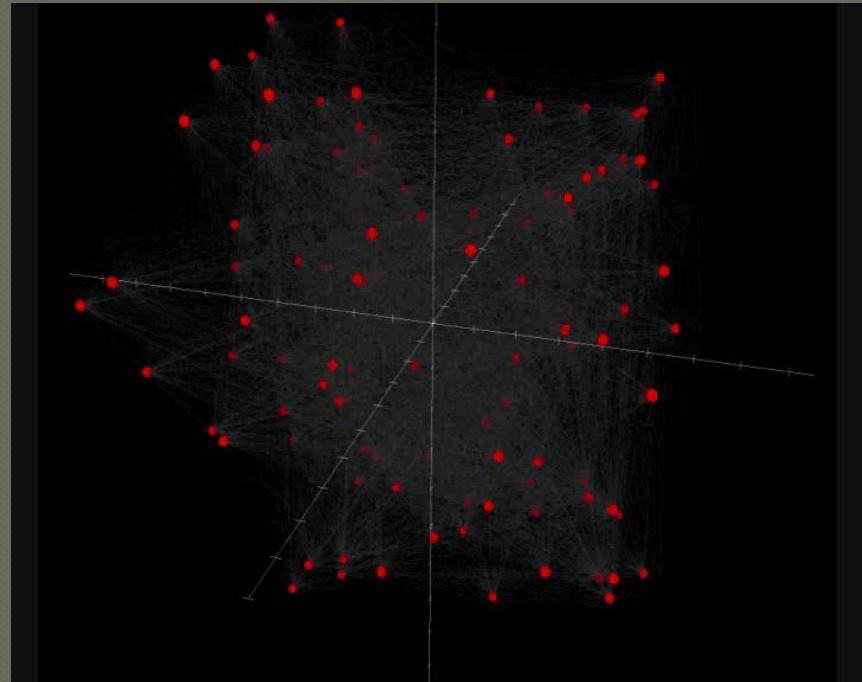
- Calculation of force for all points (non-conservative system):

$$F(x^i) = \sum_{k \neq i} F_{spring}(x^i, x^k) - \gamma \cdot mass \cdot \dot{x}^i$$

- Find new position of all points using Newton equation, and Verlet integration:

$$mass \cdot \ddot{x}^i = F(x^i)$$

$$x^i(t + \Delta t) = 2x^i(t) - x^i(t - \Delta t) + \ddot{x}^i \Delta t^2$$

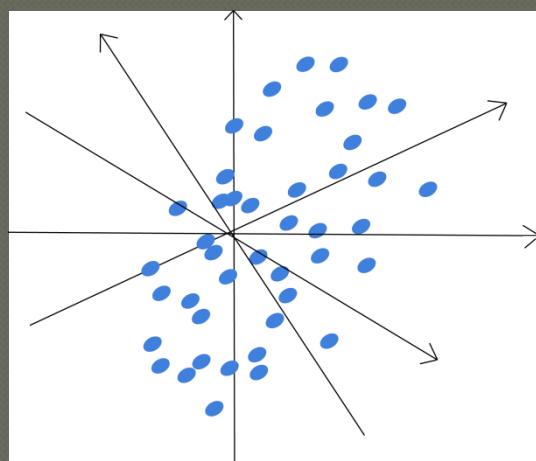


$$Stress = \sqrt{\frac{\sum_i \sum_j (\delta(i, j) - d(i, j))^2}{\sum_i \sum_j (d(i, j))^2}}$$

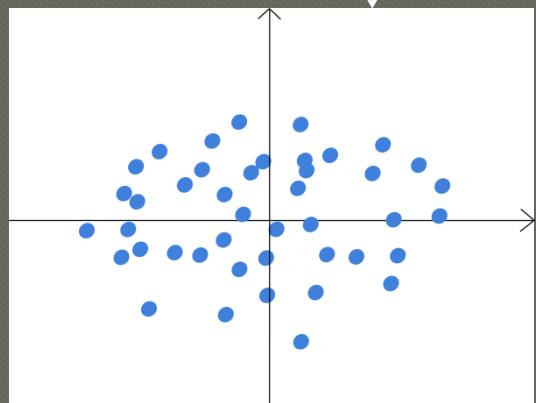
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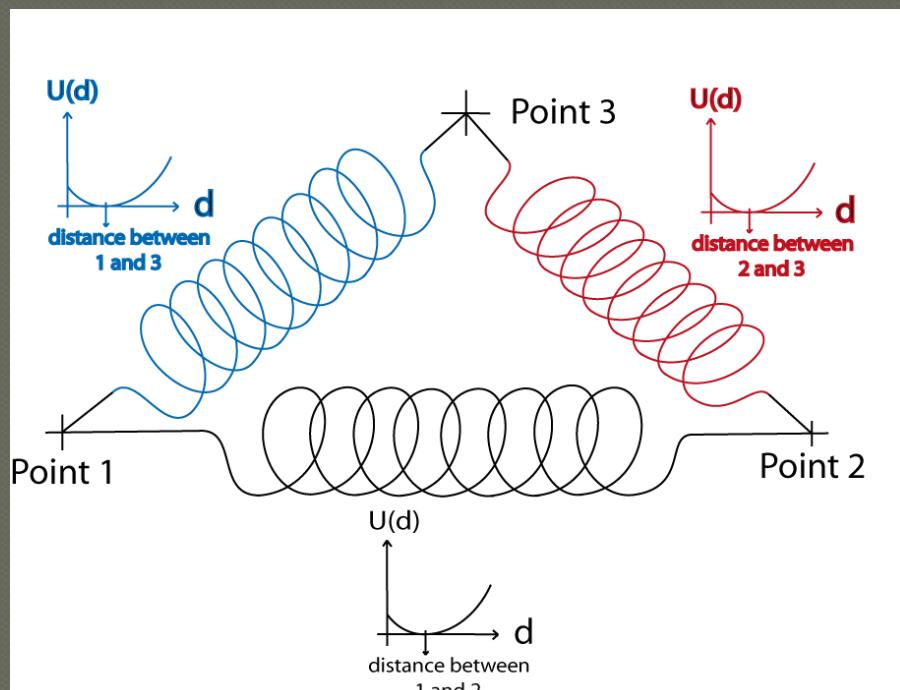
Multidimensional Scaling initialized by Singular Value Decomposition



SVD

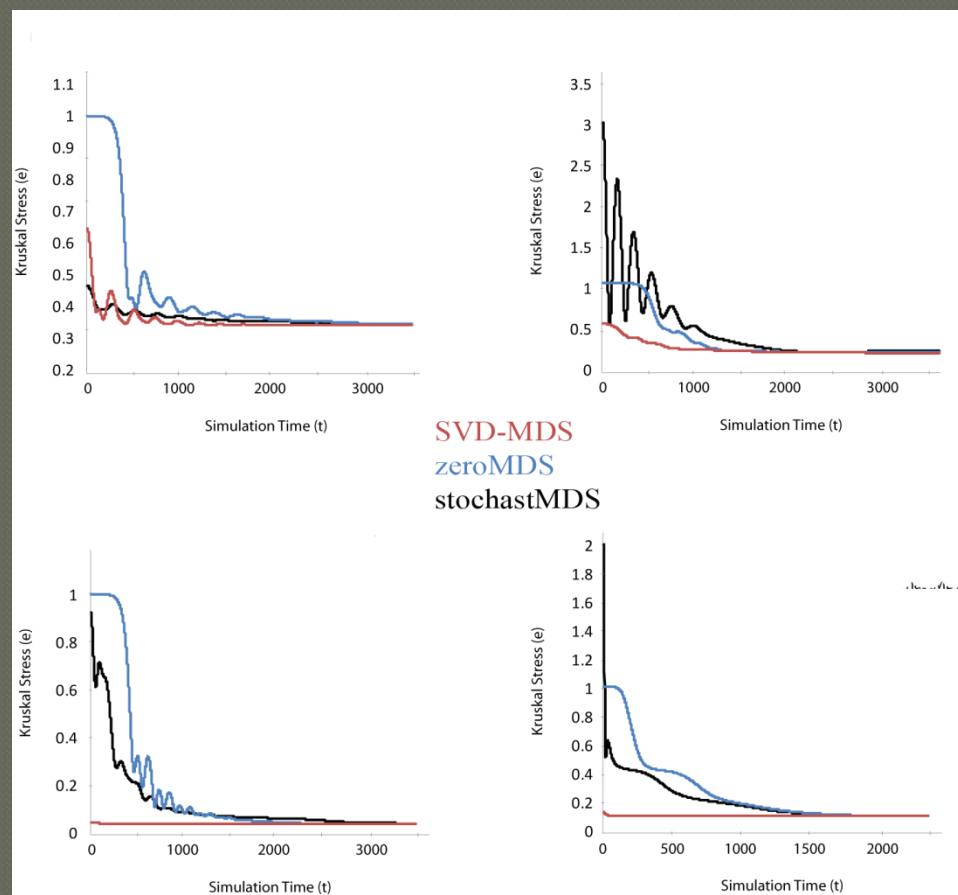


MDS using Spring analogy

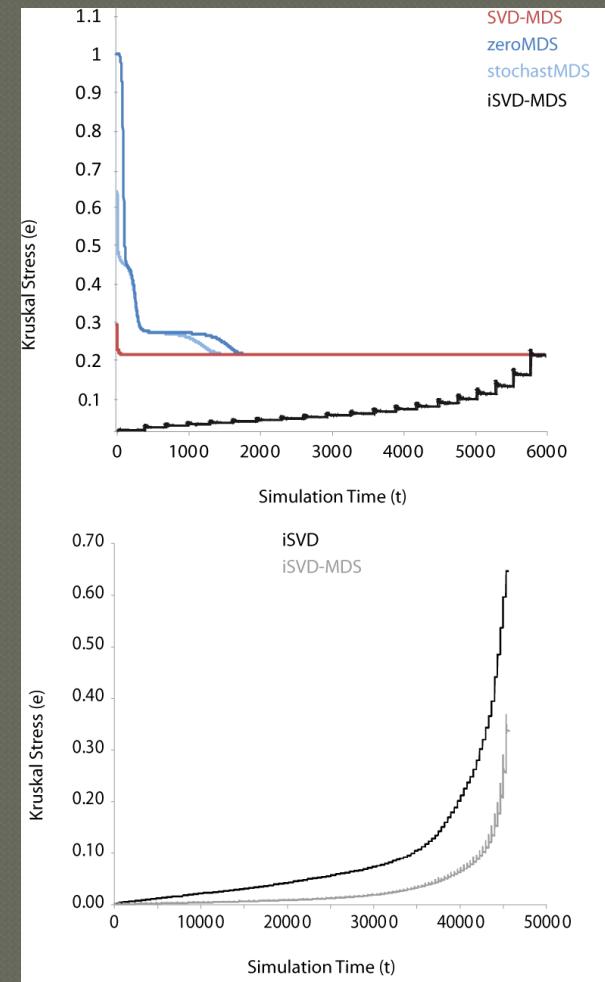
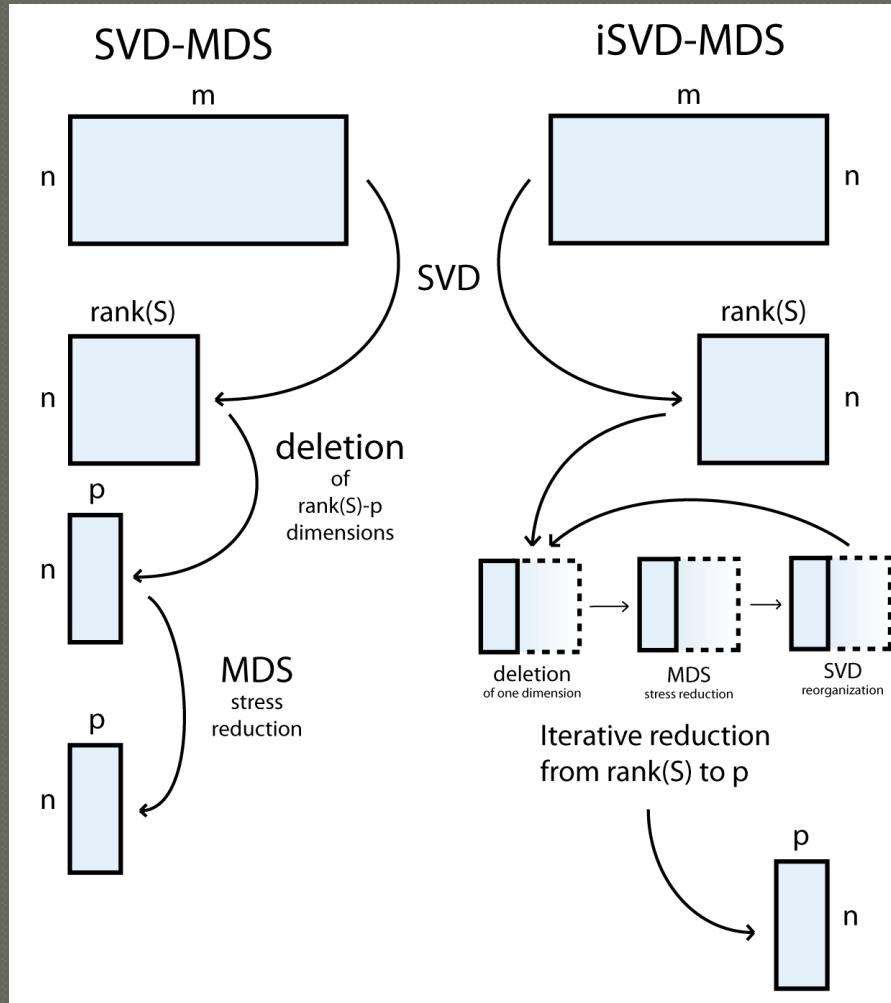


Comparison of different initialization strategies

ID	Dataset Name	No. of Instances	No. of Variables
d1	96Cell	96	32878
d2	96Cell_T	96	1553
d3	Iris	150	4
d4	Wine	178	13
d5	Stochast 200	200	50
d6	CCYier	516	12
d7	Pima	768	9
d8	96Cell_T transposed	1553	96
d9	Secom	1567	590
d10	Ozone	2565	72
d11	Stochast 3000	3000	300
d12	Ecoli	4288	7
d13	Wave	5000	22



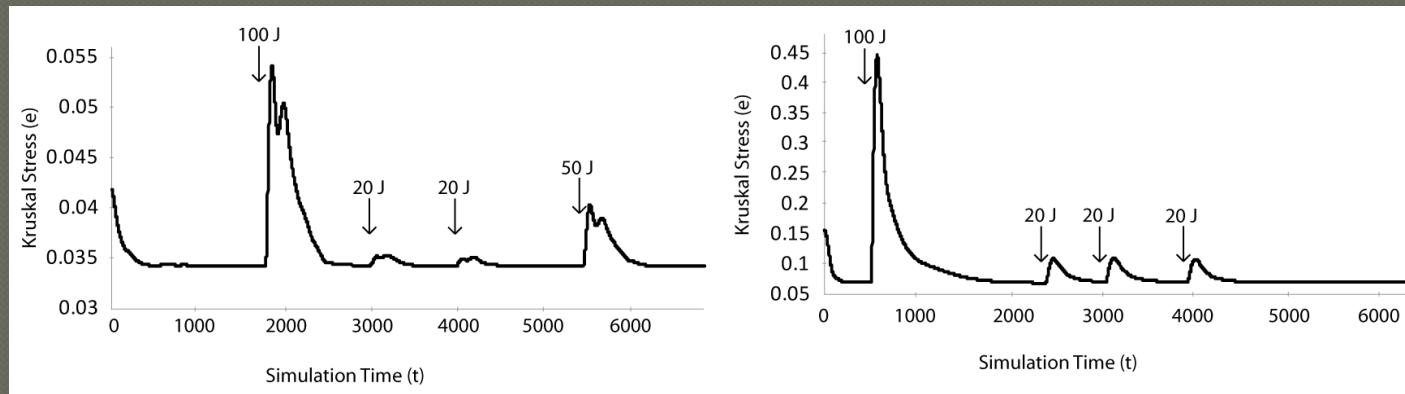
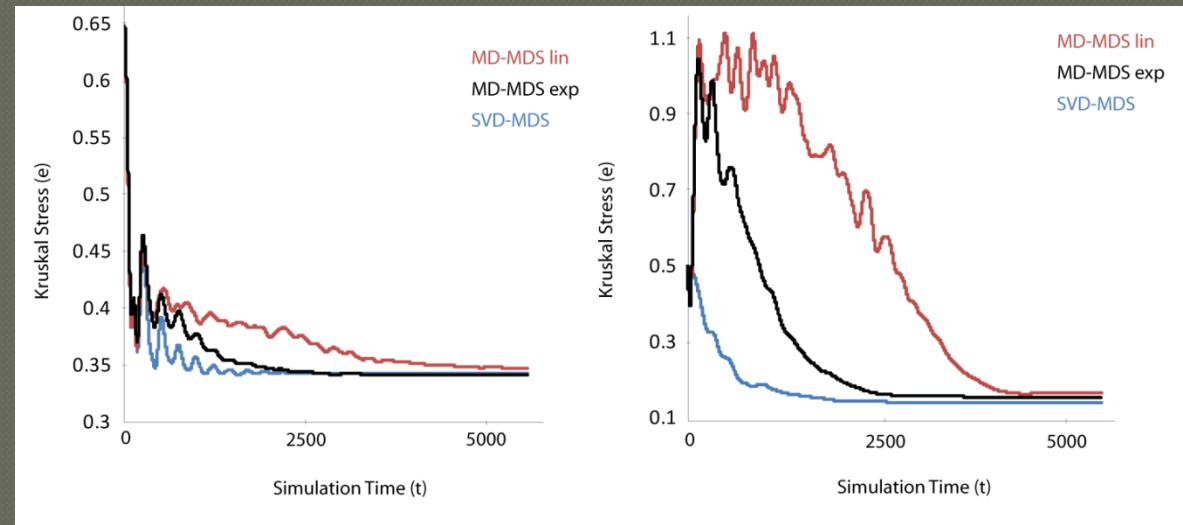
Iterative SVD-MDS



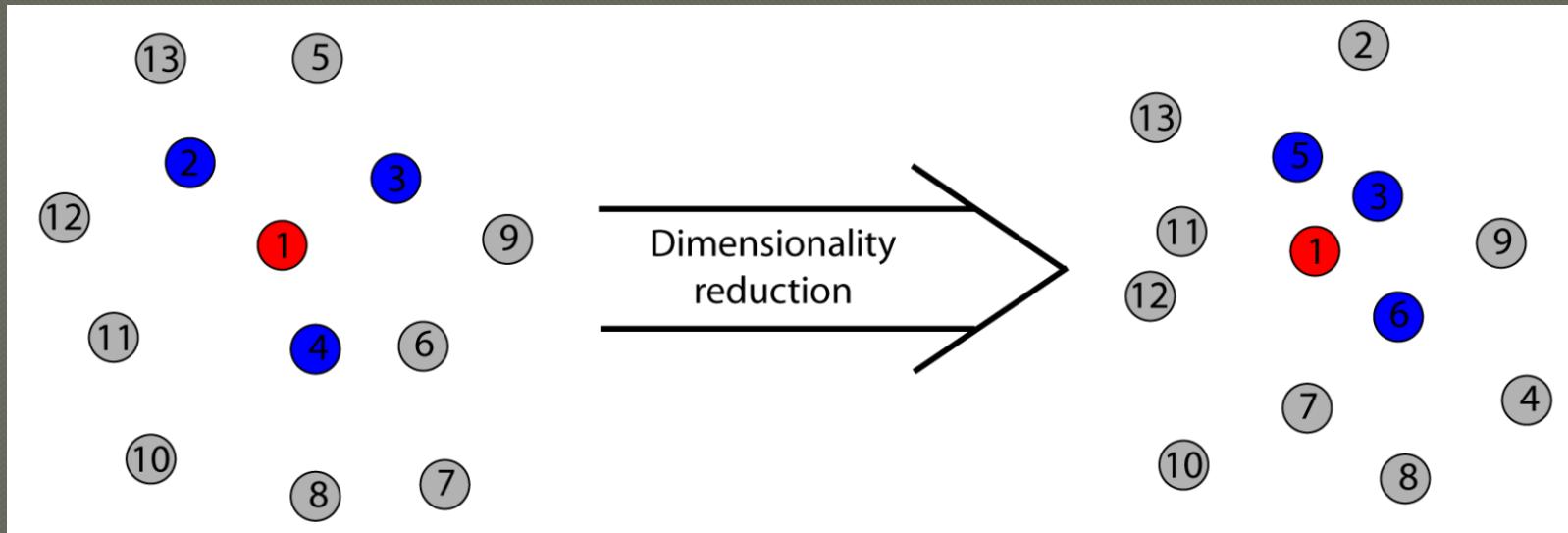
Adding stochasticity to avoid local minima ?

Stochastic force

$$F_{stoch}(x^i) = -T * s(t)$$



Entourage parameter for evaluating local deformation



$$Ent_k = \frac{\sum_{i=1}^n G_i}{G}$$

with $G_i = \text{card}(N_i^{\text{ref}} \cap N_i^{\text{new}})$

and $G = nk$

SVD-MDS

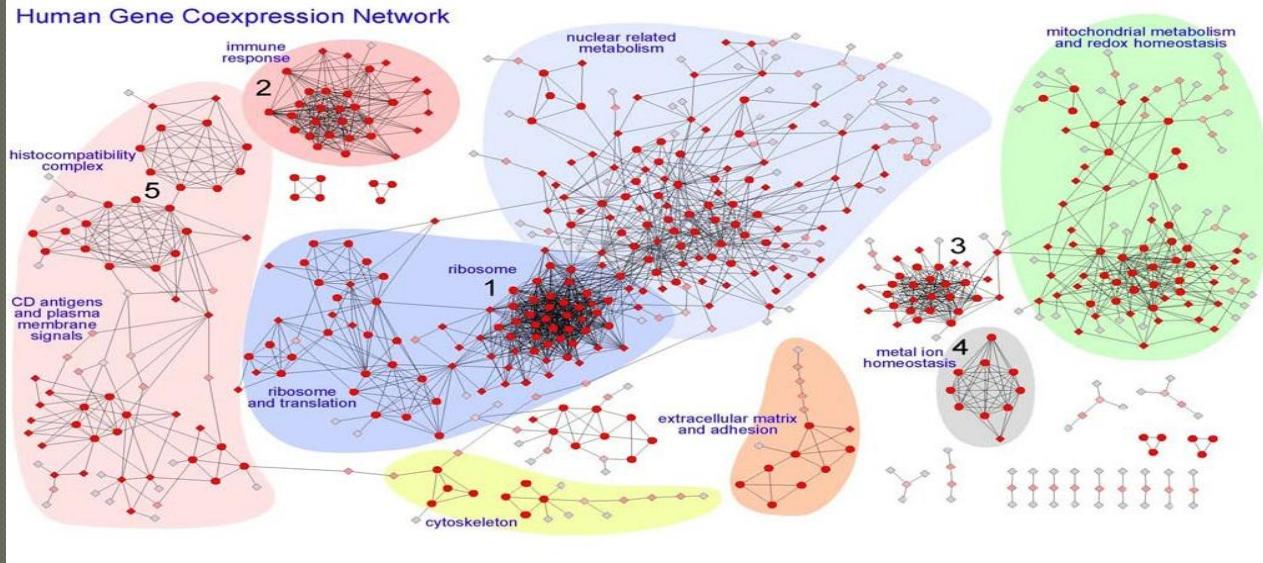
- The use of SVD is the best initialization strategy for MDS;
- Iterative dimensionality reduction does not improve the optimization;
- Adding stochastic also does not improve the process;
- Using parameter for local change assessment we prove that our representation is generally more accurate than the one obtain with our other MDS algorithm.

Bécavin et al., Bioinformatics, *Submitted*

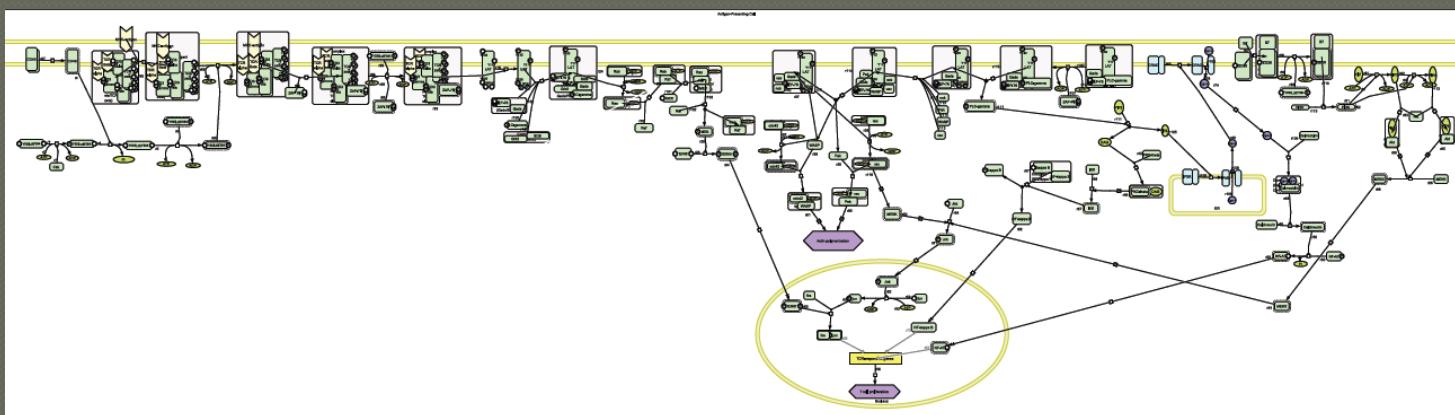
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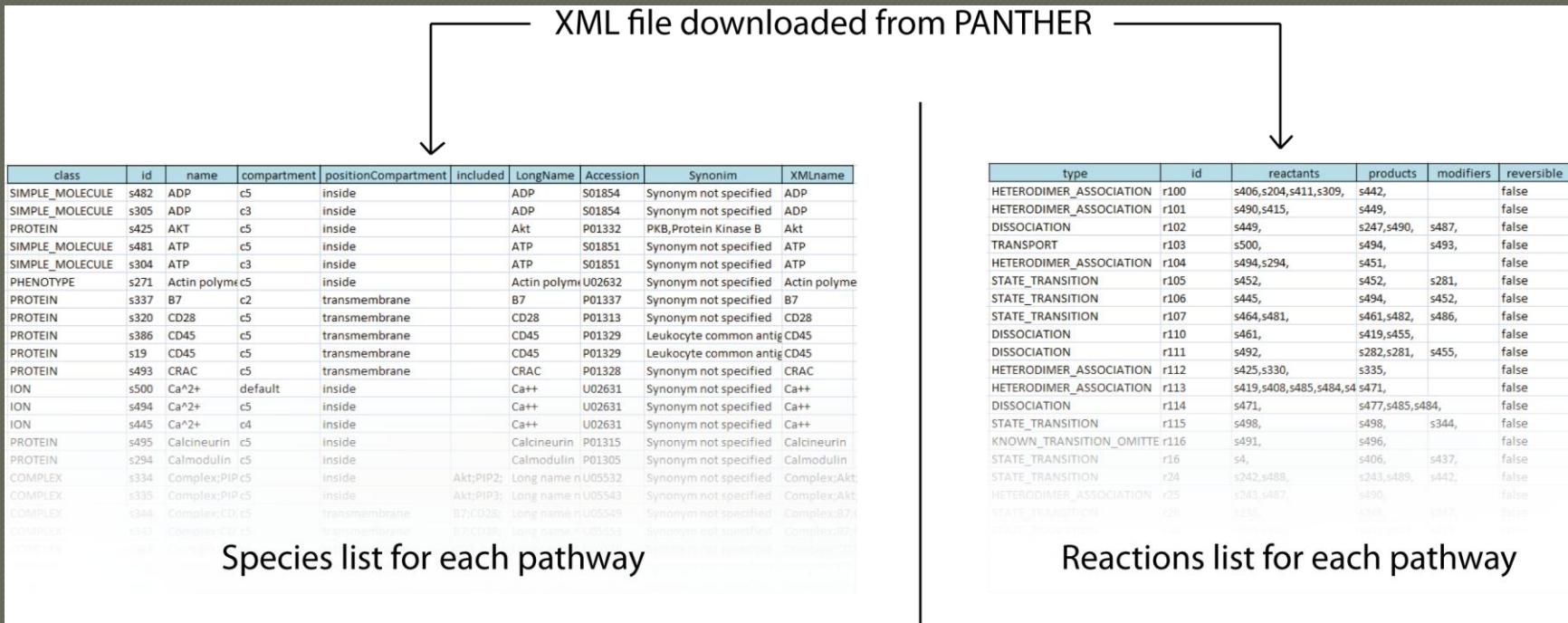
Gene expression and Pathway structure integration



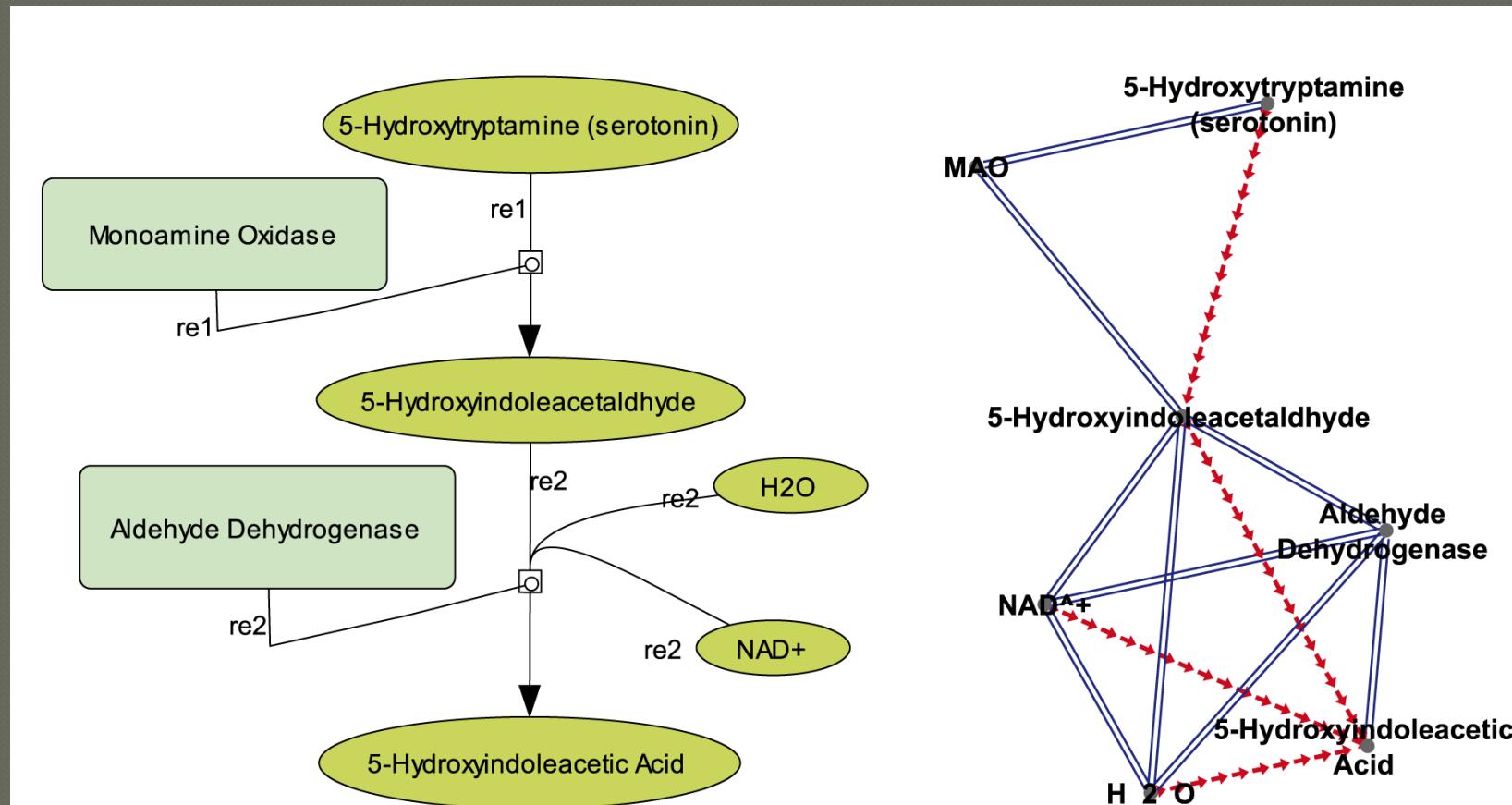
Prieto et al.,
Plos One
2008



Retrieving and curation of pathways: List of species and list of reactions

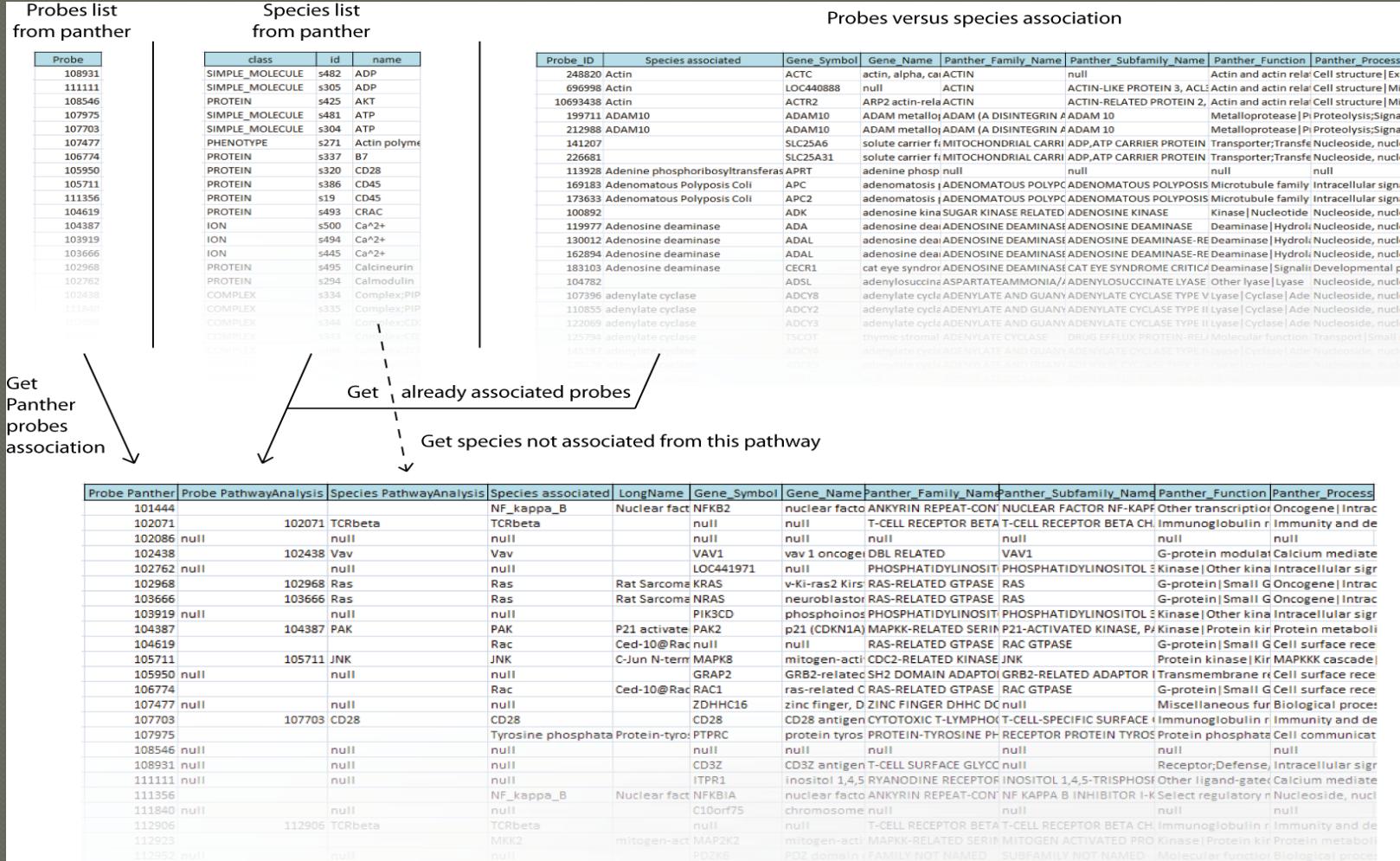


Obtaining the list of reactions



Association of all species to their probes

67% (908/1345) of proteins associated



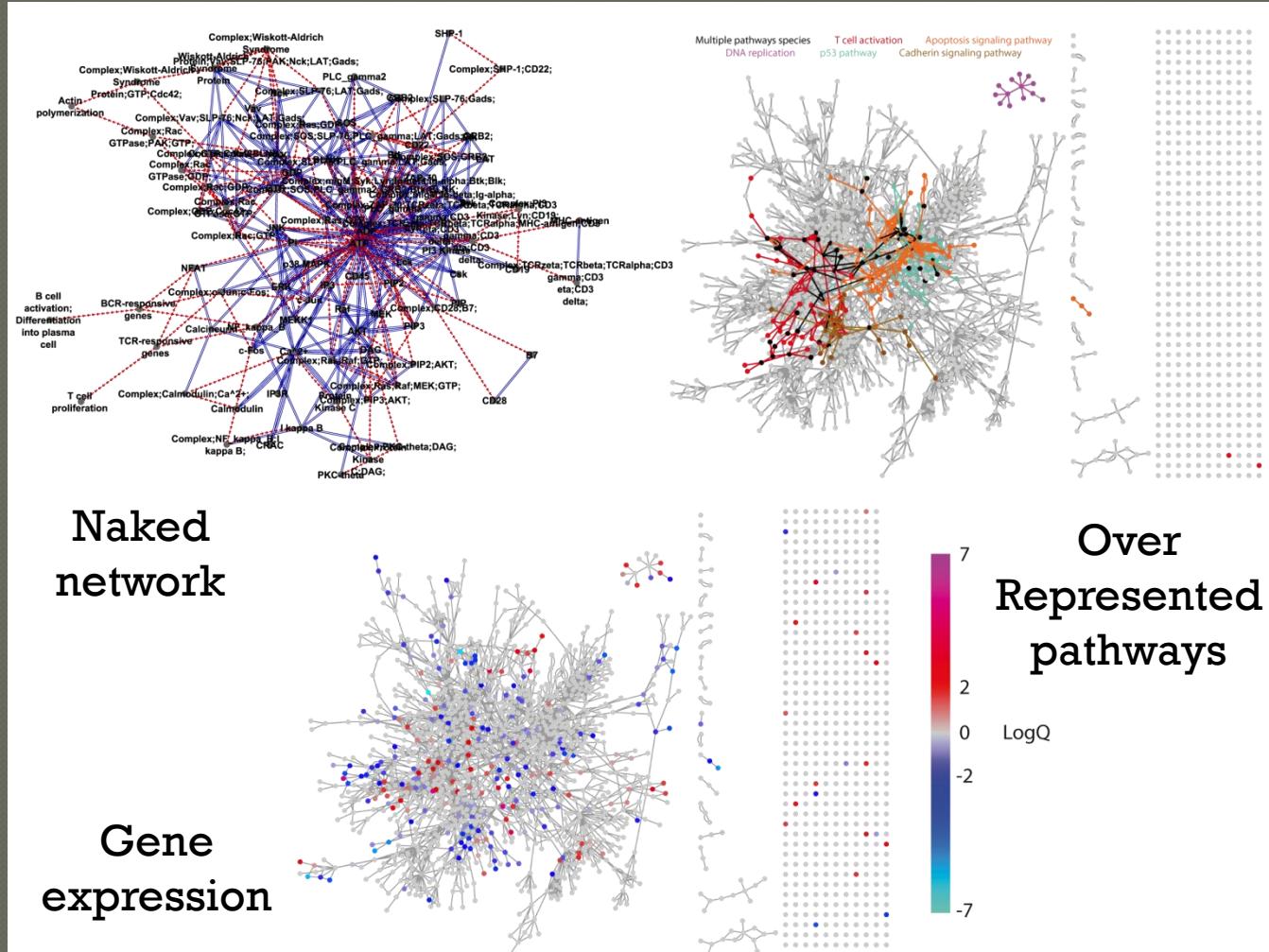
Different types of networks that can be constructed

Selection of species and reactions → Nodes and edges of the network

The screenshot shows the 'Global Pathway Analysis' software interface. The window title is 'Global Pathway Analysis'. The menu bar includes 'File', 'Set Preferences', 'Initialization', and 'Curate SpeciesVsprobes file'. The toolbar contains icons for various functions: mao, ma7, PAIEK, Acemap data, Automatic association results, Francois Xavier file, Historique des modifs species, Images, and a search icon. Below the toolbar is a 'PackageExplorer' tree view showing a 'Pathway network' folder containing files like '.svn', 'Acemap data', 'Automatic association results 2.t', 'Automatic association results rel', 'Automatic association results rel', 'Automatic association results.txt', 'FrancoisXavier file', 'Historique des modifs species na', 'Images', 'ma0', 'ma7', 'Nouveau document texte (2).txt', 'Nouveau document texte.txt', 'Nouveau document textedccxxc', 'PathwayInfo', 'PathwayNetworkBuildScript', 'PathwayNetworksJava', 'PathwayResultPajek', 'PathwayVsProbes', 'PathwayXML', 'Probe_vs_species file creation.txt', and 'RessourceFiles'. The main area has tabs for 'List of Species', 'List of Reactions', 'List of Pathways', 'Probes vs Species', and 'Correction Name of species'. The 'List of Species' tab is active, displaying a table with columns: ID, Species Name, Species Class, X, Y, Z, Color, expr, occu..., and Marg... . The table lists various biological entities with their properties. At the bottom is a 'Console' tab showing log messages: 'Get colors of reactions', 'Finished: Ma0 reading and parsing', 'Uninclude the selection of species', and 'Uninclude the selection of species'.

ID	Species Name	Species Class	X	Y	Z	Color	expr	occu...	Marg...
411	Cadherin	PROTEIN	0.0	0.0	0.0	Gray20	8.875...	189.0	1677...
2063	Receptor	PROTEIN	0.0	0.0	0.0	Gray20	3.762...	107.0	402.6...
1023	Cytokine Receptor	PROTEIN	0.0	0.0	0.0	Red	12.93...	100.0	1293...
930	Complex;hormone;Receptor;	COMPLEX	0.0	0.0	0.0	Green	0.036...	98.5	3.552...
881	Complex;beta-Catenin;Cadherin;	COMPLEX	0.0	0.0	0.0	Green	0.011...	95.5	1.114...
963	Complex;p120;Cadherin;	COMPLEX	0.0	0.0	0.0	Green	0.011...	94.5	1.114...
516	Complex;Cytokine Receptor;Cytokine;	COMPLEX	0.0	0.0	0.0	Green	0.025...	93.0	2.398...
1682	Myosin	PROTEIN	0.0	0.0	0.0	Red	18.65...	93.0	1734...
2612	hormone	PROTEIN	0.0	0.0	0.0	Gray20	3.703...	90.0	333.2...
1022	Cytokine	PROTEIN	0.0	0.0	0.0	Gray20	4.982...	86.0	428.5...
1139	E2	PROTEIN	0.0	0.0	0.0	Red	20.37...	79.0	1609...
2315	Tyrosine phosphatases	PROTEIN	0.0	0.0	0.0	Red	23.92...	78.0	1866...
893	Complex;beta-Catenin;alpha-Catenin;Cadherin;	COMPLEX	0.0	0.0	0.0	Green	0.013...	66.33...	0.885...
652	Complex;Myosin;Actin;	COMPLEX	0.0	0.0	0.0	Green	0.053...	65.5	3.499...
1437	Histones	PROTEIN	0.0	0.0	0.0	Gray20	6.506...	63.0	409.8...
629	Complex;JAK;Cytokine Receptor;Cytokine;	COMPLEX	0.0	0.0	0.0	Green	0.017...	62.66...	1.106...
1385	Growth Factor	PROTEIN	0.0	0.0	0.0	Gray20	2.683...	58.0	155.6...
1512	Interleukin	PROTEIN	0.0	0.0	0.0	Gray20	3.197...	55.0	175.8...
1188	Ets	PROTEIN	0.0	0.0	0.0	Gray20	2.326...	53.0	123.2...
1904	Phosphodiesterase	PROTEIN	0.0	0.0	0.0	Gray20	2.840...	53.0	150.5...
616	Complex;INF_gamma_Cytokine Receptor;	COMPLEX	0.0	0.0	0.0	Green	0.116...	51.0	5.925...

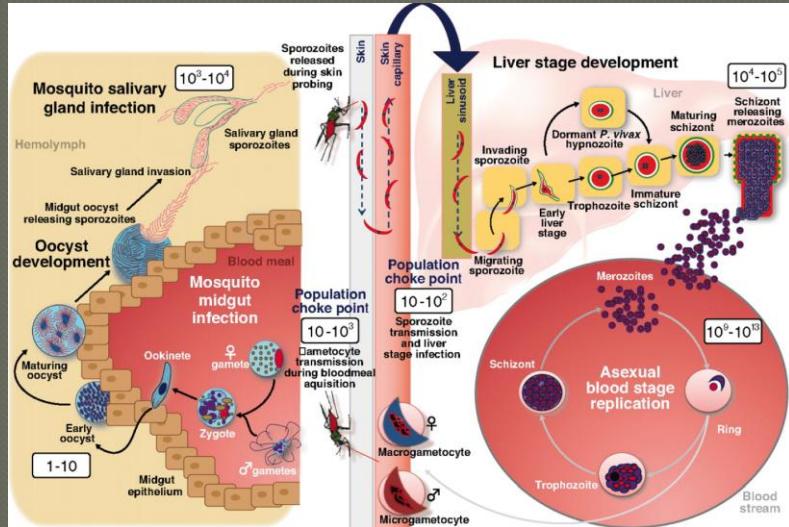
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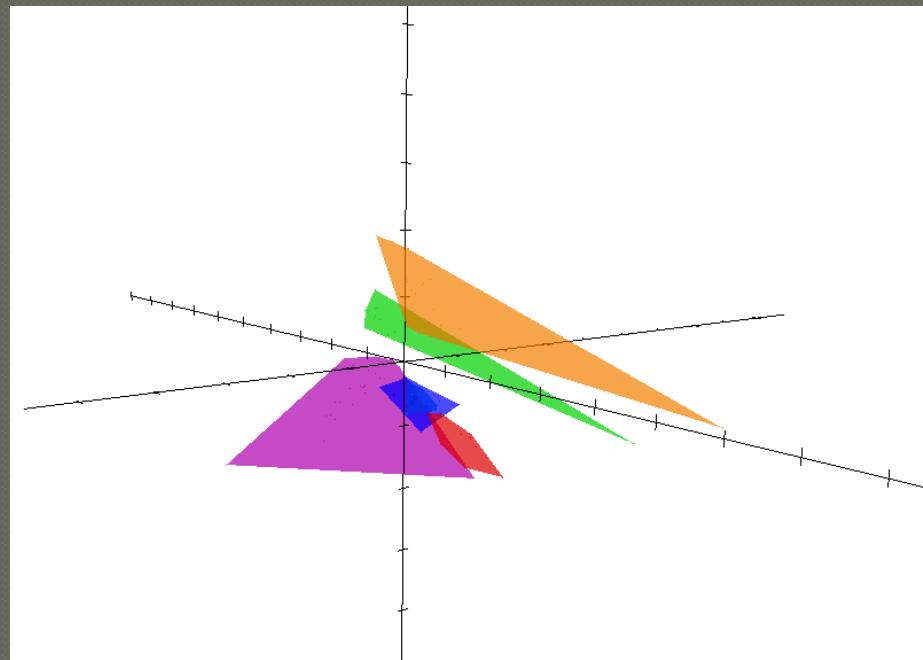
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Cerebral Malaria characterization using auto-antibodies and Cytokines



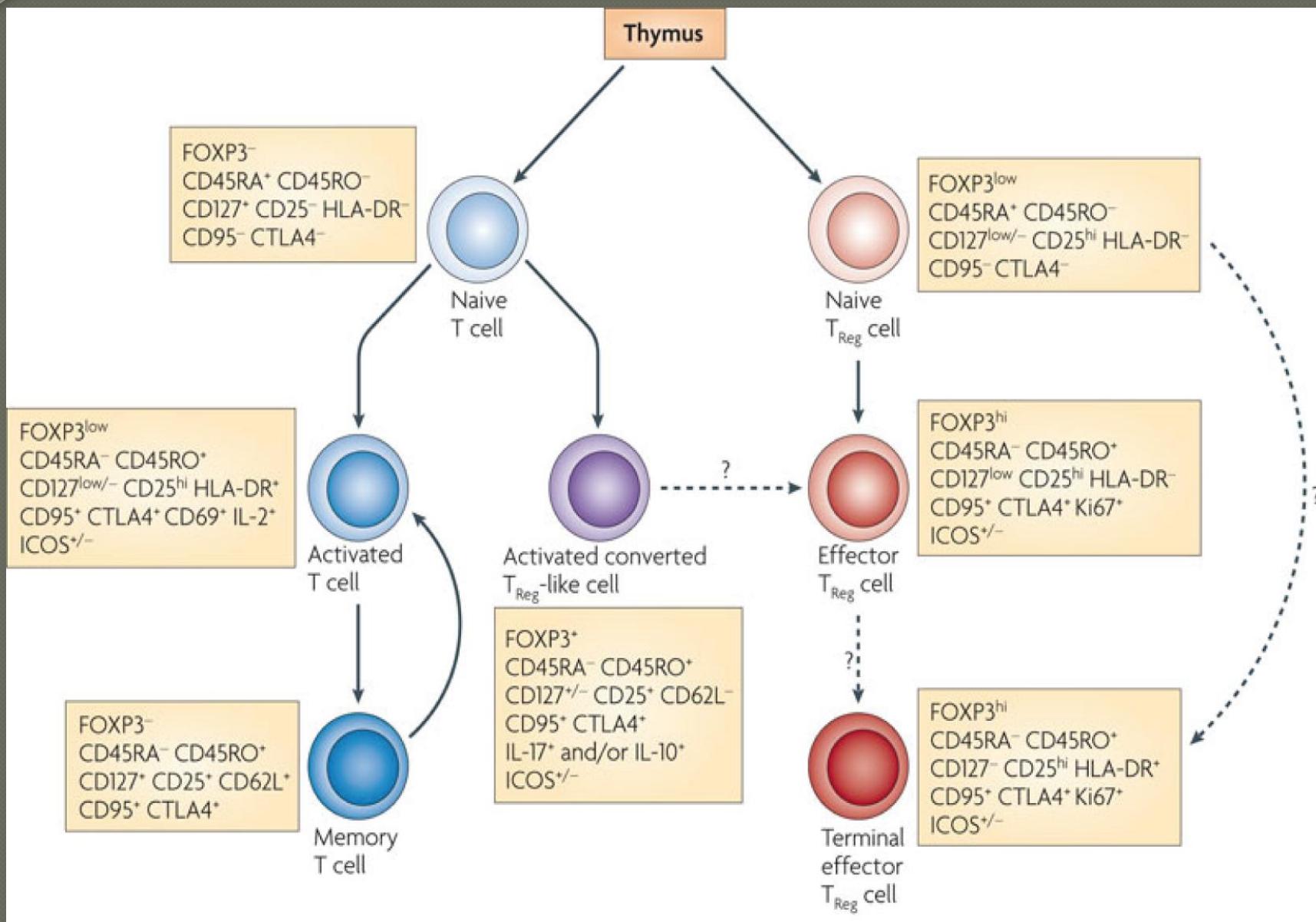
IgG Autoantibody to Brain Beta Tubulin III Associated with Cytokine Cluster-II Discriminate Cerebral Malaria in Central India.
D. Bansal, F. Herbert, P. Lim1, P. Deshpande, C. Bécavin,...
..., A. Benecke, S.Pied., PLoS ONE, 2009

Cerebral malaria (CM)
Severe non-cerebral malaria (SM)
Mild malaria (MM)
Recovered cerebral malaria (ex-CM)
Endemic controls (EC)
Non-endemic controls (NEC)



Index

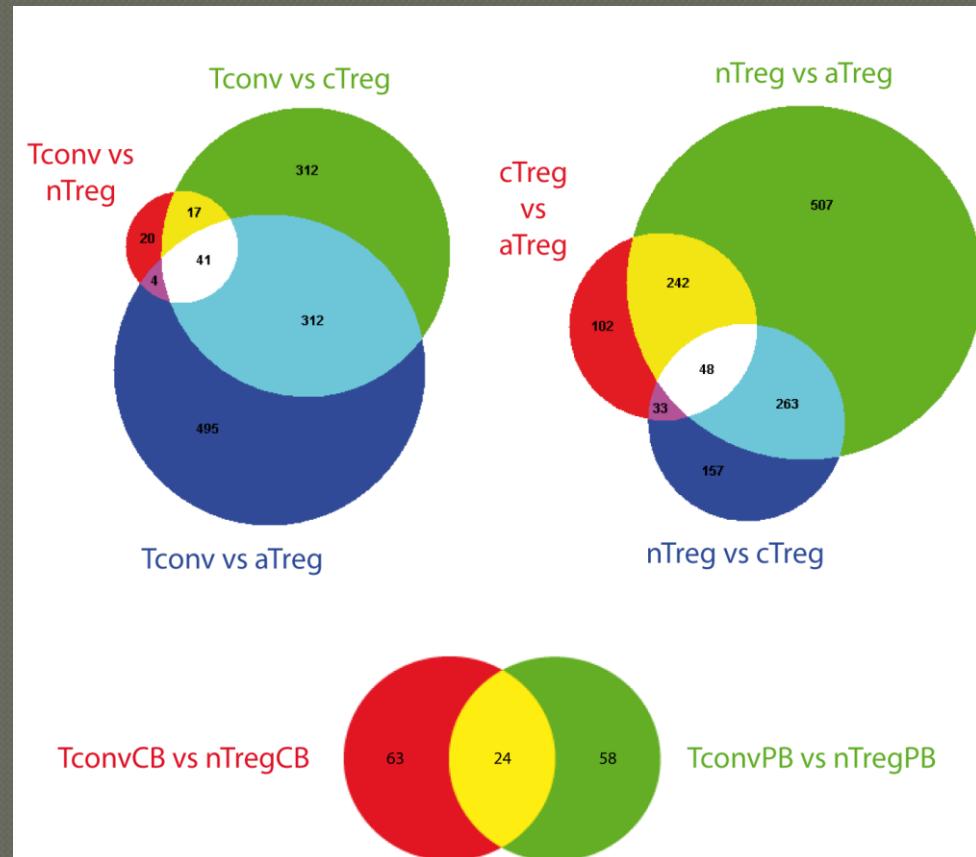
- Review of dimensionality reduction techniques
- SVD-MDS
- Pathway network analysis software
- 1st Application: Cerebral Malaria characterization
- 2nd Application: Treg characterization



We have defined a multitude of gene sets (signatures) specific to each biological condition

Peripheral blood:

- aTreg (activated Treg)
 $CD4+CD25hiCD127-CD45RA-HLADR+$
- cTreg (cytokine emiter Treg)
 $CD4+CD25hiCD127-CD45RA-HLADR-$
- nTreg (naive Treg)
 $CD4+CD25hiCD127-CD45RA+HLADR-$
- Tconv
 $CD4+CD25-CD45RA+HLADR-$

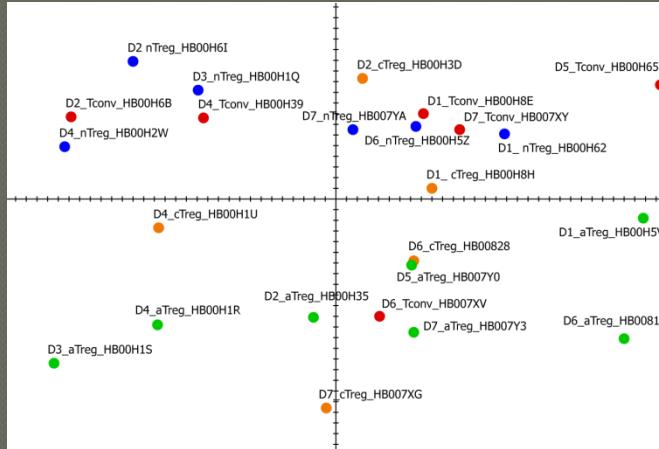


Cord Blood:

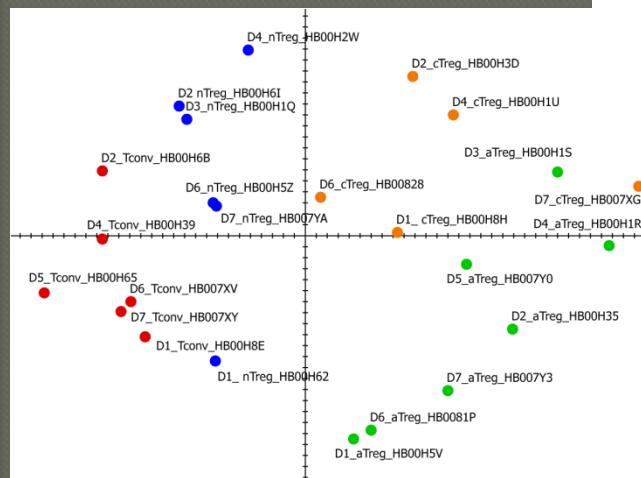
- nTreg (naive Treg)
 $CD4+CD25hiCD127-CD45RA+HLADR-$
- Tconv
 $CD4+CD25-CD45RA+HLADR-$

Representation (in correspondence basis) of the different Treg subsets for the different signatures constructed

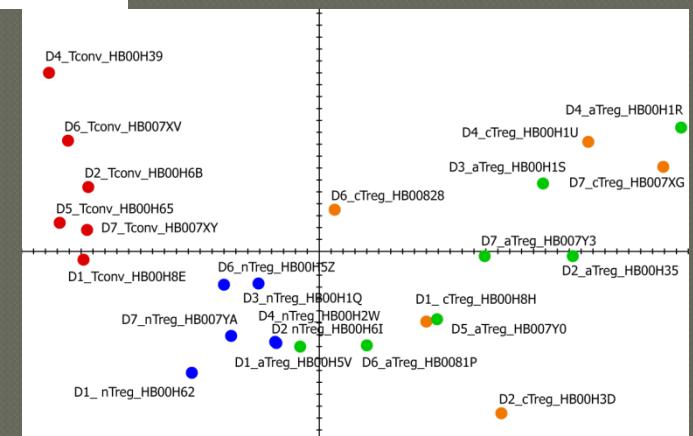
Total signature
1201 probes over-represented
and under-represented
(in comparison to Tconv)
for at least one Treg subset



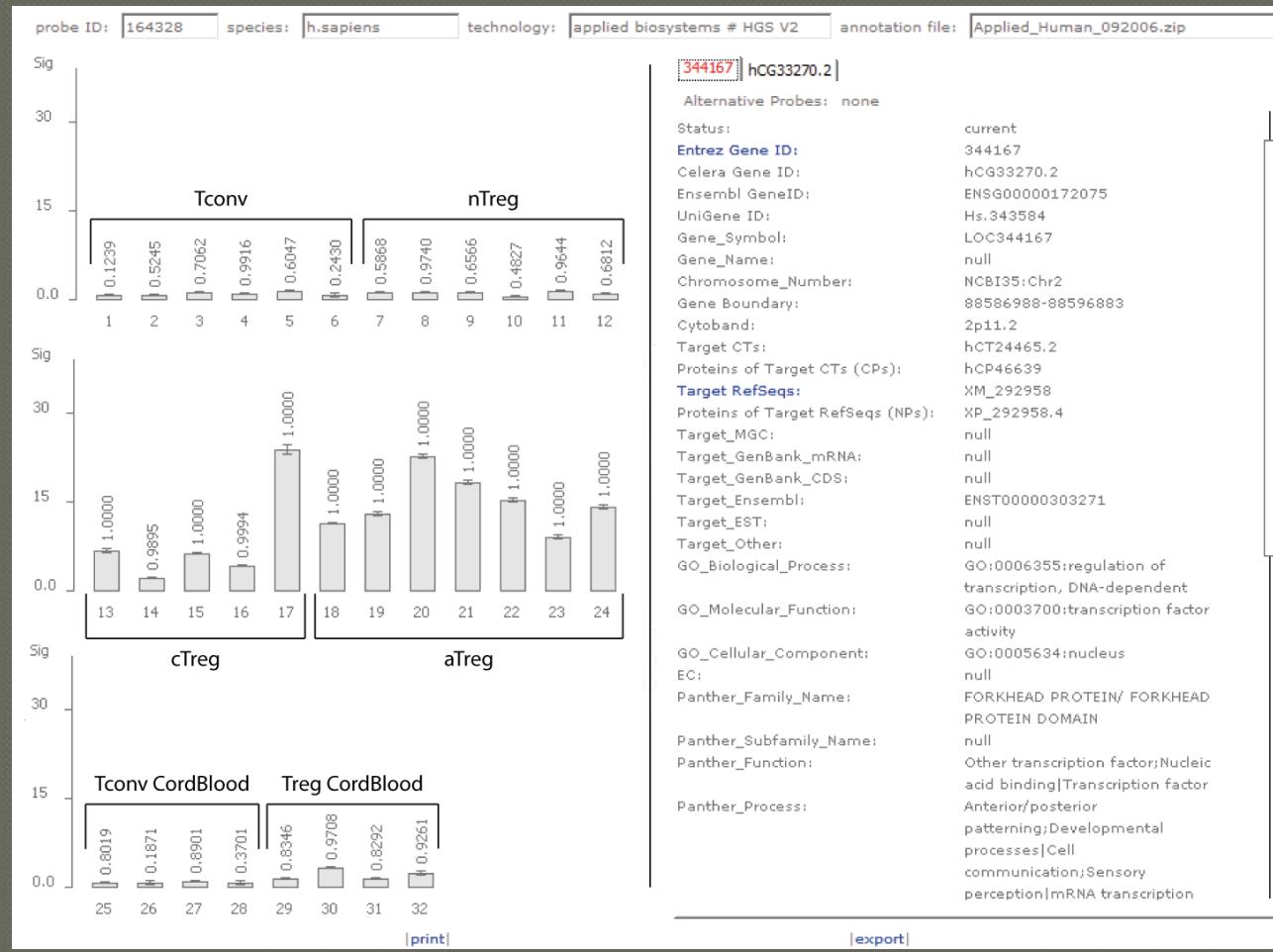
Core signature
41 probes over-represented
and under-represented
(in comparison to Tconv)
for every Treg subset



All probes
Tconv nTreg
cTreg aTreg



FOXLF a new transcription factor !



344167 hCG33270.2

Alternative Probes: none

Status:

current

Entrez Gene ID:

344167

Celera Gene ID:

hCG33270.2

Ensembl GeneID:

ENSG00000172075

UniGene ID:

Hs.343584

Gene_Symbol:

LOC344167

Gene_Name:

null

Chromosome_Number:

NCBI35:Chr2

Gene_Boundary:

88586988-88596883

Cytoband:

2p11.2

Target CTs:

hCT24465.2

Proteins of Target CTs (CPs):

hCP46639

Target RefSeqs:

XM_292958

Proteins of Target RefSeqs (NPs):

XP_292958.4

Target_MGC:

null

Target_GenBank_mRNA:

null

Target_GenBank_CDS:

null

Target_Emboss:

ENST00000303271

Target_EST:

null

Target_Other:

null

GO_Biological_Process:

GO:0006355:regulation of transcription, DNA-dependent

GO_Molecular_Function:

GO:0003700:transcription factor activity

GO_Cellular_Component:

GO:0005634:nucleus

EC:

null

Panther_Family_Name:

FORKHEAD PROTEIN/ FORKHEAD PROTEIN DOMAIN

Panther_Subfamily_Name:

null

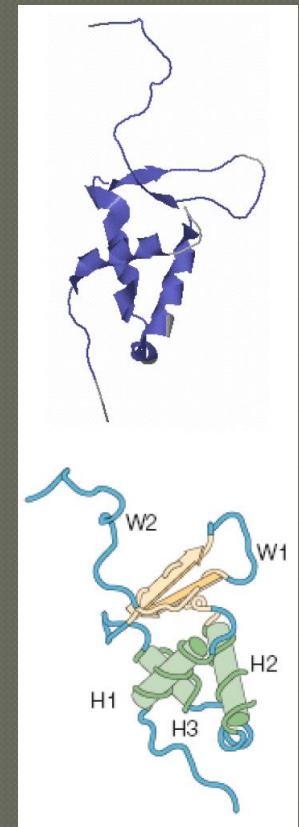
Panther_Function:

Other transcription factor; Nucleic acid binding|Transcription factor

Panther_Process:

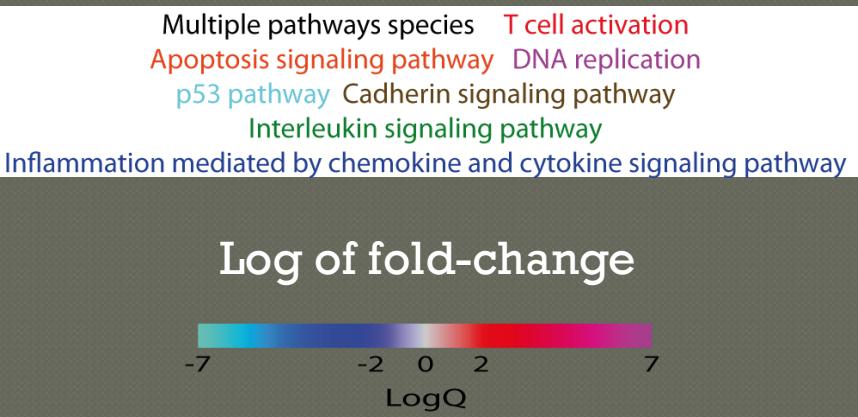
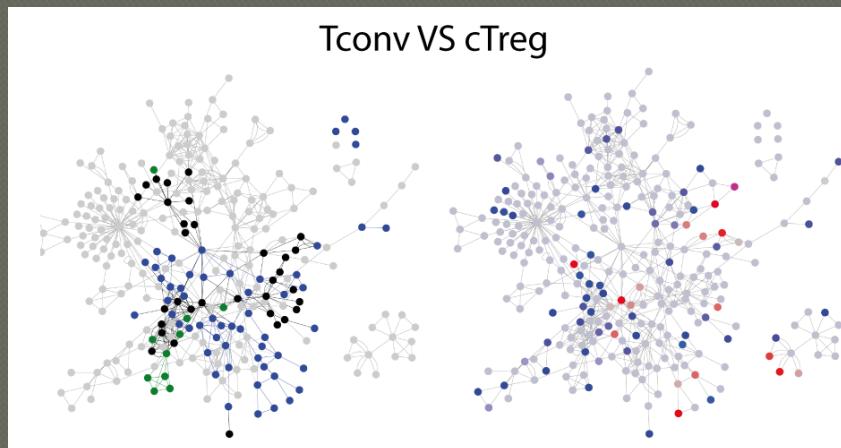
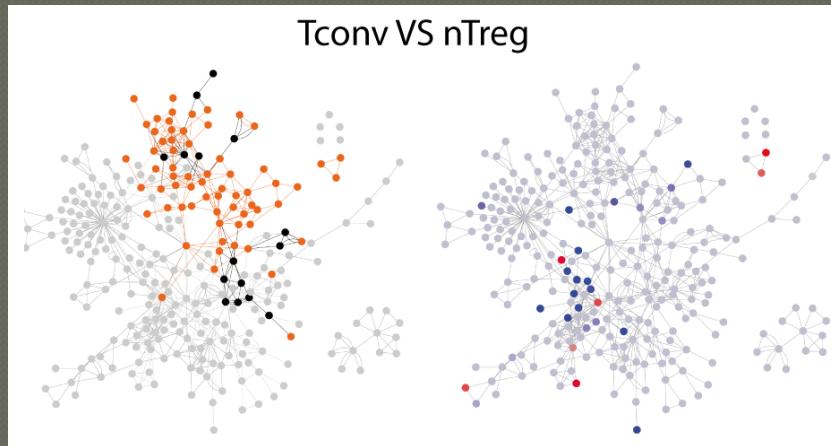
Anterior/posterior patterning; Developmental processes|Cell communication; Sensory perception|mRNA transcription

FOXLF



FOXP3

Search of the most representative pathways



Conclusion-perspective

- SVD-MDS: New MDS algorithm which is accurate and computationally efficient.

New dimensionality reduction methods for the representation of high dimensional "omics" data. *C. Becavin, A. Benecke. Expert Review of Molecular Diagnosis, will appear January 2011*

Molecular dynamics multidimensional scaling initialized by singular value decomposition leads to computationally efficient analysis of high dimensional data. *C. Becavin, N. Tchitchev, C. Mintsa-Eye, A. Lesne, A. Benecke submitted to Bioinformatics*

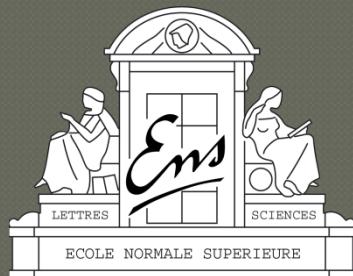
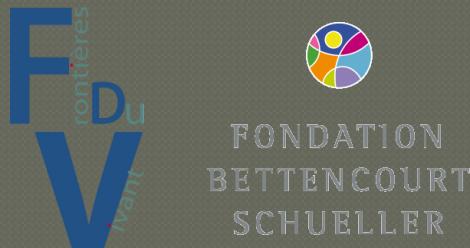
- Software developed for gene expression and Pathway structure integration
- Three different applications to biology

IgG autoantibody to Brain beta Tubulin III associated with cytokine Cluster-II Discriminate Cerebral Malaria in Central India. *Bansal D, Herbert F, Lim P, Deshpande P, Becavin C, Guiyedi V, de Maria I, Rousselle JC, Namane A, Jain R, Cazenave PA, Mishra GC, Ferlini C, Fesel C, Benecke A, Pied S. Plos One 4(12) (2009)*

HMGAl-dependent and independent 7SK RNA gene regulatory activity. *Sebastian Eilebrecht, Christophe Becavin, Helene Leger, Bernd-Joachim Benecke, and Arndt Benecke. RNA Biology, In press.*

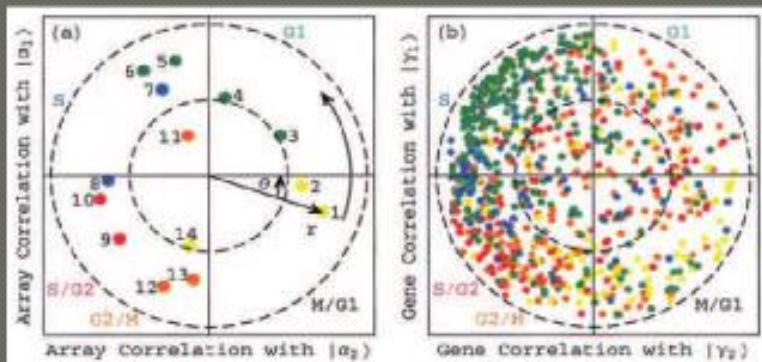
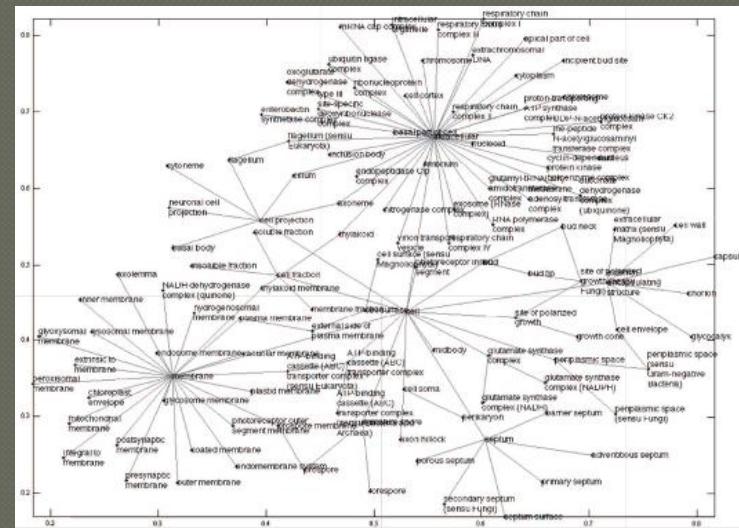
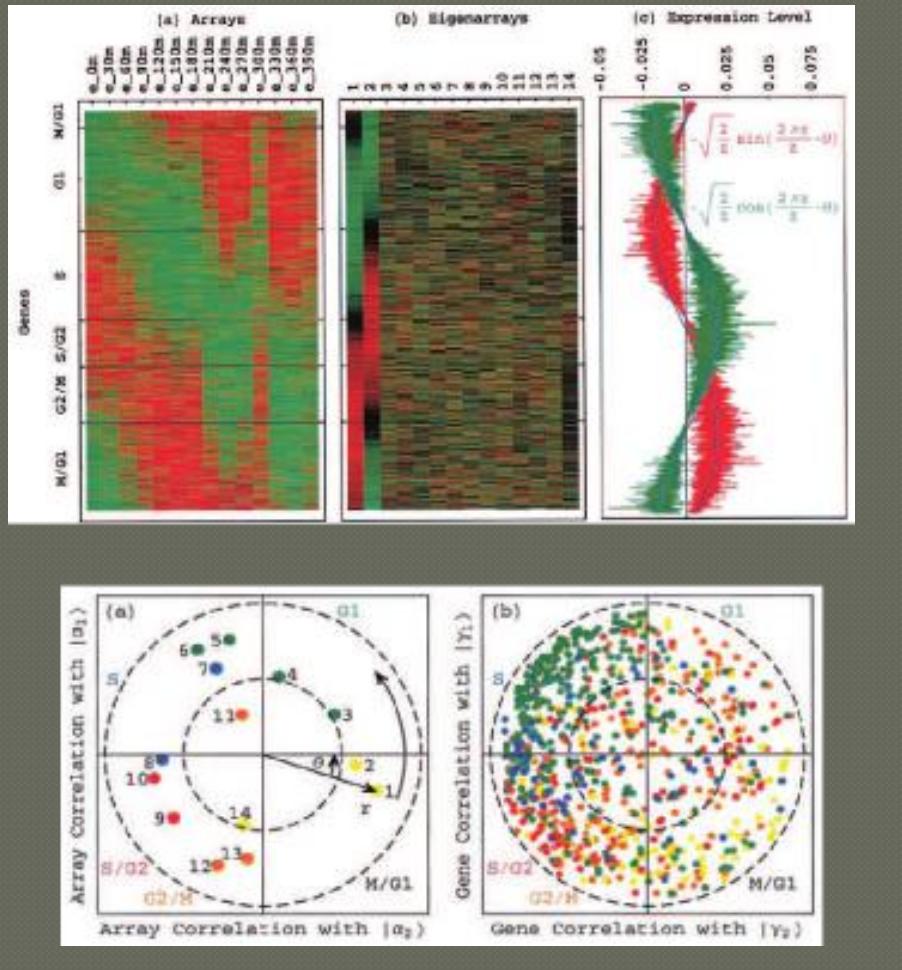
Publication of the results of the study on Treg subsets with Lars Rogge..

Remerciements

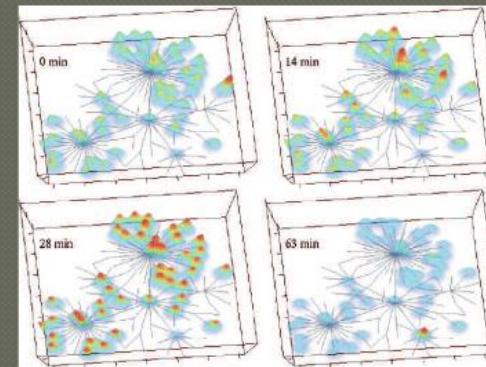


- All jury members: Alain Arneodo, Lars Rogge, Sylviane Pied, Jean Marc Victor, Andrei Zinovyev.
- My Thesis supervisors: Annick Lesne, Arndt Benecke.
- All my colleagues: Nicolas, Felipe, Brice, Guillaume, Hélène, Sebastian, François-Xavier.
- My collaborators: Sylvia Maiella and the members of Lars Rogge's and Sylviane Pied's laboratories.
- All the people from my doctoral school.
- Ma famille, mes amis.

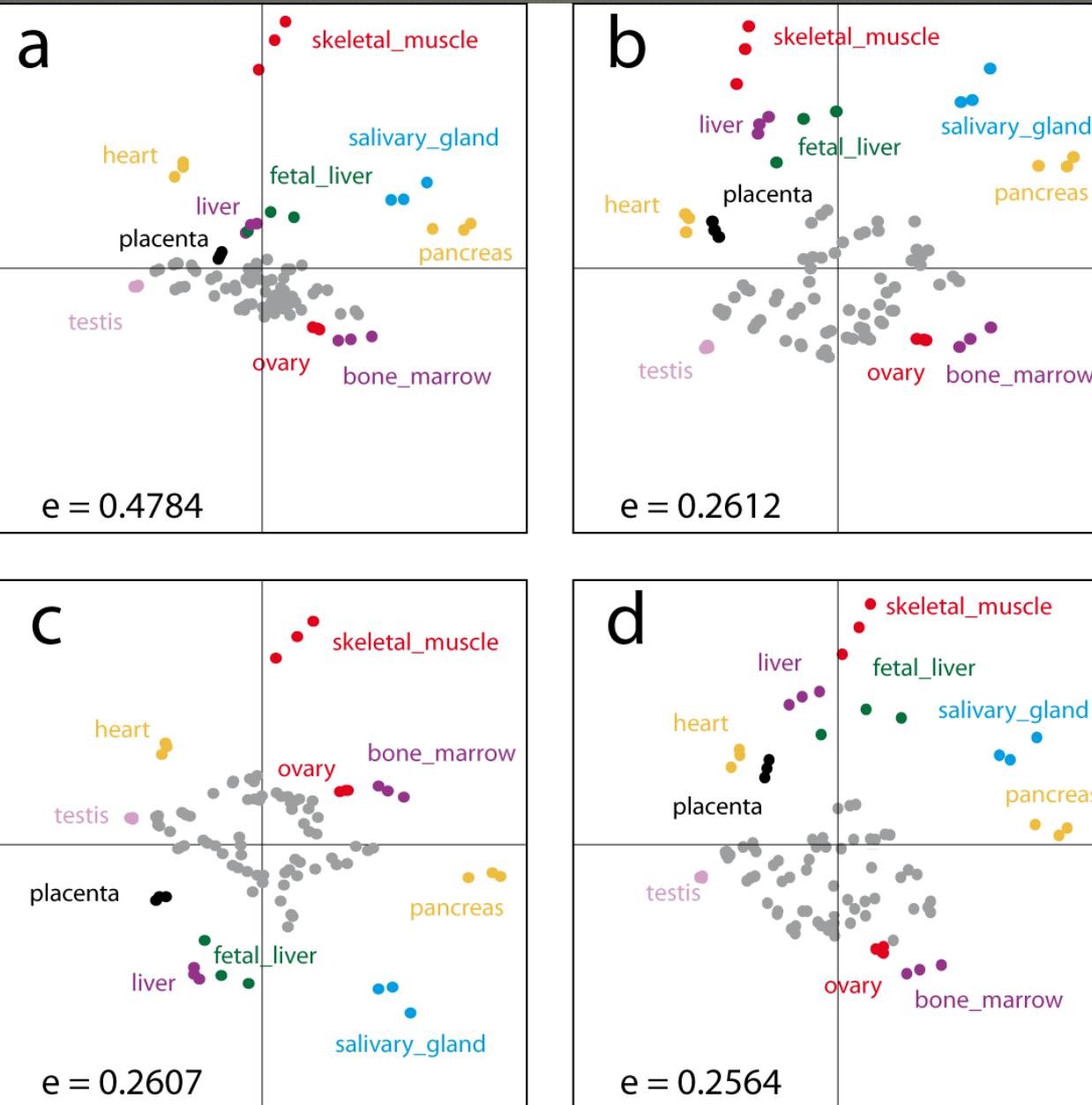
Example of applications of dimensionality reduction techniques



Alter et al., PNAS, 2000



Ebbels, Bioinformatics, 2006



General view on linear analysis and new developments

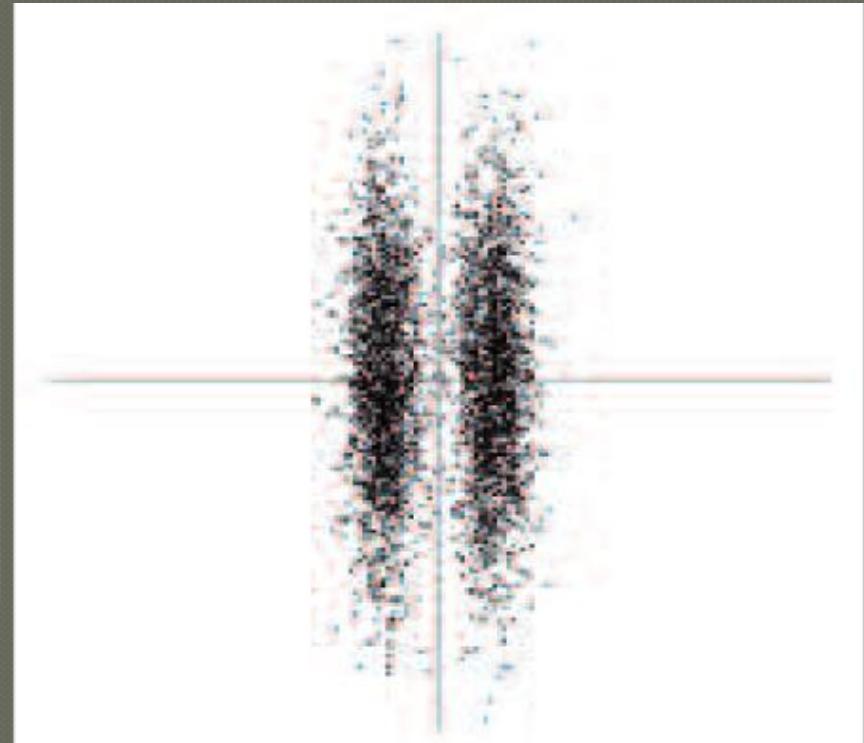
Orthogonality
(e.g.: PCA, Factor Analysis)



Independence
(i.e.: Independent Component Analysis)

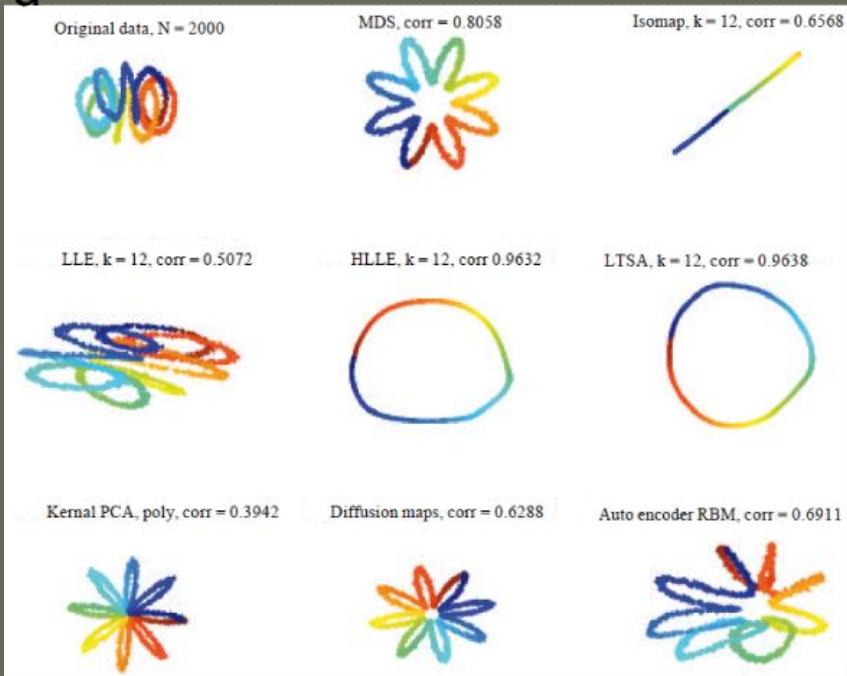


Decoster, 1998

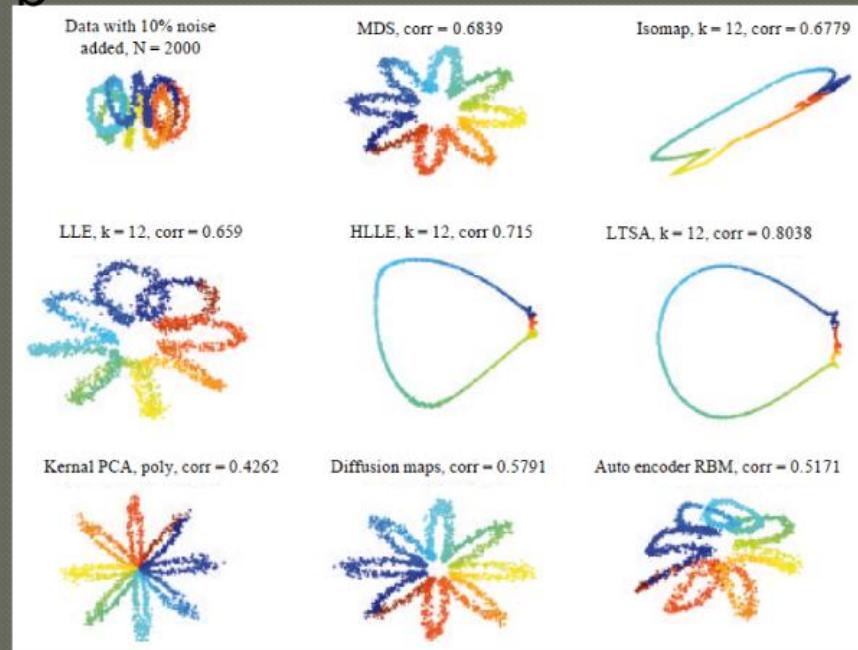


Effect of noise

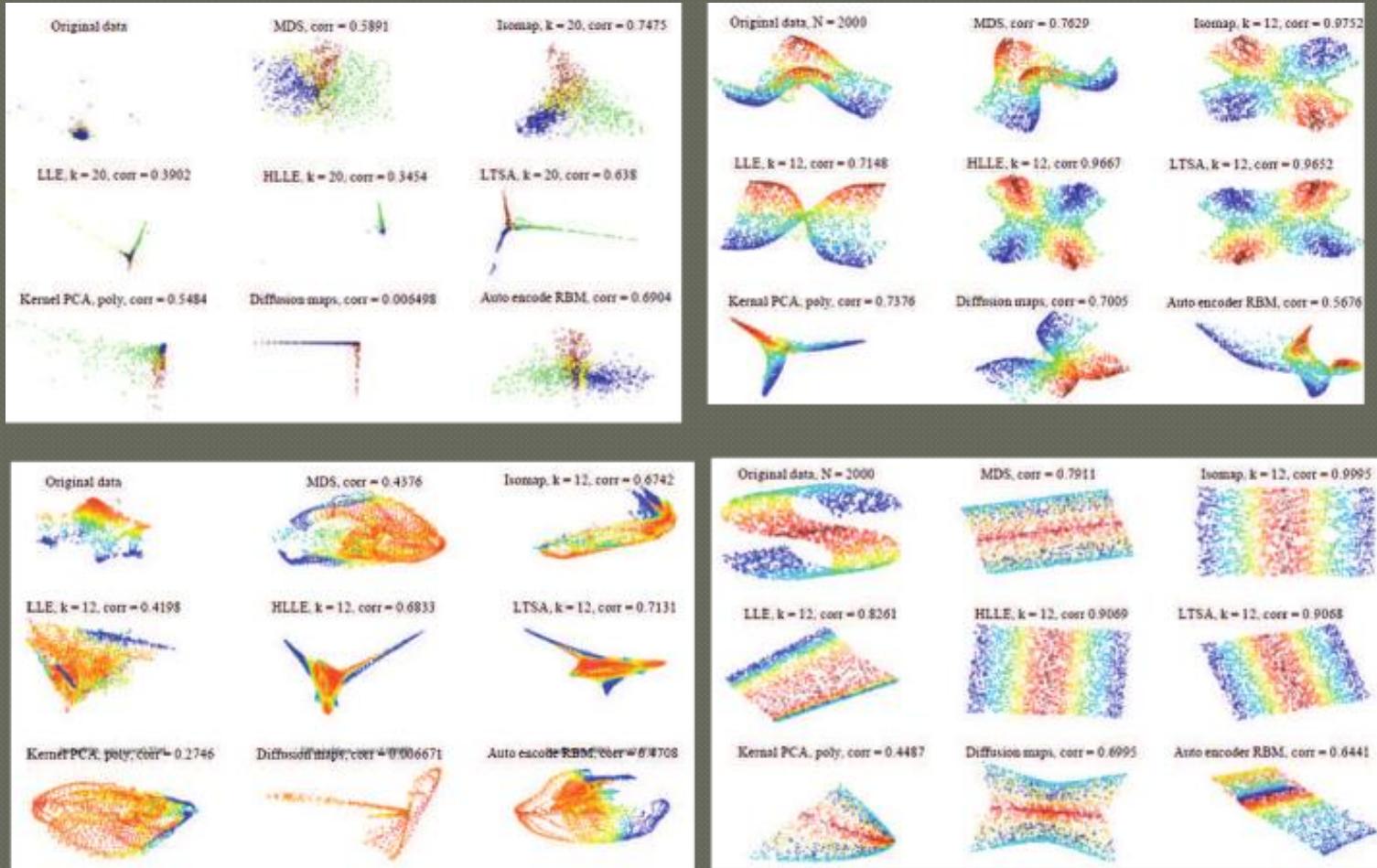
a



b



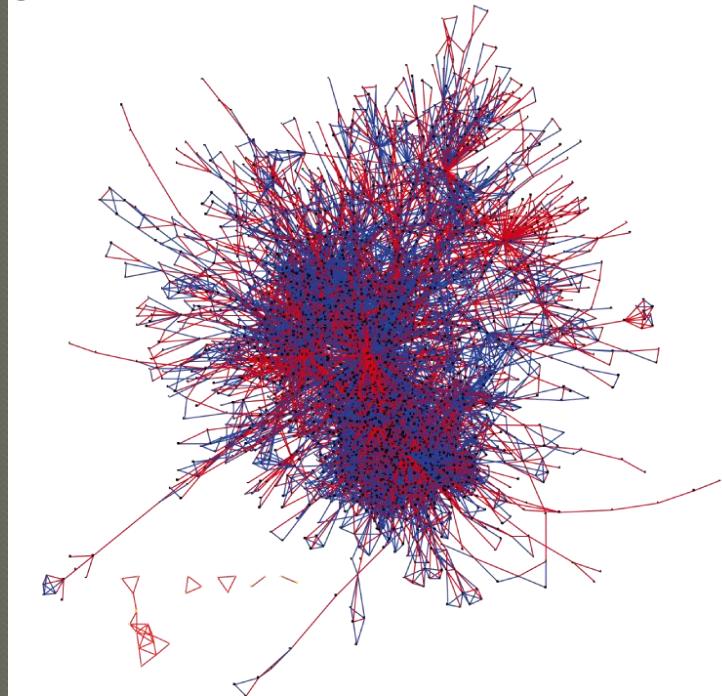
A great diversity of results given by each dimensionality reduction technique



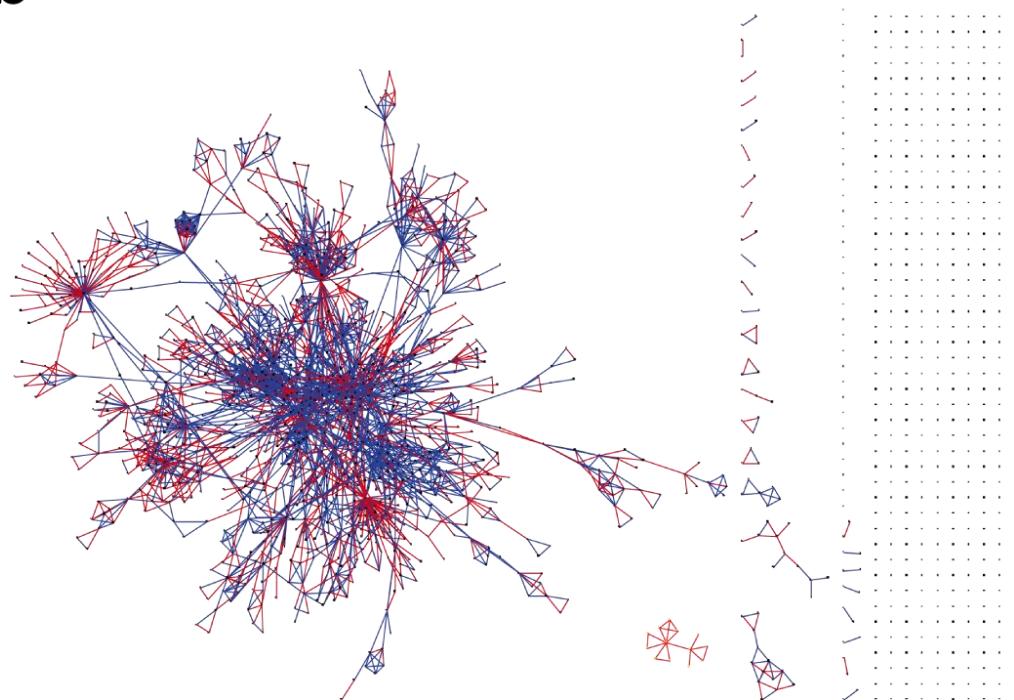
Tsai F., Journal of Artificial Intelligence, 2010

Soutenance de thèse de Christophe Bécavin 6 Décembre 2010

a

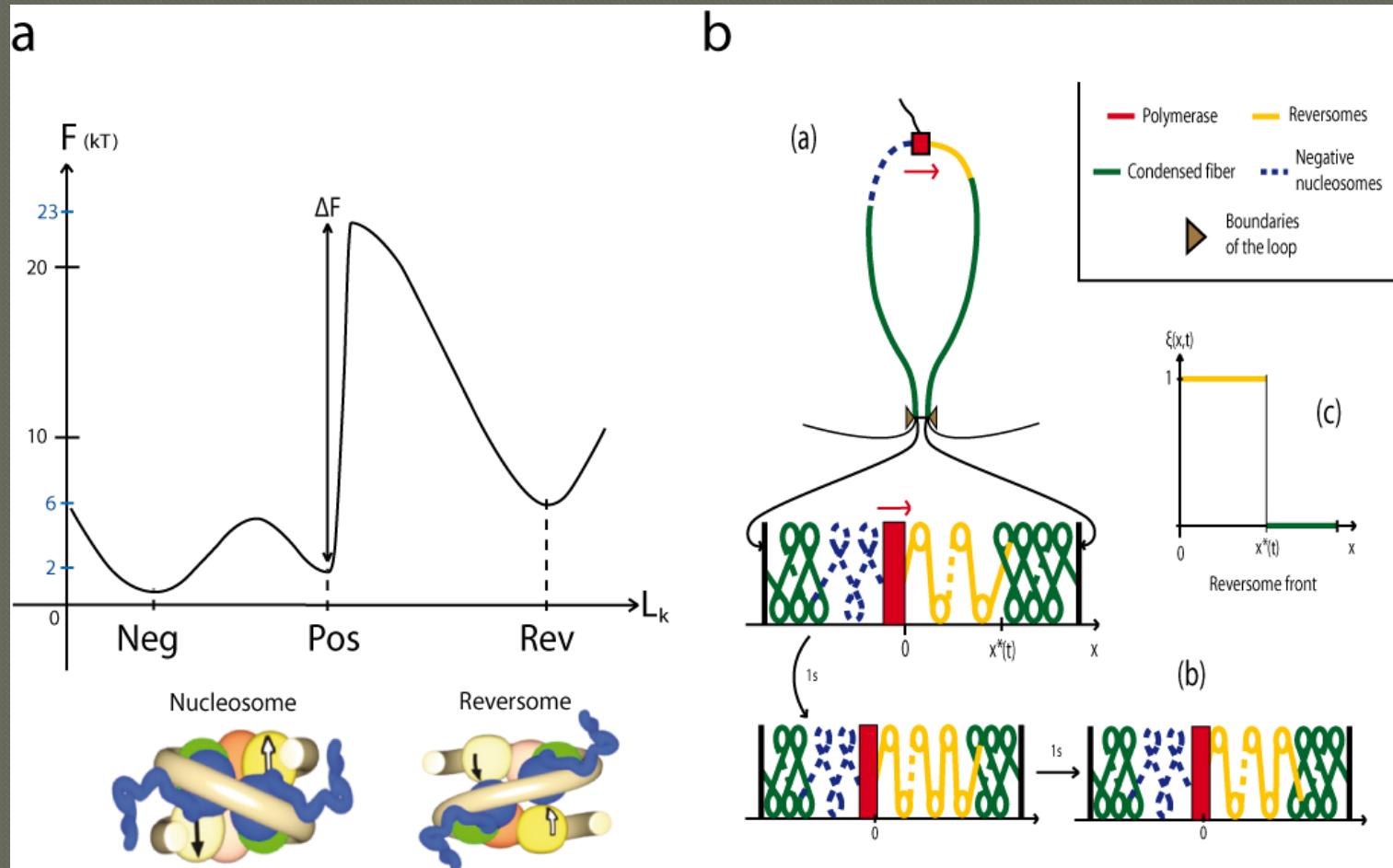


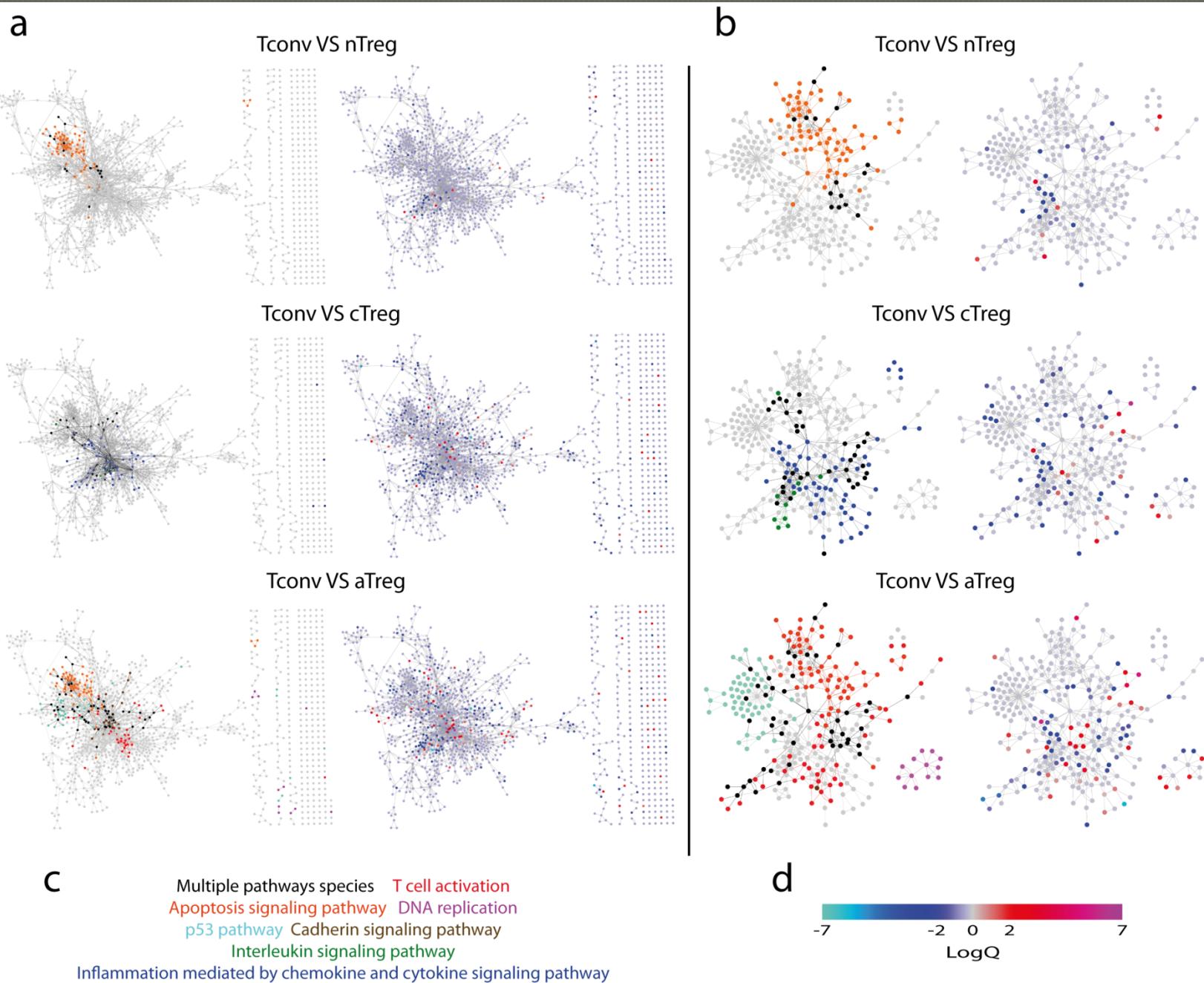
b

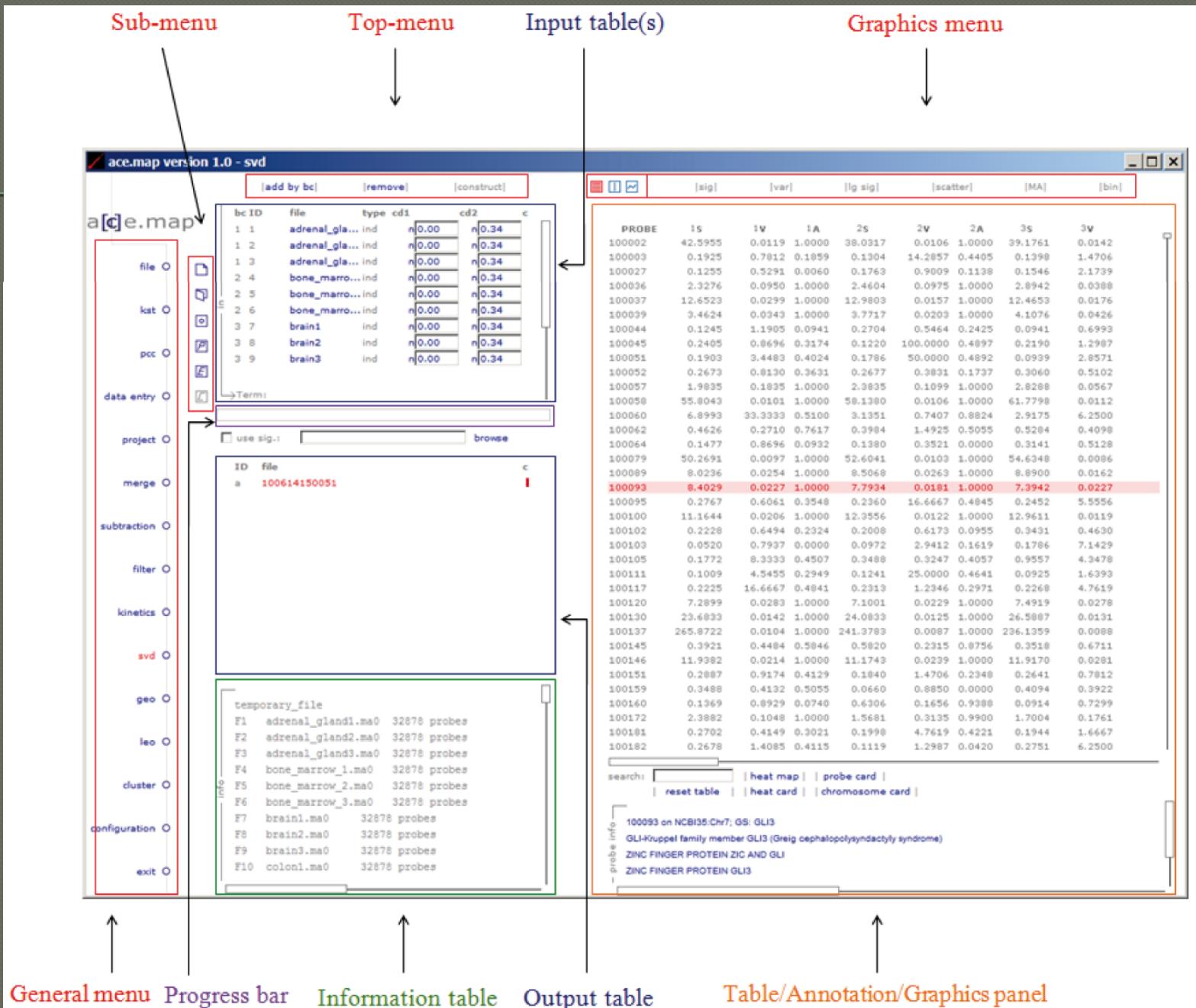


Chromatin during transcription

Bécavin et al., Biophysical Journal, 2009







Treg purification using FACS

