



Calcul de motifs sous contraintes pour la classification supervisée Constraint-based pattern mining for supervised classification

Dominique Joël Gay

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Encadrement : Nazha Selmaoui-Folcher et Jean-François Boulicaut

ERIM EA3791, PPME EA3325, Université de la Nouvelle-Calédonie LIRIS CNRS UMR5205, INSA-Lyon

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Preliminaries	Feature Construction	Applications	Conclusion & Perspectives
Context			

Supervised classification...

 \dots in labeled 0/1 samples

Recent developments : Pattern-based classification



Challenging problems

- Classification in noisy data
- Classification in multi-class imbalanced data

fitcare

Applications

Conclusion & Perspectives

Contributions to open problems

Classification when attributes are noisy

an application-independent pattern-based noise-tolerant feature construction method

Multi-class imbalanced classification

- a new framework dedicated to multi-class imbalanced data
- a parameter-free pattern-based method

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fitcare

Application

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Pattern-based classification : an example

Shall we organize "Les jeudis du centre ville" if it's rainy, with cooling temperature and without wind?

"Les jeudis du centre-ville"

		Attributes							Classes			
	r	(outloo	k	temperature		humidity		wii	ndy	jeudi	
		sunny	overcast	rainy	hot	mild	cool	high	normal	true	false	yes/no
	t_1	1	0	0	1	0	0	1	0	0	1	no
	t_2	1	0	0	1	0	0	1	0	1	0	no
	t_{14}	0	0	1	0	1	0	1	0	1	0	no
Ē.	t_8	1	0	0	0	1	0	1	0	0	1	no
ai	t_3	0	1	0	1	0	0	1	0	0	1	yes
ĿÈ	t_5	0	0	1	0	0	1	0	1	0	1	yes
s	t_7	0	1	0	0	0	1	0	1	1	0	yes
GC	t_9	1	0	0	0	0	1	0	1	0	1	yes
Ē	t_{10}	0	0	1	0	1	0	0	1	0	1	yes
0	t_{11}	1	0	0	0	1	0	0	1	1	0	yes
	t_{12}	0	1	0	0	1	0	1	0	1	0	yes
	t_{13}	0	1	0	1	0	0	0	1	0	1	yes
est	t_4	0	0	1	0	1	0	1	0	0	1	?
гĔ	t_6	0	0	1	0	0	1	0	1	1	0	?

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 Pattern mining and classification

Task

Mining a set of relevant class-characterizing patterns to predict class labels

Various types of pattern

■ Association rules (γ -frequency , confidence)_(Agrawal et al. SIGMOD'93) π : outlook_sunny and humidity_normal \rightarrow yes (freq : 2; conf : 1)

Emerging itemsets (γ -frequent ρ -EPs)_(Dong et al. KDD'99) humidity_high \rightarrow no (freq : 6; GR : 4)

inductive rules, ...

How to predict class labels for a new incoming object t?

Combining patterns supported by t to compute a score.

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 Noise handling : what has been done ?

Effects of noise

- Class-noise / Attribute-noise
- Low classification performance / low accuracy results

Noise handling

- Class-noise / Attribute-noise
- Noise detection / filtering / deletion / correction

$\hookrightarrow \mathsf{Undesirable} \text{ information loss}$

Our proposal

- Robust (noise-tolerant) feature construction based on frequent patterns
- without filtering, deleting or correcting any instance

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Our propo	sal		

Noise-Tolerant Feature Construction processus (NTFC)



A relevant pattern is

- frequent itemset
- class-characterizing
- noise-tolerant

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Why itemsets? Why frequent ones?

Intuition

"A frequent itemset could be interesting"



Frequent itemsets are preferable to single items

Pattern-based classification : key points

Let Y be an itemset characterizing class c_i .

Discrimination (w.r.t. an interestingness measure)

Let S be a set of itemsets characterizing class c_i .

- Coverage of training data (~ for a relevant data set representation)
- Minimality : $\nexists X$ characterizing c_i s.t. $X \subseteq Y$
- Redundancy : $Z \in S$ characterizing c_i s.t. $Y \subseteq Z$ is redundant
- $\blacksquare S$ is a concise set

Redundancy has been studied by means of the so-called condensed representations of frequent itemsets

Closure Équivalence Classes (CECs)

Bastide et al. SIGKDD Expl.'00 / Boulicaut et al. PKDD'00

Grouping itemsets having the same support/closure (CECs)

r	A	B	C	D	E	F	
t_1	1	1	1	1	1	0	
t_2	1	1	1	0	1	0	
t_3	0	1	1	0	1	0	
t_4	1	0	0	1	1	0	
t_5	0	1	1	0	0	1	
t_6	0	1	0	1	0	1	



$$\begin{split} \gamma &= 2\\ freq(AB) = freq(ABCE) = 2 \text{ (equivalent support)}\\ cl(AB) = cl(AC) = cl(ABC)\\ = cl(ABE) = cl(ACE)\\ = cl(ABCE) = ABCE \end{split}$$

Important

From a CEC, we may derive a strong association rule between a free itemset and each element of its closure

e.g., $AB \Rightarrow C$ and $AB \Rightarrow E$ are strong rules.

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 δ -Closure
 Equivalence
 Classes
 (δ -CECs)_{Boulicaut et al.}
 DMKD'03

From equivalence classes (δ -CECs) to relevant itemsets

r	A	B	C	D	c_1	c_2
t_1	1	1	1	1	1	0
t_2	1	1	1	0	1	0
t_3	0	1	1	0	1	0
t_4	1	0	0	1	1	0
t_5	0	1	1	1	0	1
t_6	0	0	1	1	0	1
t_7	1	0	1	1	0	1



$\gamma = 3; \delta = 1$
freq(A) = 4
freq(AC) = 3
freq(AD) = 3
$freq(Ac_1) = 3$

Important

From a δ -CEC, we may derive a δ -strong rule between a δ -free itemset and each element of its δ -closure.

e.g., $A \Rightarrow D$ and $A \Rightarrow c_1$ are δ -strong rules.

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We may derive one or more relevant (γ -frequent δ -free) itemsets from a δ -CEC.

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Fair properties of δ -CECs Crémilleux et al. ES'02

Let $\pi: X \to c$ be a δ -strong rule (X is a γ -frequent δ -free itemset).

High confidence

For small δ values, π is highly confident : $conf(\pi,r) \geq 1-\delta/\gamma$

Avoiding classification conflicts

If $\delta < \gamma/2$, we may avoid following conflicts :

- equal body conflict $(\pi': X \to c' \text{ does not exist})$
- included body conflict $(\pi': X \cup Y \to c' \text{ does not exist})$

Discriminative power of Emerging patterns Gay et al. PAKDD'08

If
$$\delta < \frac{\gamma \cdot |r \setminus r_{c_i}|}{\rho \cdot |r|}$$
 (r_{c_i} is the major class), X is a ρ -emerging pattern.

 \hookrightarrow Set $S_{\gamma,\delta}$ of relevant non-conflicting δ -strong characterization rules

Principle

From each itemset (rule body), a new descriptor is built.

- For $\pi: X \to c$, we have NewAttribute $(t, X) = \frac{|X \cap \text{Items}(t, X)|}{|X|}$
- Thus, NewAttribute $(t) \in \{0, \frac{1}{|X|}, \dots, \frac{|X|-1}{|X|}, 1\}$

Noise-Tolerant Feature Construction processus (NTFC)



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Minimum frequency : γ

- Extreme values ⇒ low interest
- Tuning? Still an open question...

A strategy for δ setting (given γ)



Increasing δ starting from 0 until stability point : δ_{opt}

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Experime	ntal protocol		

Protocol

- 1. UCI data sets
- 2. Uniform attribute-noise injection [0-50%] only in training data sets
- 3. Classification techniques : C4.5, NB and SVM

- 11 data sets : 55 noisy versions
- \blacksquare Two types of accuracy results : using δ_{opt} and using the best γ, δ combination



Summary

- + A solution to deal with attribute-noisy data : enhancing data set description with robust features
 - For imbalanced data sets a low γ threshold is needed It enforces low δ values. . .

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Effects of class disproportion

- Low per class accuracy results for minor class(es)
- Bias towards the majority class

Handling imbalanced problems

- Re-balance class distribution by over/under-sampling
- $\hookrightarrow \mathsf{Under}\text{-sampling} : \mathsf{Undesirable} \text{ information loss}$
- \hookrightarrow Over-sampling : Over-fitting, additional computational task

Pattern-based classification

Handling multi-class imbalanced problem with pattern-based techniques?

fitcare

Applications

Limits of existing frameworks

Examples of One-Versus-All (OVA) frameworks



- Frequency-confidence framework $Conf(Y \rightarrow c_2, r) = 40/45$ $GR(Y, r_{c_3}) = \frac{5/5}{40/95} > 2$ Y characterizing class c_2 or c_3 ?
- $\begin{array}{l} \hline {\bf EPs-based framework} \\ GR(X,r_{c_1}) = (7/10)/(2/90) > 31 \\ GR(X,r_{c_3}) = (2/5)/(7/95) > 5 \\ X \mbox{ characterizing class } c_1 \mbox{ or } c_3 \mbox{ ?} \end{array}$
- Positive correlation framework $FInt(X, c_1, r) = (100 \times 7)/(9 \times 10) > 1$ $FInt(X, c_3, r) = (100 \times 2)/(9 \times 5) > 1$ X characterizing class c_1 or c_3 ?

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 Other Limits of existing frameworks

Unsuitable global frequency threshold

Frameworks using a global frequency threshold are biased towards the majority class

Causes of limitations

- Class distribution is not taken into account
- Repartition of errors made by pattern into classes is not taken into account

Idea

One-Versus-Each framework :

- having a frequency threshold per class
- for each class, having an error threshold per each other class

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 OVE
 framework
 : OVE-characterizing rules
 (OVE-CRs)

OVE-characterizing rules

An OVE-characterizing rule for a class c_i is :

- frequent in r_{c_i} (relatively)
- infrequent (relatively) in every other class taken independently
- as general as possible

OVE-characterizing rule (formally)

An OVE-characterizing rule for r_{c_i} is :

$$freq_r(X, r_{c_i}) \ge \gamma_{i,i}$$

$$\forall j \neq i, freq_r(X, r_{c_j}) < \gamma_{i,j}$$

 $\exists \forall Y \subset X, \exists j \neq i \mid freq_r(Y, r_{c_j}) \geq \gamma_{i,j}$

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p^2 parameters for a *p*-class problem

$$Y = \begin{pmatrix} \gamma_{1,1} & \gamma_{1,2} & \dots & \gamma_{1,p} \\ \gamma_{2,1} & \gamma_{2,2} & \dots & \gamma_{2,p} \\ \vdots & \vdots & \ddots & \vdots \\ \gamma_{p,1} & \gamma_{p,2} & \dots & \gamma_{p,p} \end{pmatrix}$$

Consistency constraints on Γ lines / columns

$$\mathbb{C}_{line} \equiv \forall i \in \{1, \dots, n\}, \forall j \neq i, \gamma_{i,j} < \gamma_{i,i}$$

$$\mathbb{C}_{column} \equiv \forall i \in \{1, \dots, n\}, \forall j \neq i, \gamma_{j,i} < \gamma_{i,i}$$

Conflictless rule set

 $\mathbb{C}_{line} = true \land \mathbb{C}_{column} = true \Rightarrow \mathsf{rule} \text{ set } S_{\Gamma} \text{ of OVE-CRs is conflictless.}$

D.Gay

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fitcare ____

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OVE framework : fitcare

Our proposal

fitcare : an OVE parameter-free associative classification method

- Extraction of a set S_{Γ} of OVE-CRs w.r.t. Γ
- Elassification based on S_{Γ}
- Automatic parameter tuning (locally optimal consistent parameters Γ_{opt})

Preliminaries

Efficiently mining OVE-CRs and classification

Extraction

- Breadth-first search strategy
- anti-monotonicity properties of minimum frequency and minimal body constraints
- Per-class mining : $S = \bigcup_{i \in \{1,...,p\}} S_{c_i}$

Classification using per class frequencies

Given an object t, its likeliness score in c_i is :

$$l(t,c_i) = \sum_{\{c \in \mathcal{C}\}} \left(\sum_{\{\pi: X \to c \in S | X \subseteq Items(t,r)\}} freq_r(X, r_{c_i}) \right)$$

The class which maximizes l, indicates the class label for t.

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 fitcare : an optimization-based method

Principle : Hill-Climbing

Maximizing the quality of the classifier (rule set) by adjusting the most promising parameter of Γ with commit/roolback strategy.

Initialization

- Freaches the first stable state for Γ w.r.t. \mathbb{C}_{line} and \mathbb{C}_{column}
- indicates the maximal positive cover rate obtained.

Positive cover rate

The maximal positive cover rate obtained at initialization must be maintained during the optimization phase.

Confusion measure : Objective function to optimize

• Measuring the confusion made with class c_j when classifying objets of \mathcal{T}_{c_i} .

$$g(c_i, c_j) = \frac{\sum_{t \in \mathcal{I}_{c_i}} l(t, c_i)}{\sum_{t \in \mathcal{I}_{c_i}} l(t, c_j)}$$

When g increases, confusion weakens.

The greatest term of the denominator of g indicates the parameter to lower.

Accuracy comparisons (Win-Tie-Loss) with HARMONY and CPAR

Global accuracy fitcare vs HARMONY : 6-2-11 fitcare vs CPAR : 14-1-4

Per class accuracies for minor classes

fitcare vs HARMONY : 13-3-3 fitcare vs CPAR : 12-4-3

fitcare : performances

OVE fitcare >> OVA HARMONY, CPAR



Experiments : bias towards the majority class



Summary

OVE fitcare avoids the bias towards the majority class

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Soil erosion characterization with LRouet

Tasks

- Combinations of attributes that are suitable for erosion phenomenon?
- Semi-automatic mapping of erosion zones in a region.
- What about erosion hazard?





... in erosion data set



. . .

Results : analysis of OVE-CRs set

Soil erosion characterization

A set of DVE-CRs confirmed by domain experts. Now, observed phenomenons may be quantified (with frequency values) and qualified (with Growth rate values).

Combinations favourable to (non) appearance of erosion

exploitation and excavation mining zones \rightarrow eroded soil (0.0280; 0,0008; 31.6)

- Frequency in $r_{eroded} = 0.0280$
- Frequency in $r_{non-eroded} = 0.0008$
- Growth rate = 31.6

dense forest \rightarrow non-eroded soil (0.0114; 0.0902; 7.9)

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Results :	prediction		

Semi-automatic mapping



Confusion matrix

Dumbea	Real classes			Ouenghi	Real	classes	
Predictions	non-eroded	eroded		Predictions	non-eroded	eroded	
non-eroded	112827	743		non-eroded	137016	835	
eroded	14437	926 $\simeq 55\%$		eroded	31173	$3194 \simeq 79\%$	
Global accuracy : fitcare \simeq C4.5, NB, HARMONY							
Accuracy for minor class : fitcare \gg C4.5, NB, HARMONY							

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Results	: erosion hazard		

Erosion hazard estimation

Estimation of the probability of erosion occurrence using per class frequencies normalization (with fitcare)



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Summary

Contributions to open questions : pattern-based classification in difficult contexts

Noisy data

- A generic robust feature construction method
- New NTFC features ≫_{better} original features

Noisy data : perspectives

What about class-noise handling?

fitcare : bilan

- A new framework and method dedicated to multi-class imbalanced problem
- High per class accuracies for minor classes
- Solving the problem of bias towards the majority class

fitcare : perspectives

- Exploring the field of optimization algorithms, local optimum search . . .
- Cost-sensitive fitcare?

Application to erosion data set

- Quantification and qualification of erosion phenomenon
- Semi-Automatic mapping of erosion zone in a region
- Erosion hazard assessment

Applications : perspectives

- \blacksquare Generic methodological contributions \Rightarrow Various applications
- From pixel data to spatial data and spatial pattern mining

Preliminaries	Feature Construction	Applications	Conclusion & Perspectives
That's a	ll folks!		

Question time

Thank you for your attention.