

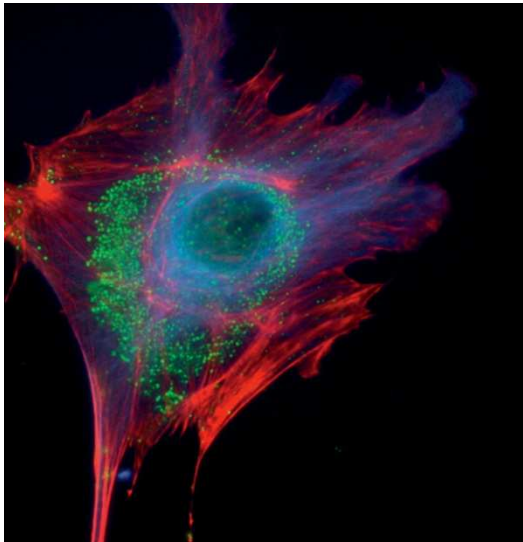
Un microlaboratoire électrophorétique pour l'étude du  
couplage entre transport et cinétique chimique :  
application à la réaction d'hybridation d'oligonucléotides

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9 juillet 2007

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# Goal



1 cell =  $10^5$  chemical species

Large concentration range

- miRNA  $10$ - $10^4$  copies

D.P. Bartel *Cell* 2004

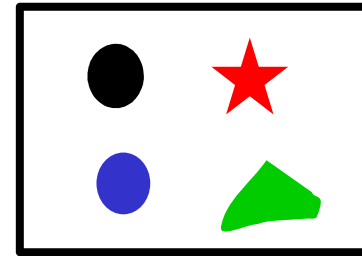
- ATP  $10^7$  (1 mM)

**Need of powerful tools for Analytical Chemistry**

selective and fast

# Selectivity in analytical chemistry

Issue: select a species inside a mixture



2 strategies:

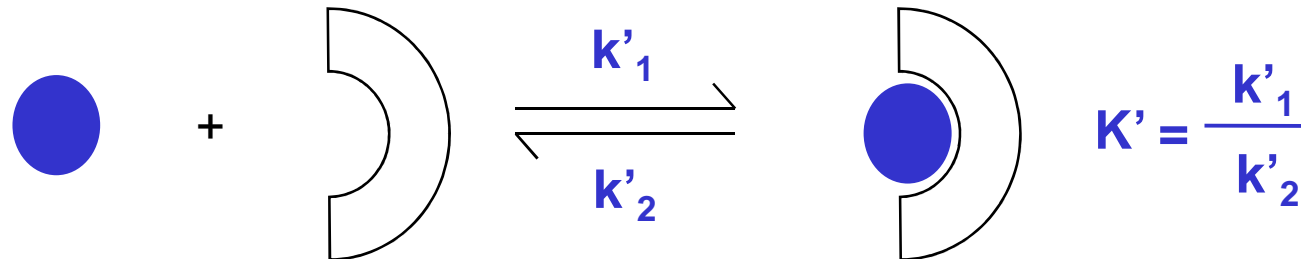
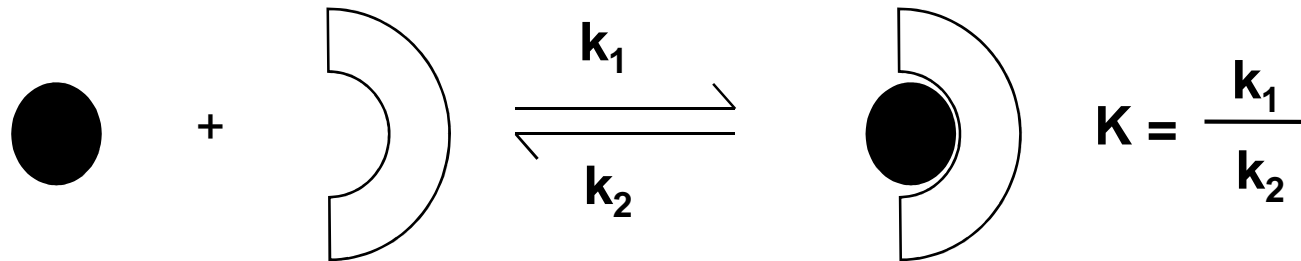
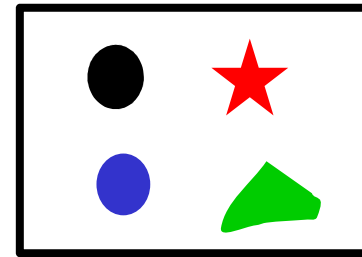
Improve existing strategies

- Spectroscopy
- Affinity separations (K)

Develop new selection strategies: reactivity ( $k_1$ ,  $k_2$ )

# Selecting on kinetics

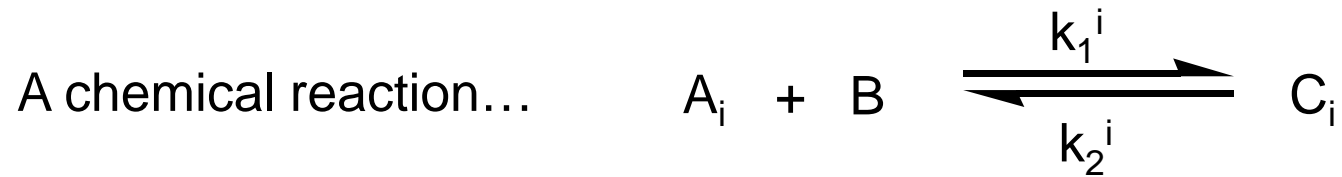
chemical species  $\longrightarrow$  reacting object



Thermodynamics:  $K$

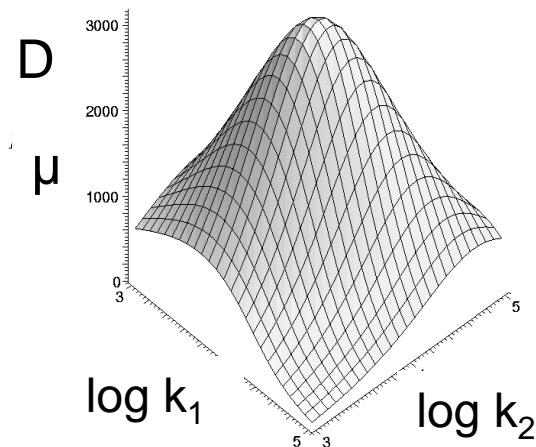
Kinetics:  $k_1, k_2$

# Resonance



... and a periodic excitation...  $u(t) = u \cos(\omega t)$

... yield:



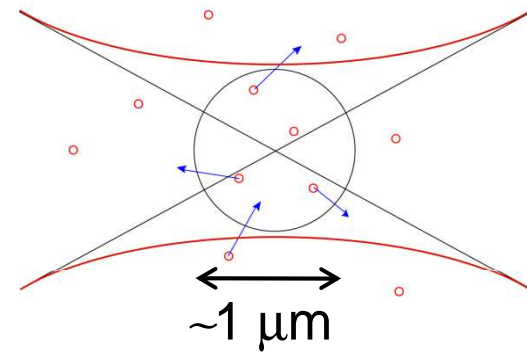
**Response always maximum**

**Focus on diffusion (D)**

# Quantifying diffusion

Two main approaches:

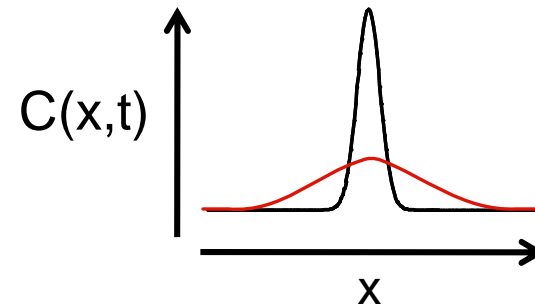
1. Fluctuations near equilibrium: FCS



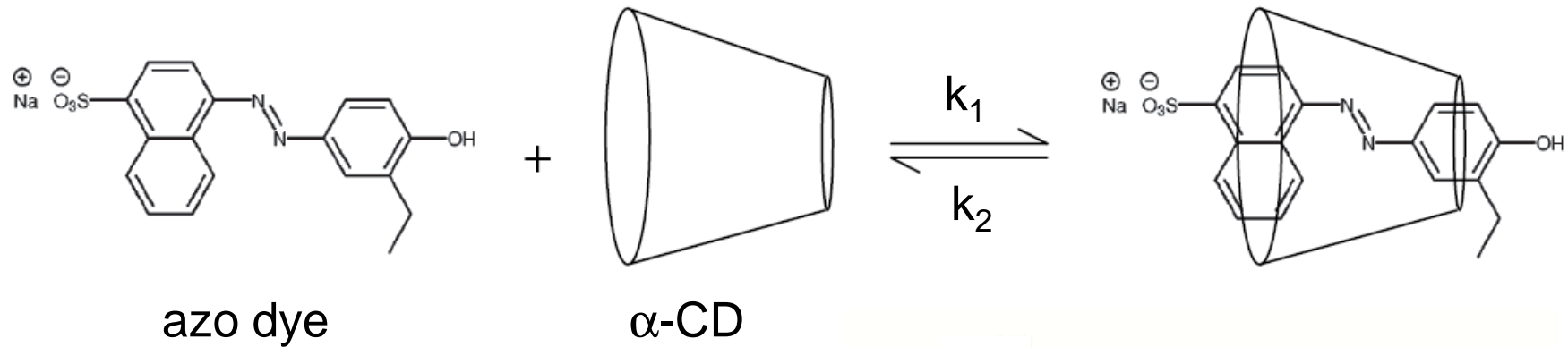
2. Relaxation of out-of-equilibrium concentration profile

- FRAP D. Axelrod *et al*, *Biophys. J.*, 1976

- Injection



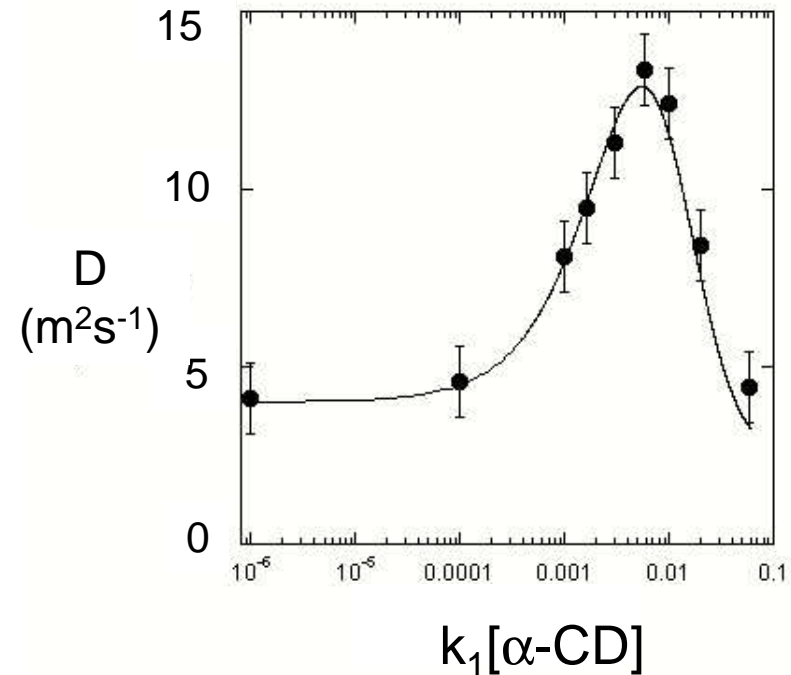
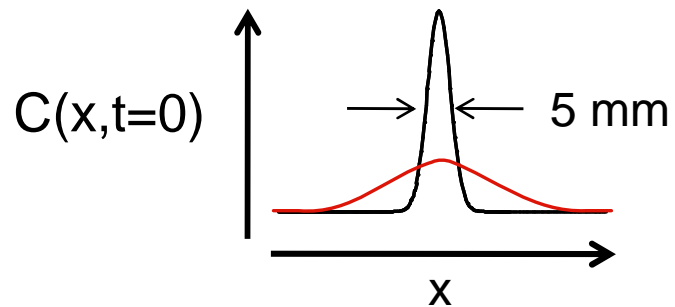
# Controlling diffusion: electrodiffusion



D maximum when:

$$k_1[\alpha\text{-CD}] = k_2 = \frac{\omega}{2}$$

Initial condition:



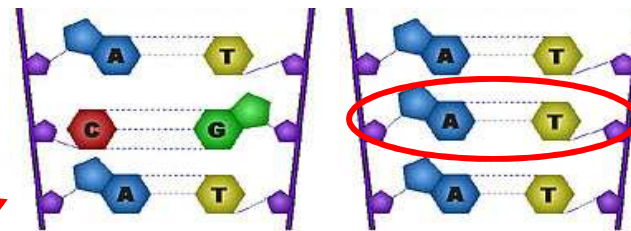
# Outline

1. DNA hybridization reaction
2. A functional microlaboratory
3. A powerful tool to analyze dynamics



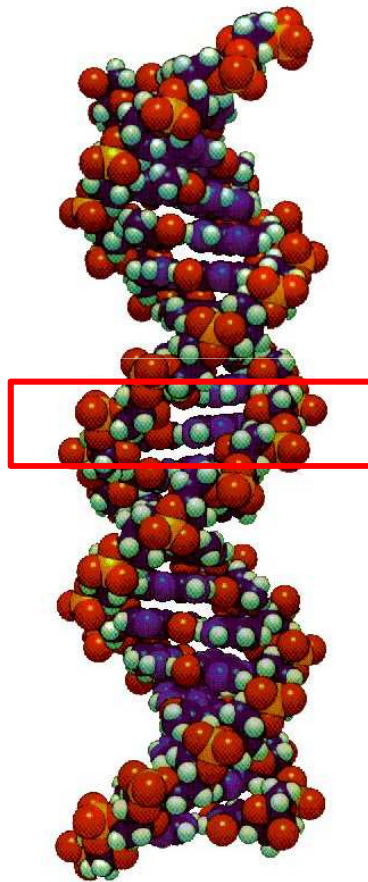
# DNA point mutations (SNP)

What is a point mutation?



wild type

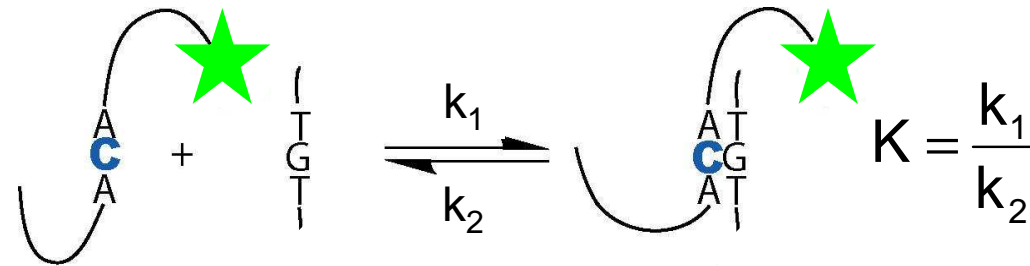
mutated



Why detecting them?

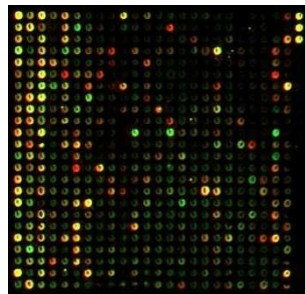
- Related to important diseases
- Identification of bacterial strains
- $10^6$  SNPs in genome

# SNP detection



DNA chips rely on thermodynamics

Slow (10-1h) Liu, Quake, *Angew.Chem.*, 2006  
Weak observable (intensity)

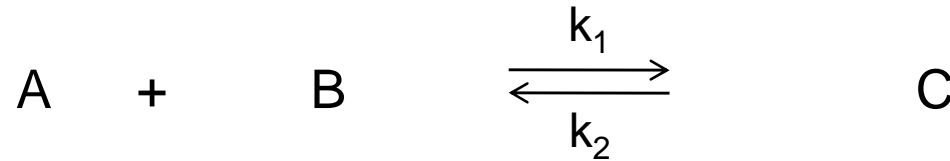


Electrodifusion rely on kinetics

Fast (seconds)  
Reliable observable (distance)



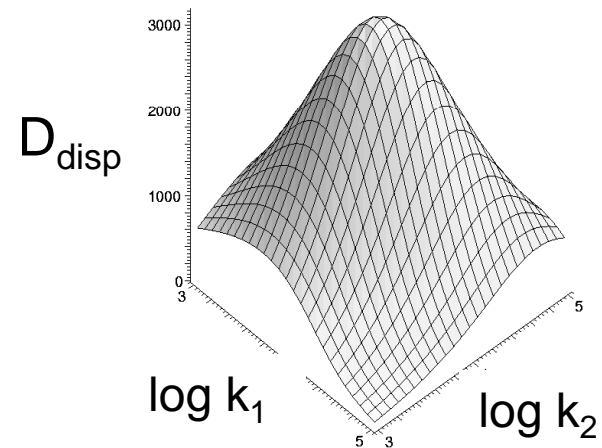
# Dynamics of electrodiffusion



Important parameters:

Reaction dynamics:  $k_1, k_2$

Transport dynamics:  $\mu_A, \mu_C, D_A, D_C$



$$D_{disp} = E^2 (\mu_A - \mu_C)^2 \frac{k_1 k_2}{(k_1 + k_2)^3} \left[ \frac{1}{2 \left( 1 + \frac{\omega^2}{(k_1 + k_2)^2} \right)} \right]$$

# Dynamics of DNA oligonucleotides

1. Easy predicted kinetics

}	K can be calculated	J. SantaLucia Jr. <i>PNAS</i> <b>1998</b>
	$k_1$ set by salt	A.P. Williams <i>et al Biochemistry</i> <b>1991</b>
	$k_2 = k_1 / K$	

2. Problem:  $k_1$  independent of sequence (nucleation mechanism)  
D.Pörschke, M. Eigen *J. Mol. Biol* **1971**

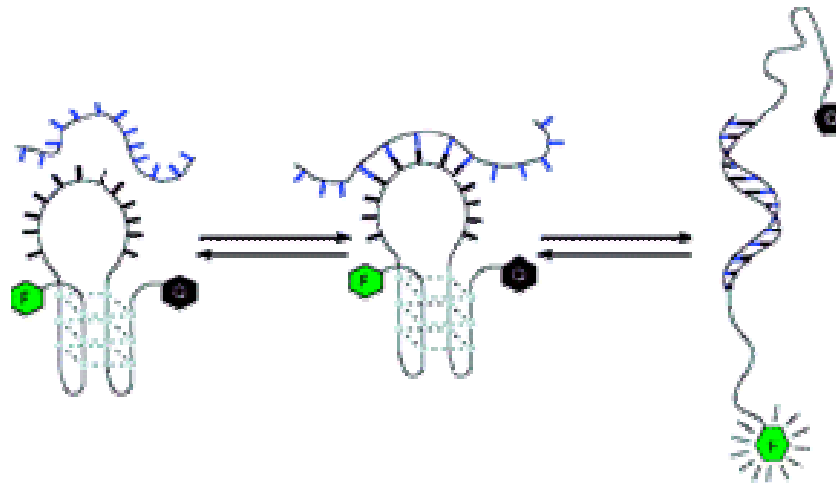
3. Problem: Electrophoretic mobility independent of length (free draining)  
N. Stellwagen *et al Biochemistry* **2003**

4. Easy to have  $D_A \neq D_C$  (changing length)

# Results: control of kinetics

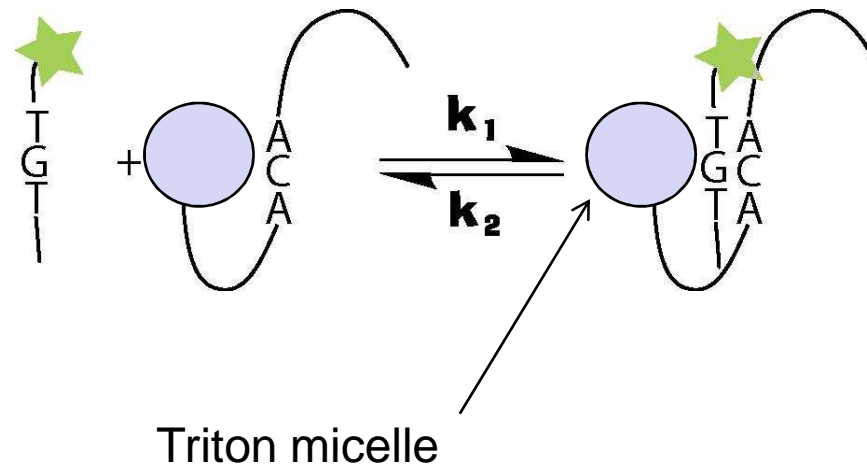
1. An oligonucleotide bank with widespread kinetics  $\left\{ \begin{array}{l} k_1 (10^4 - 10^6 \text{ M}^{-1} \text{ s}^{-1}) \\ k_2 (10^2 - 10^4 \text{ s}^{-1}) \end{array} \right.$

2.  $k_1$  might depend on sequence but slow dynamics



## Results: mobility reduction

3. Electrophoretic mobility can be tuned  $\mu_A \neq \mu_C$



Very good dynamic model:  $k_1, k_2, D$  and  $\mu$  can be modulated

# Experimental constraints

$$k_2 \sim 1 \text{ s}^{-1}$$

shorter times



$$x \sim \sqrt{\frac{D}{k_2}} \sim 100 \mu\text{m}$$

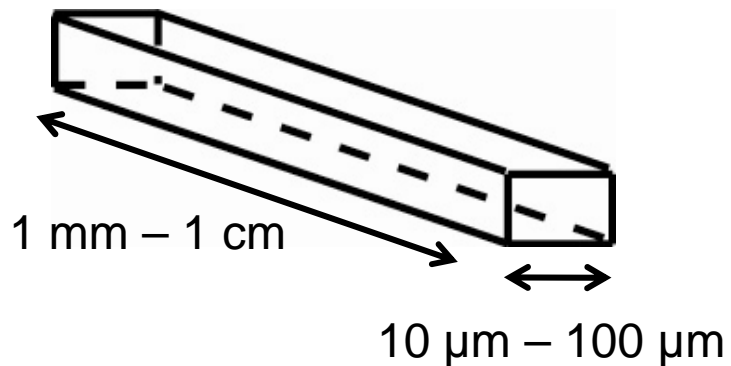
shorter lengths



better heat dissipation

$$E = 10^4 - 10^5 \text{ V m}^{-1}$$

**Need of microfluidics**



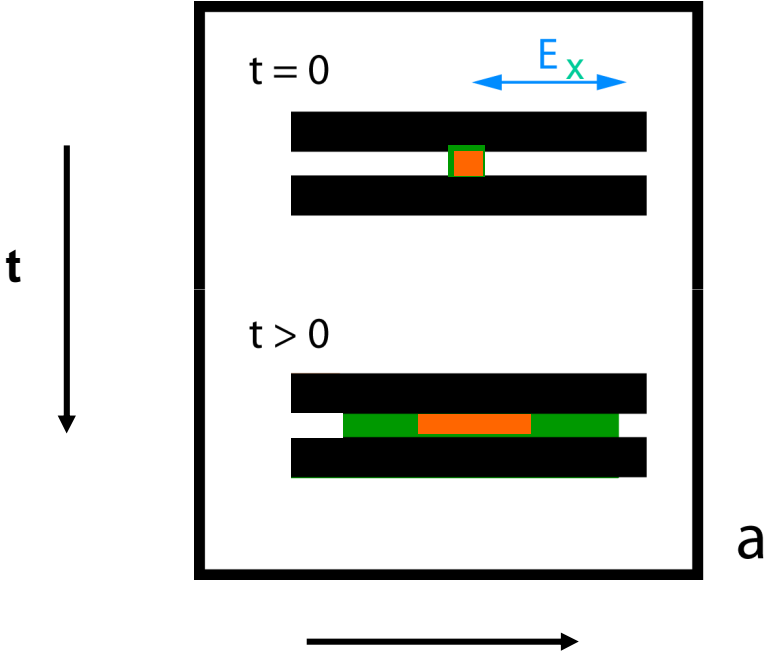
# Outline

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2. A functional microlaboratory
3. A powerful tool to analyze dynamics



# Initial condition: 1D

non-stationary

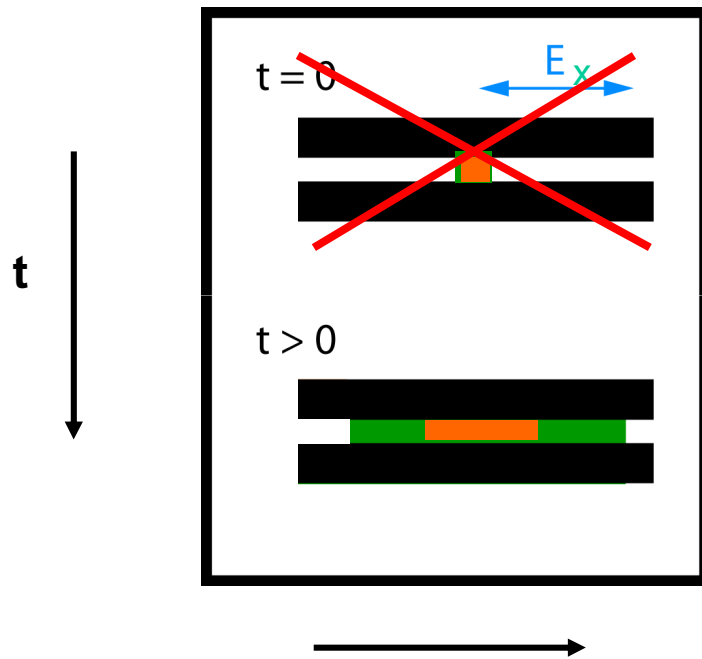


- resonant
- non-resonant

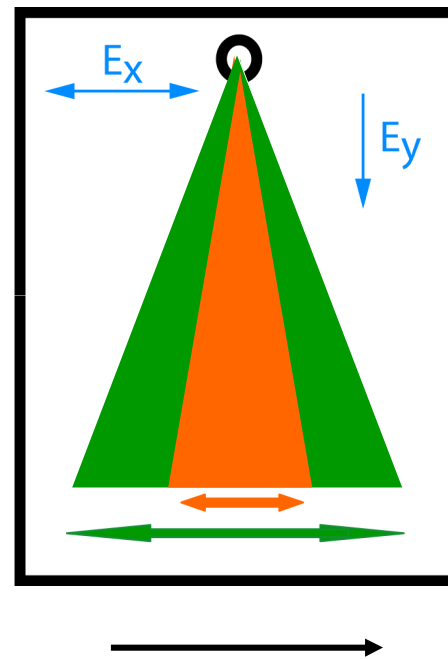
# Initial condition: 2D

non-stationary

stationary



a

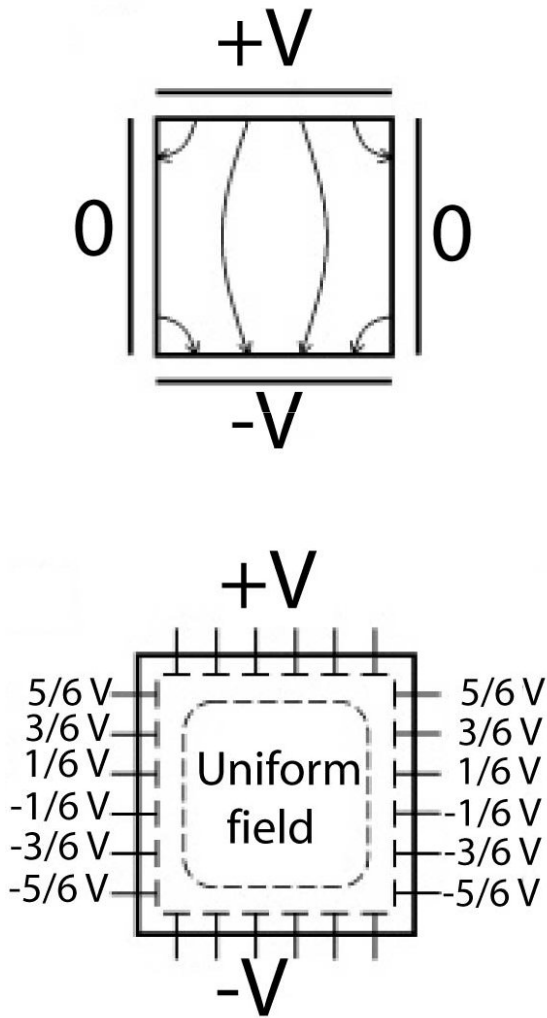


b

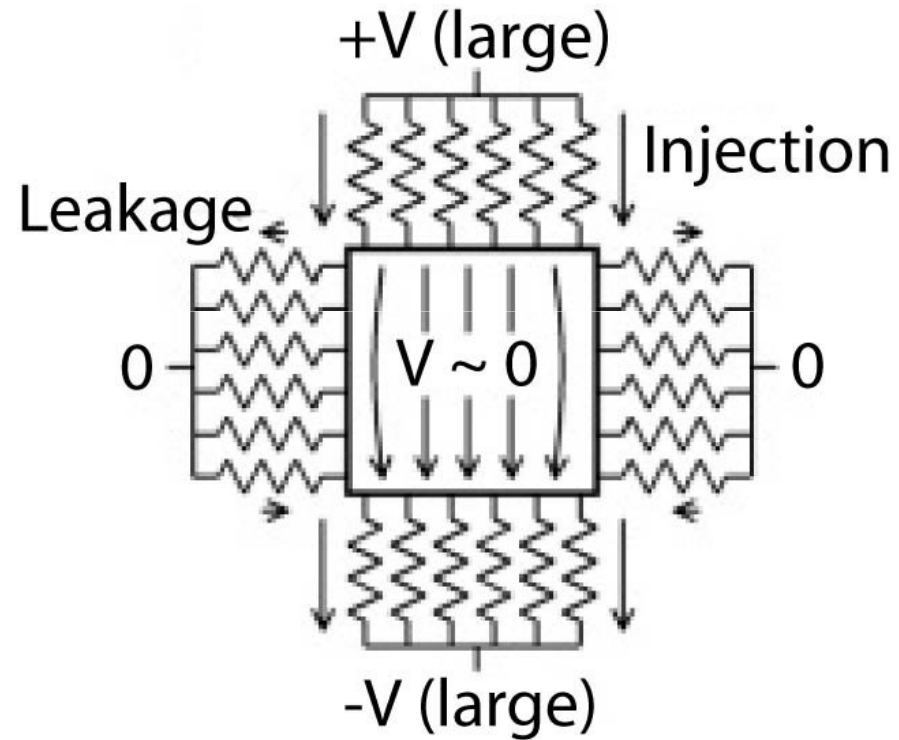
- resonant
- non-resonant

**Uniform velocity?**

# Cross-field generation

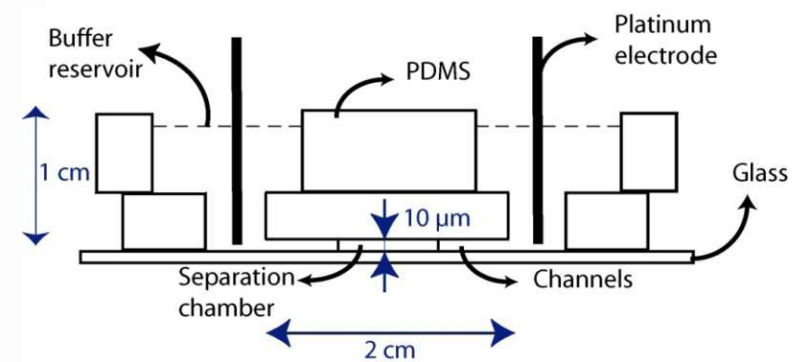
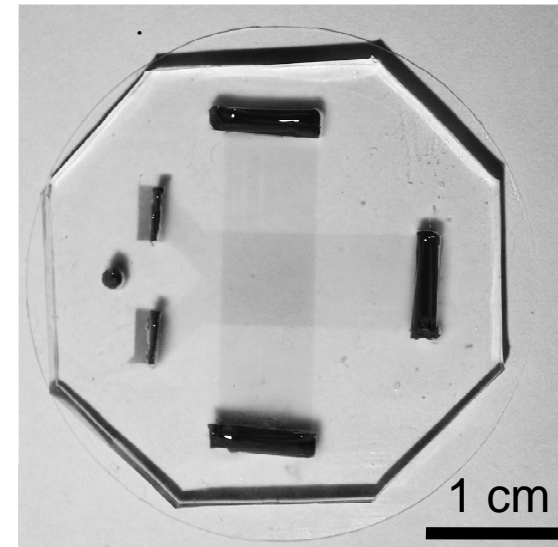
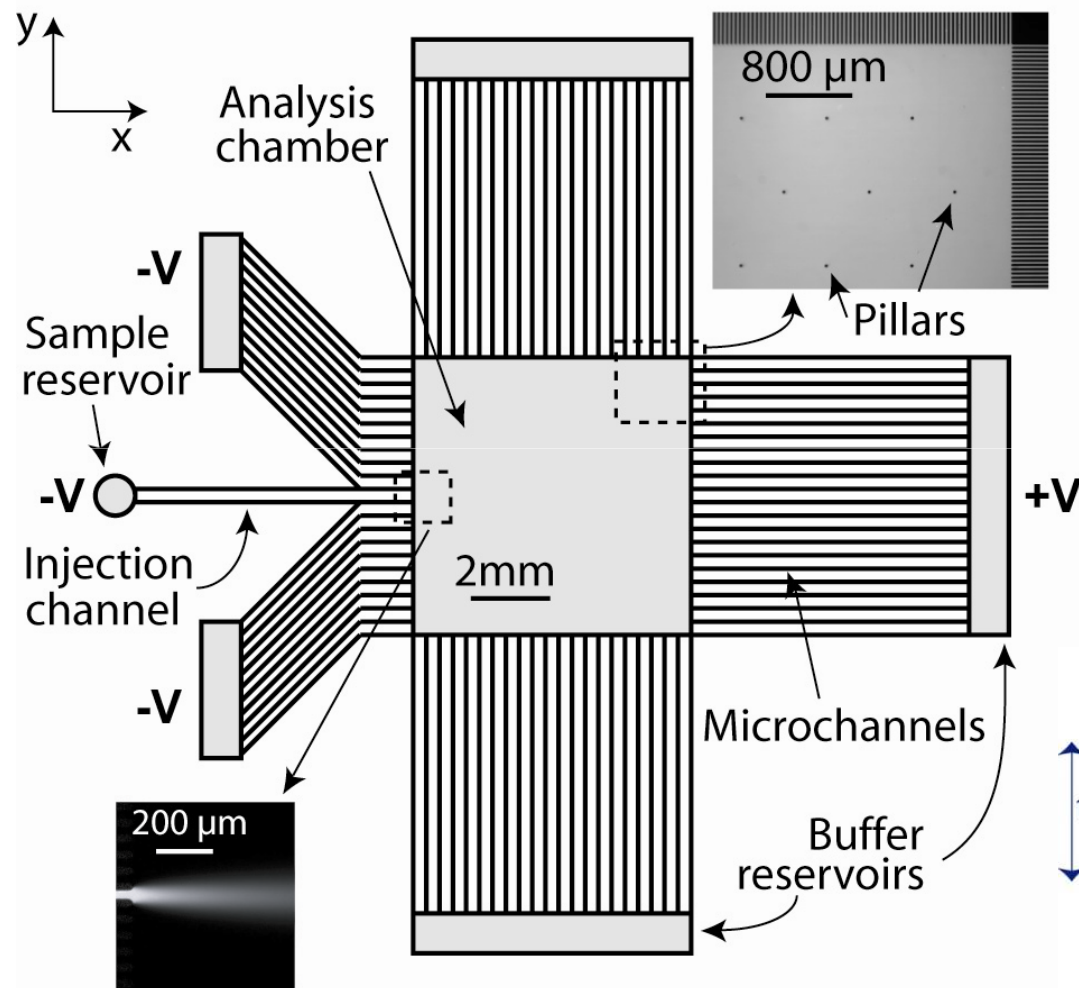


D. C. Schwartz C.R. Cantor *Cell* **1984**



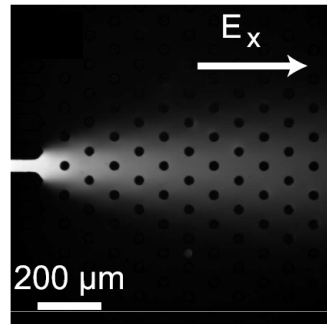
L. R. Huang et al. *Int. Elect. Dev. Meet. Tech. Digest*, **2001**

# A versatile 2D electrophoretic device



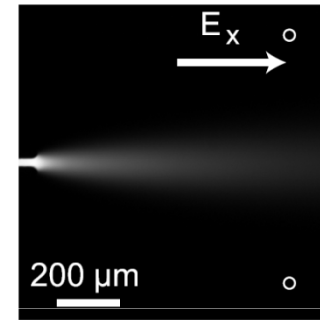
## Solved issues

Reduction of pillar density



$$D = 150 \pm 10 \mu\text{m}^2\text{s}^{-1}$$

Pillars induce dispersion

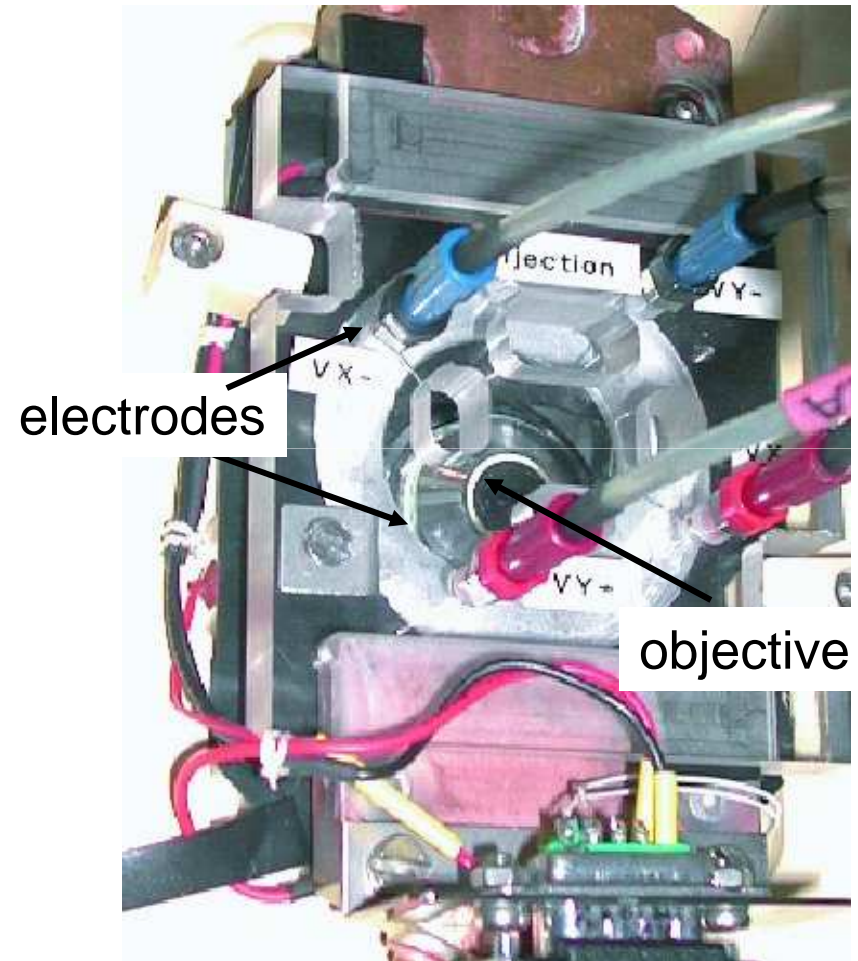
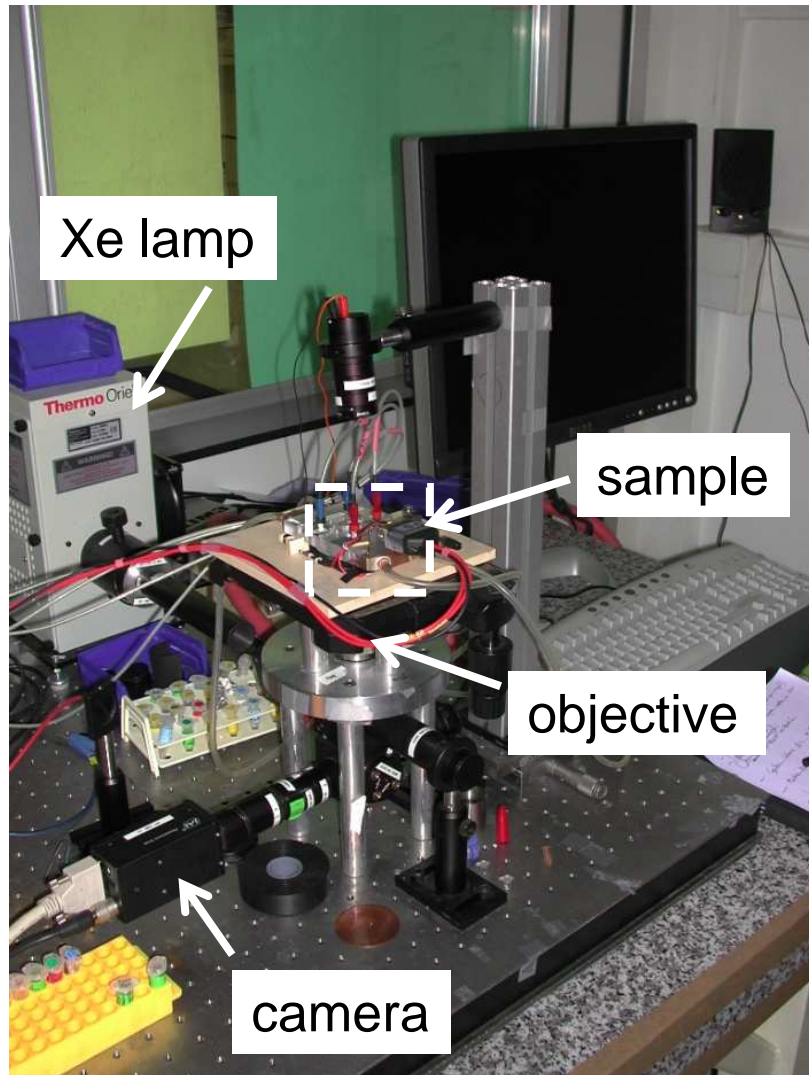


$$D = 100 \pm 10 \mu\text{m}^2\text{s}^{-1}$$

Filling protocol avoid collapsing:

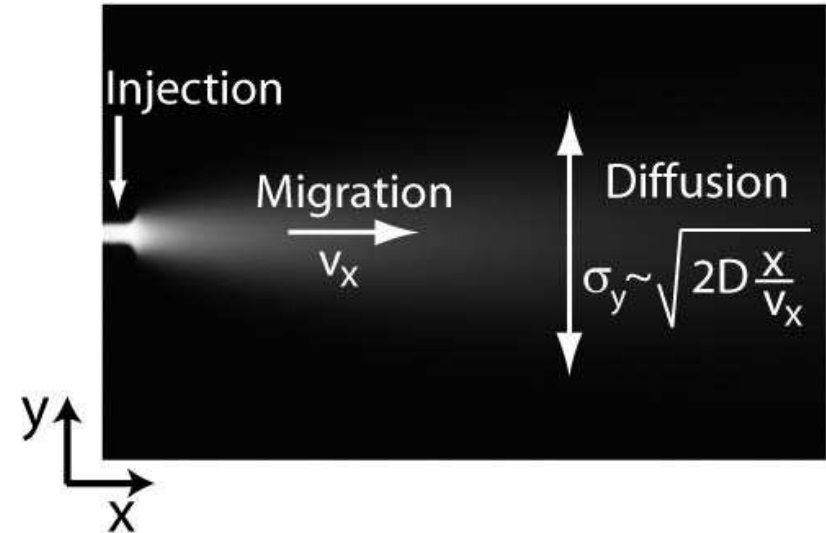
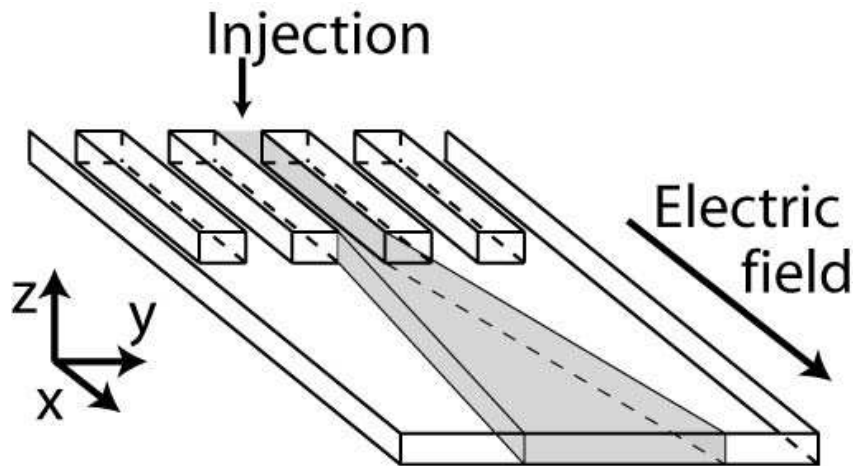
1. Plasma treatment
2. Chip heating for capillary force reduction
3. Vacuum pumping

# Observation set-up



**Chip mounted on a thermostat**

# Stationary electrophoretic device



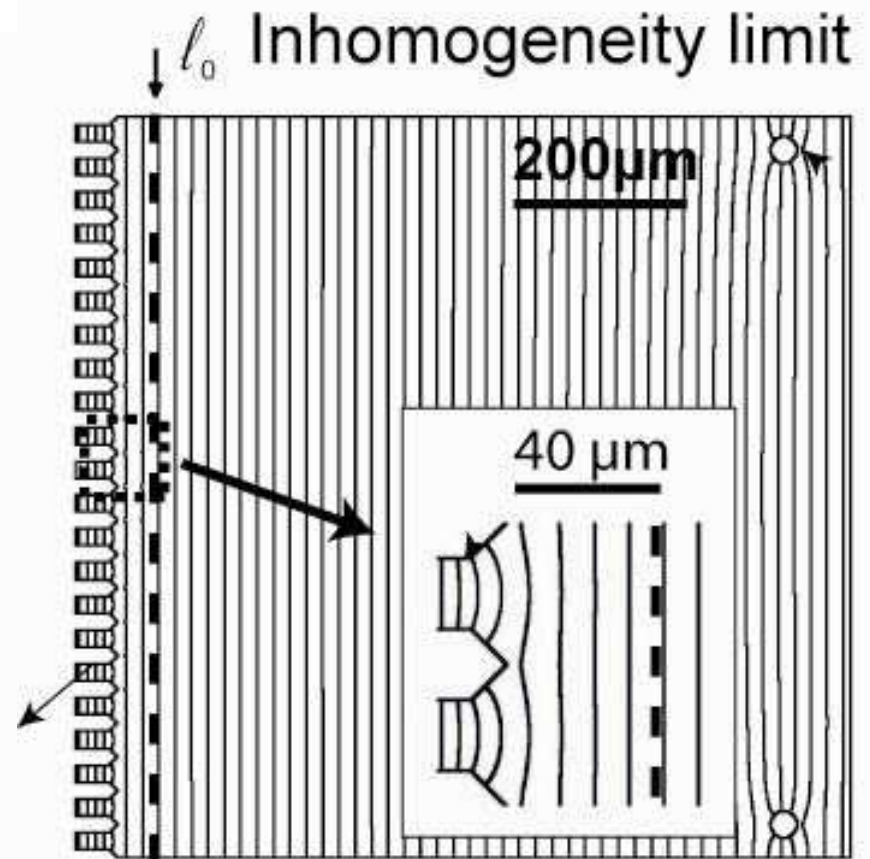
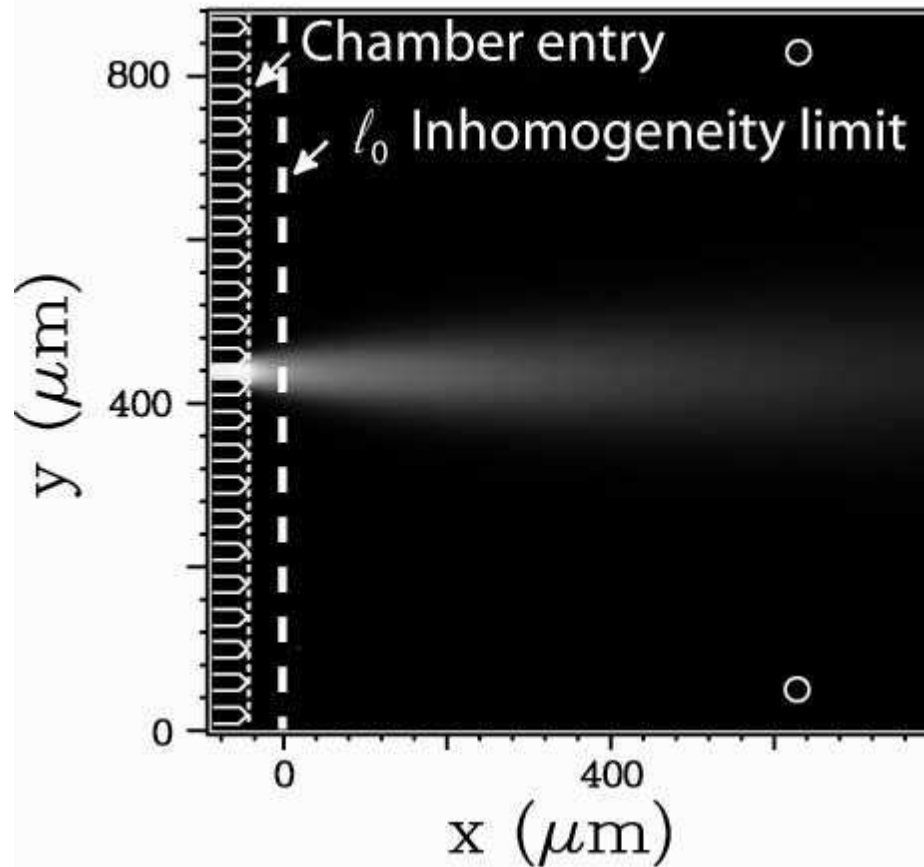
## Velocity field homogeneity

$$\vec{v} = (\mu + \mu_{EO}(x, y, z)) \vec{E}(x, y, z)$$

**Electric field must be uniform**



# Electric field homogeneity

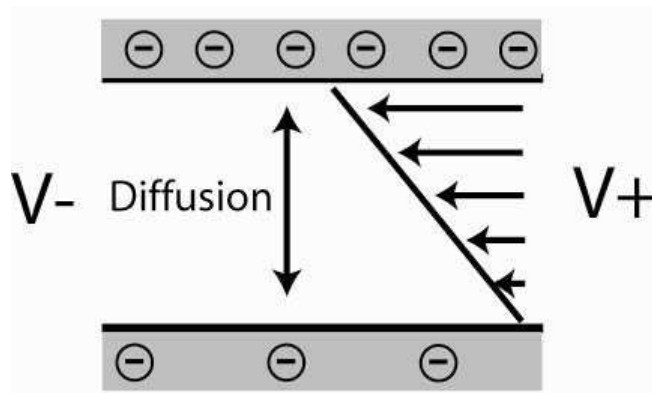


Simulations with Finite Element Methods

# Electroosmosis homogeneity

$$\vec{v} = (\mu + \underbrace{\mu_{EO}(x, y, z)}_{\text{heterogeneous}}) \vec{E}$$

Heterogeneous  
electroosmosis :

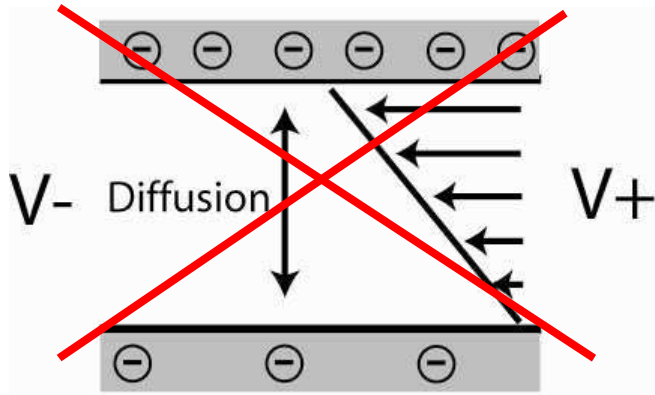


→ Taylor dispersion

# Electroosmosis homogeneity

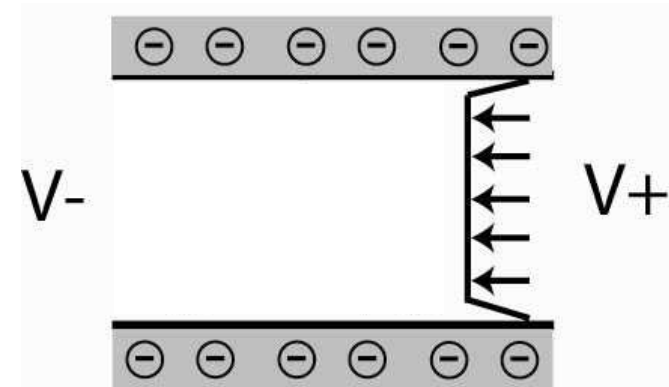
$$\vec{v} = (\mu + \underbrace{\mu_{EO}(x, y, z)}_{\text{heterogeneous}}) \vec{E}$$

Heterogeneous electroosmosis :



→ Taylor dispersion

Homogeneous electroosmosis :



**Electroosmosis must be controlled**

# Electroosmosis control medium

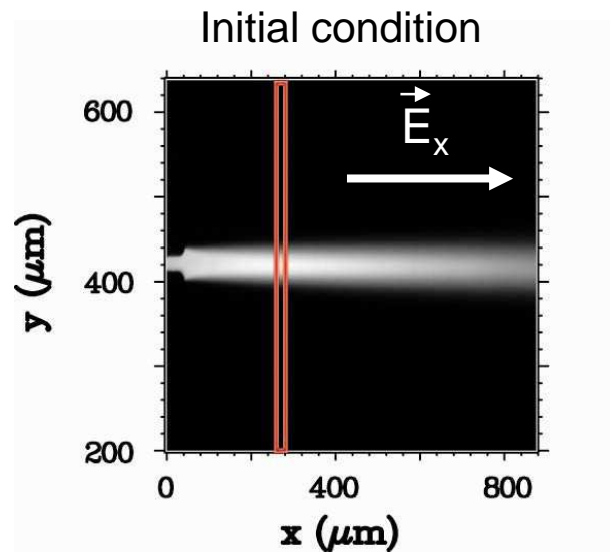
- 1% Agarose
  - Null hydrodynamic flow
  - But limited lifetime of the chip

- 0.1% PDMA (polydimethylacrylamide):
  - Dynamic coating
  - Controlled electroosmosis

**May allow to work  
with uncharged species**

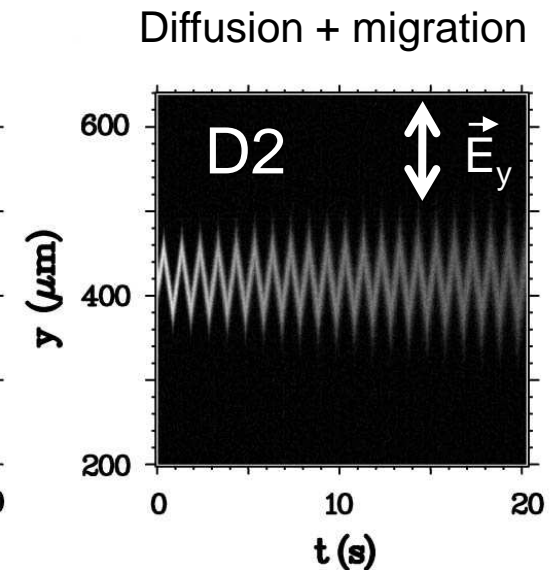
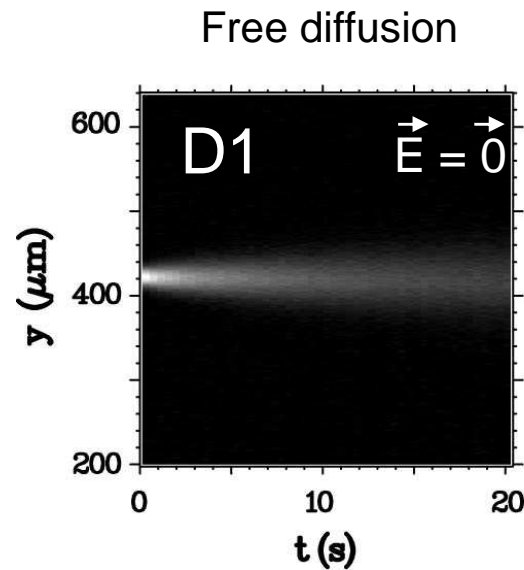
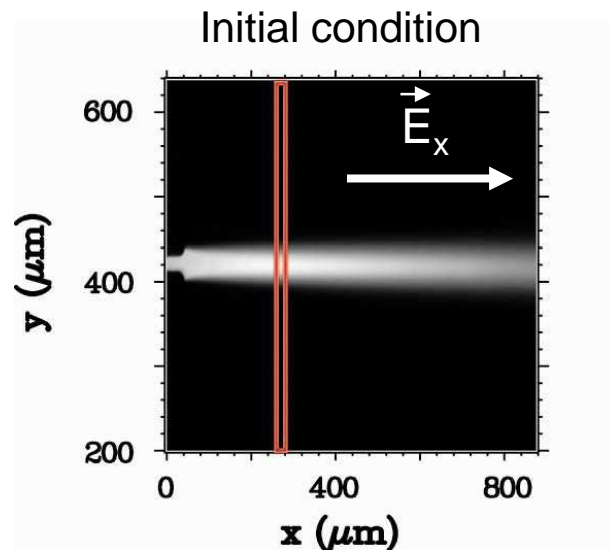
# Taylor dispersion?

We designed a time-based control experiment:



# Taylor dispersion?

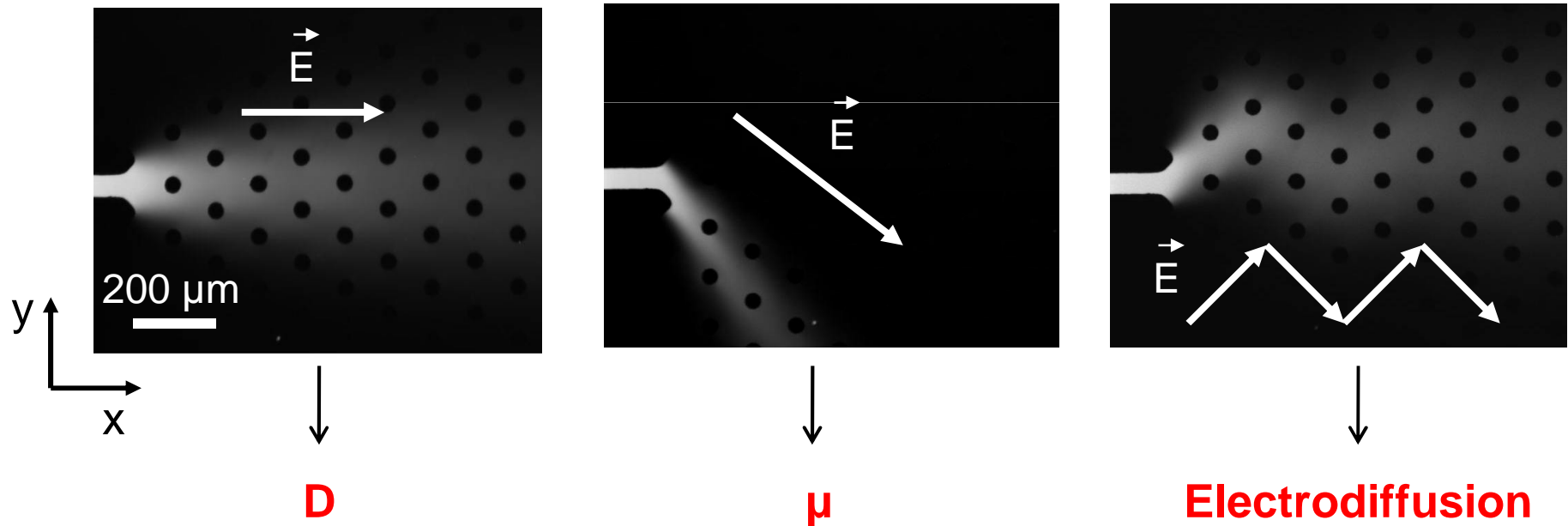
We designed a time-based control experiment:



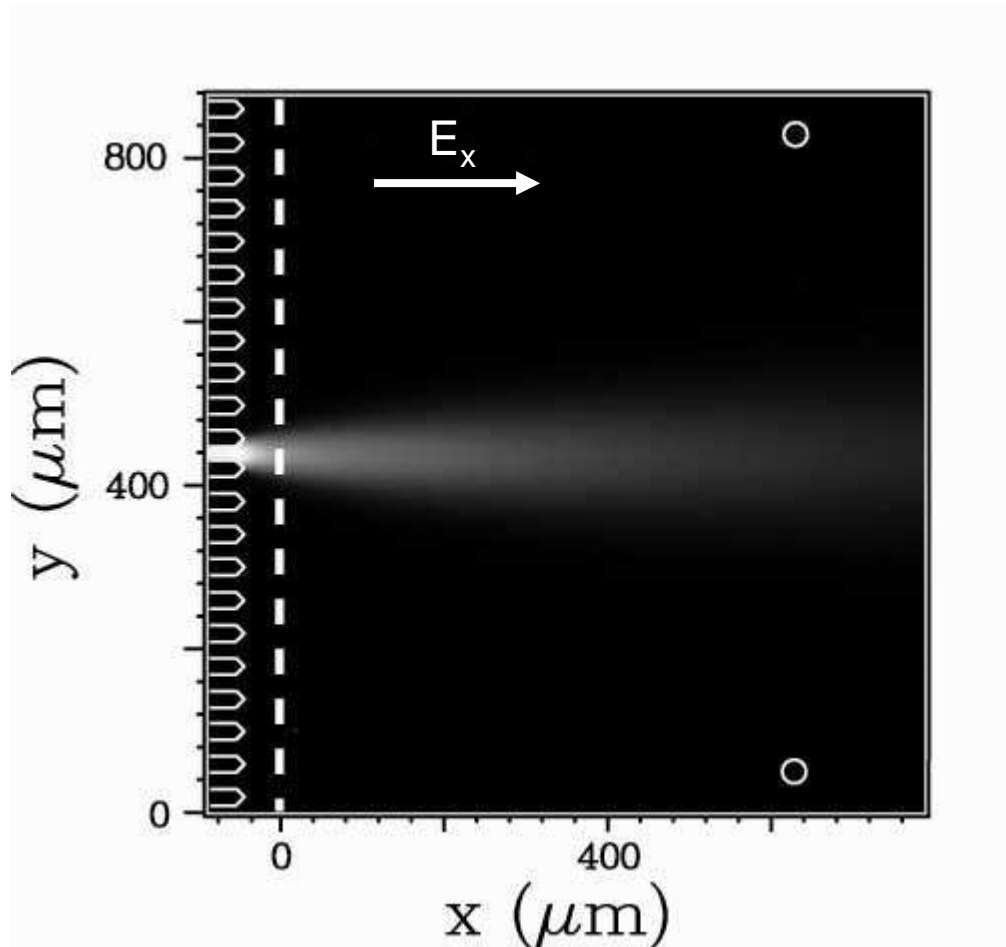
**D1 = D2  $\longrightarrow$  Total absence of Taylor dispersion**

# A functional 2D electrophoresis chip

Constant and alternative electric field in 2D



# Diffusion analysis by Fourier Transform



$$\frac{\partial A}{\partial t} = D \frac{\partial^2 A}{\partial y^2}$$

$$\frac{\partial \tilde{A}}{\partial t} = -D q_n^2 \tilde{A}$$

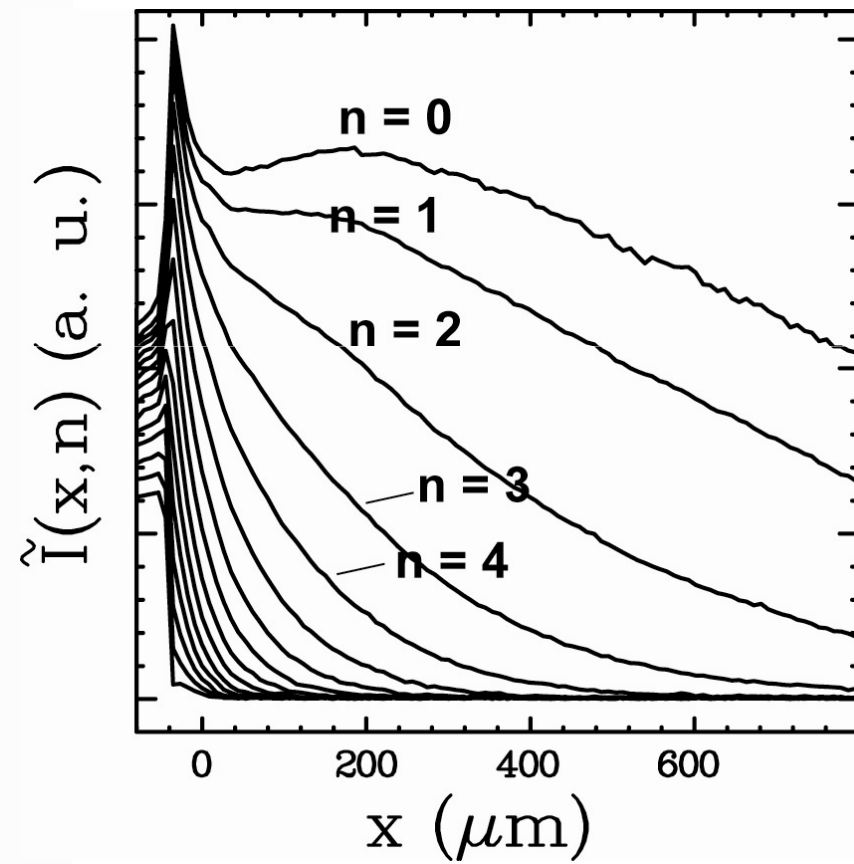
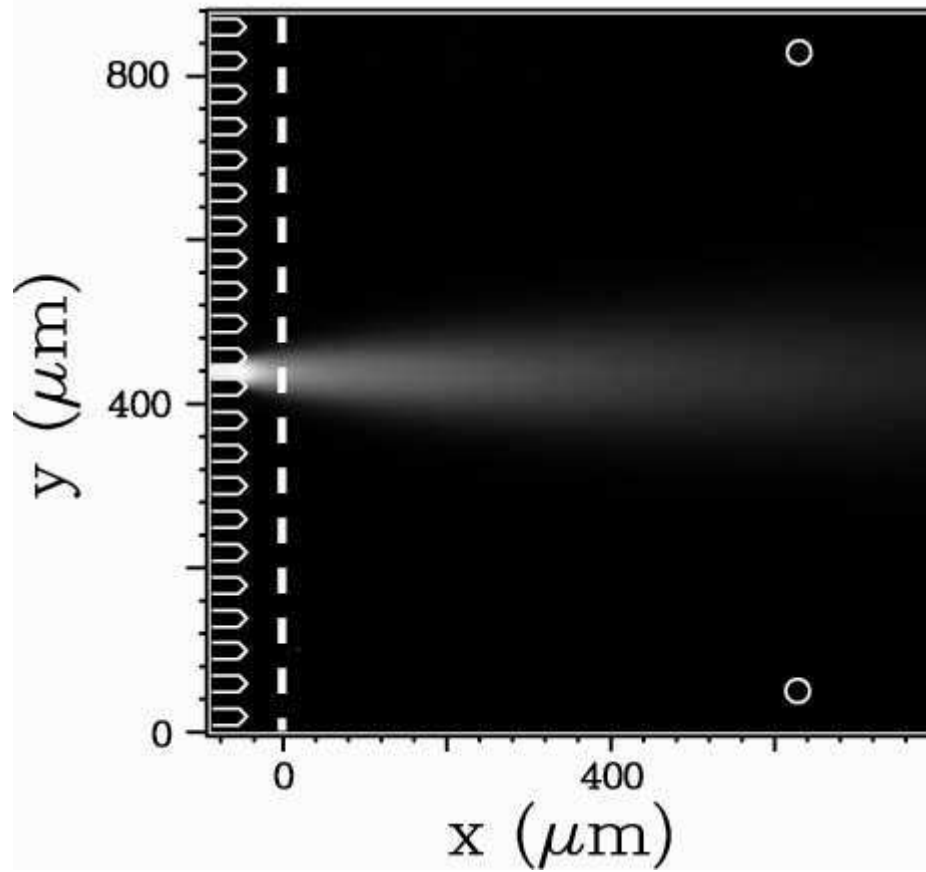
$$\tilde{A} = \tilde{A}_0 e^{-D q_n^2 t}$$

$$\tilde{A} = \tilde{A}_0 e^{-\frac{D}{v_x} q_n^2 x}$$

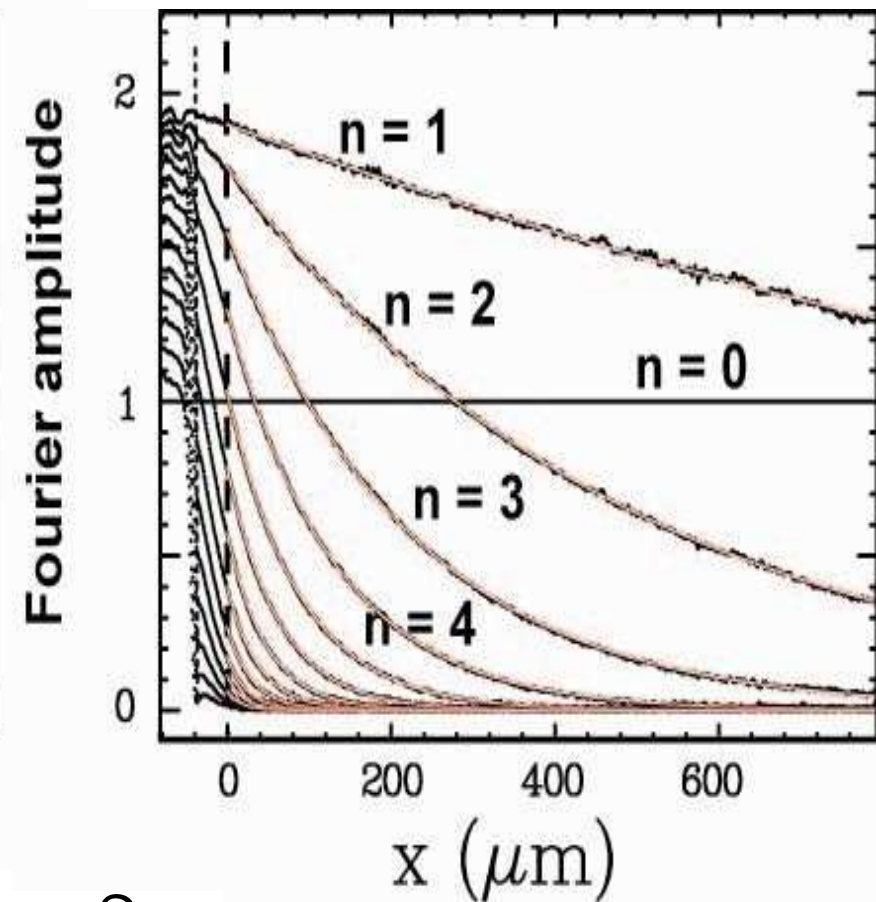
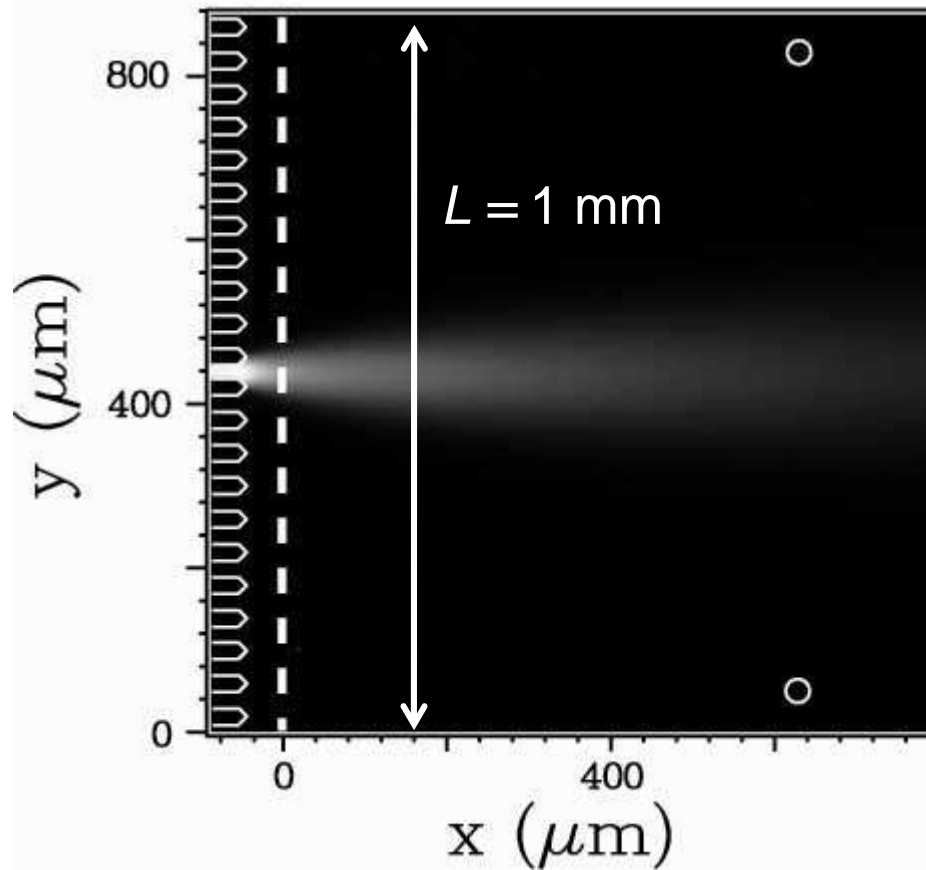
- Independent of initial condition
- Monoexponential fits



## Before illumination correction

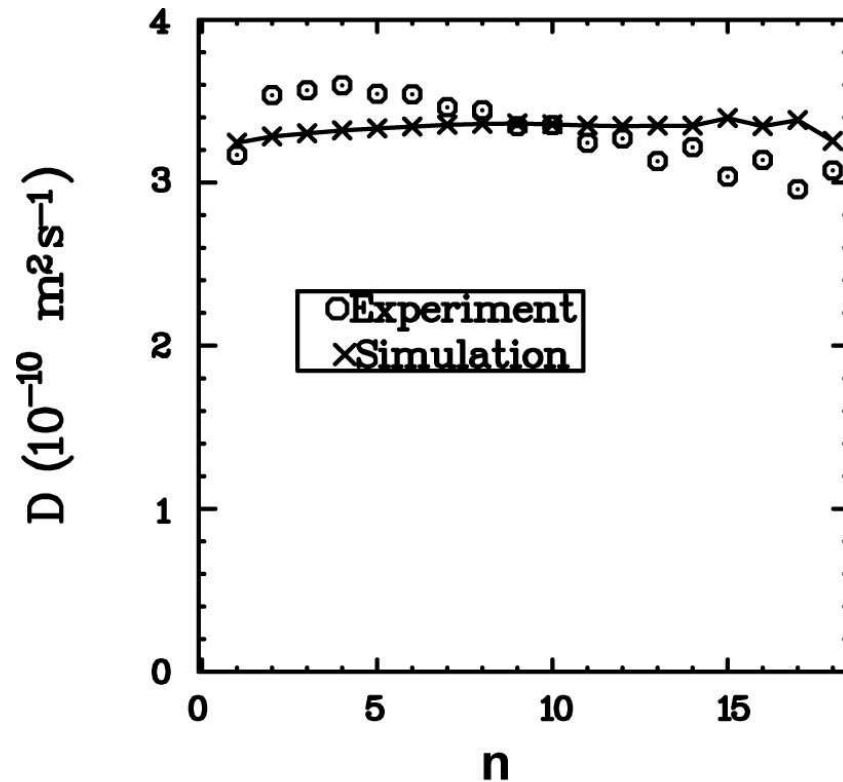


## After illumination correction



spatial frequency  $\longrightarrow q_n = \frac{2\pi n}{L}$   $\longleftarrow$  Fourier mode

## D independent of Fourier mode



Fourier mode is  $[m^{-1}]$

$$q_n = \frac{2\pi n}{L}$$

$n$	$(q_n)^{-1}$ ( $\mu\text{m}$ )
1	140
20	7

**Fourier analysis is multiscale**

## Validation of D measurement

D ( $10^{-12} \text{ m}^2 \text{ s}^{-1}$ )

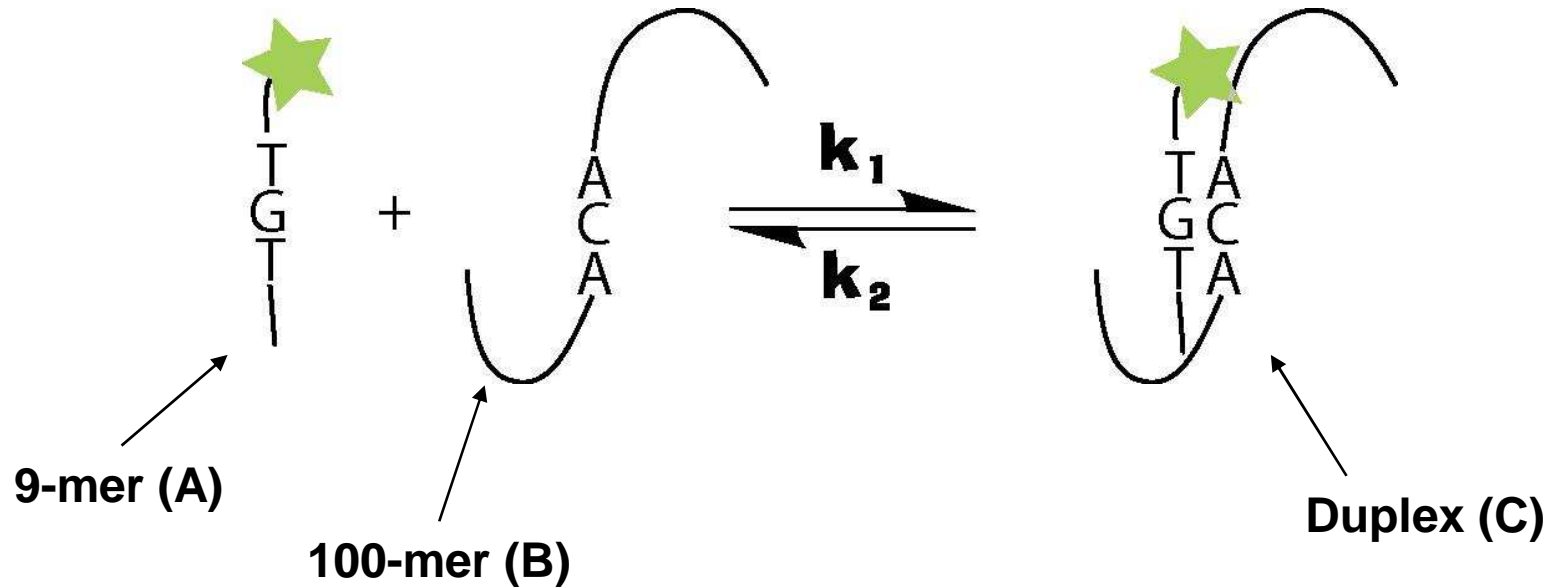
	Fluorescein	ssDNA (105 bases)	dsDNA (1200 bp)
Stationary	$310 \pm 24$	$39 \pm 4$	$3.8 \pm 0.7$
Non-stationary	$320 \pm 20$	$40 \pm 2$	$4.2 \pm 0.3$
FCS	$350 \pm 70$	$44 \pm 5$	—

Large  $M_w$  range:  $10^2$ - $10^6 \text{ g mol}^{-1}$

# Outline

1. DNA hybridization reaction
2. A functional microlaboratory
3. A powerful tool to analyze dynamics

# Dynamics of a reacting mixture

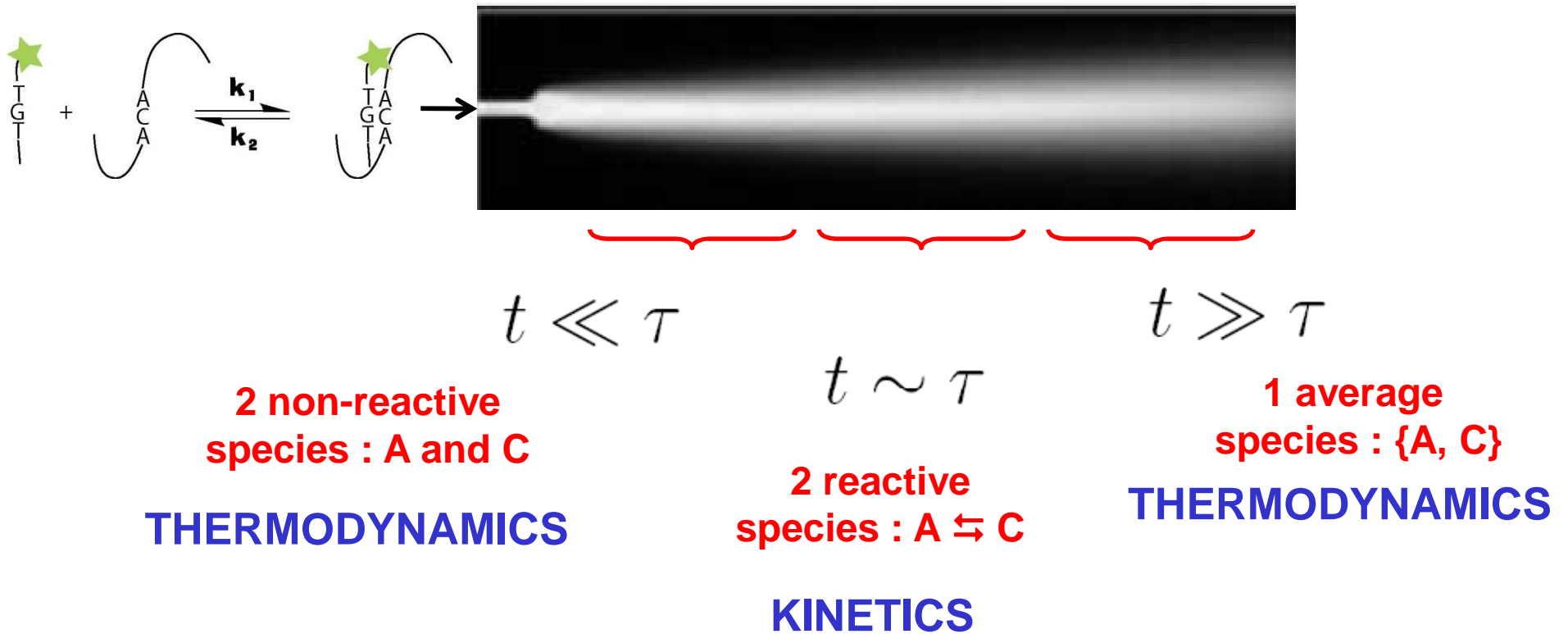


$$\tau = \frac{1}{k_1[B] + k_2}$$

characteristic time  
of the reaction

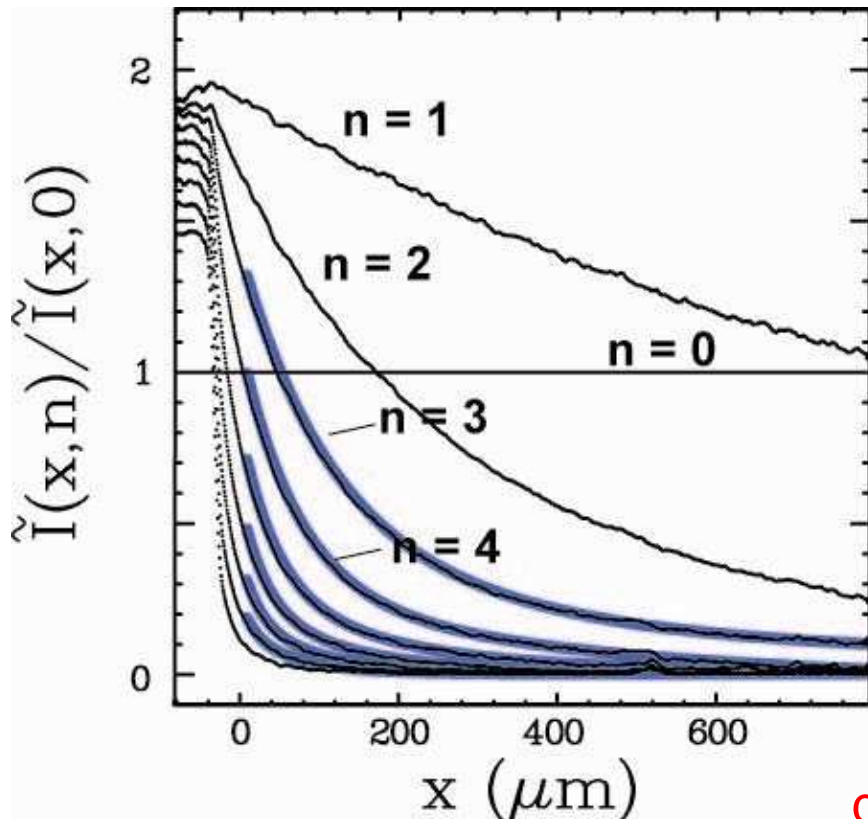
# Finding the good time window

$$t = x/v_x$$



# Analysis of a binary mixture

$$\frac{\tilde{I}(x, n)}{\tilde{I}(x, 0)} = a_1(n)e^{-l_1(n)x} + a_2(n)e^{-l_2(n)x}$$



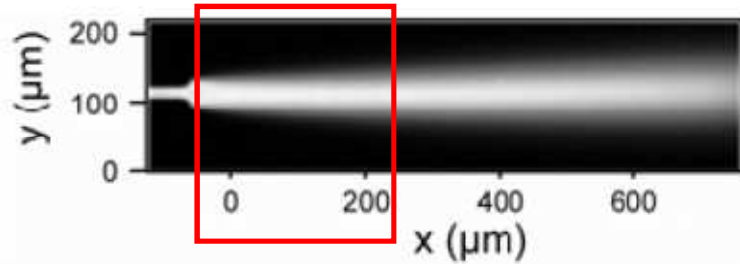
$l_1(n)$   
 $l_2(n)$  } → dynamics  
(diffusion + kinetics)

$a_1(n)$   
 $a_2(n)$  } → concentrations

Fourier analysis + microfluidics  
decouples diffusion/kinetics/concentrations



# Thermodynamic library screening

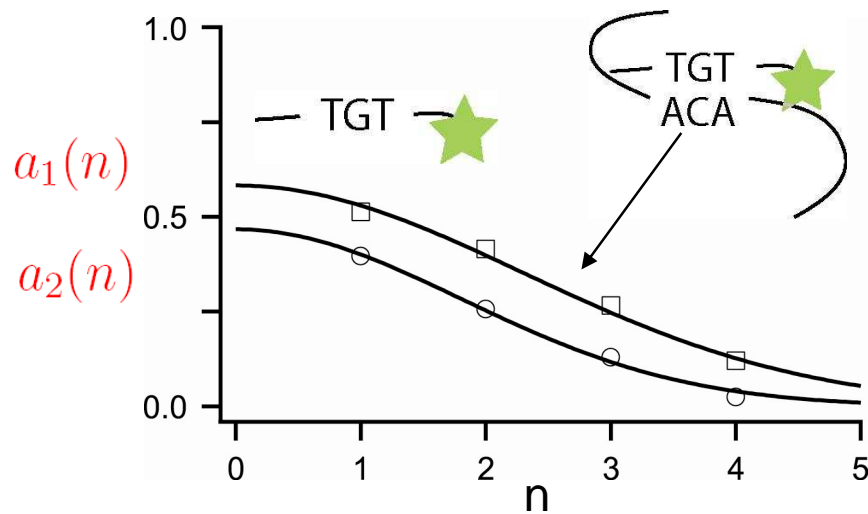


$$t \ll \tau$$

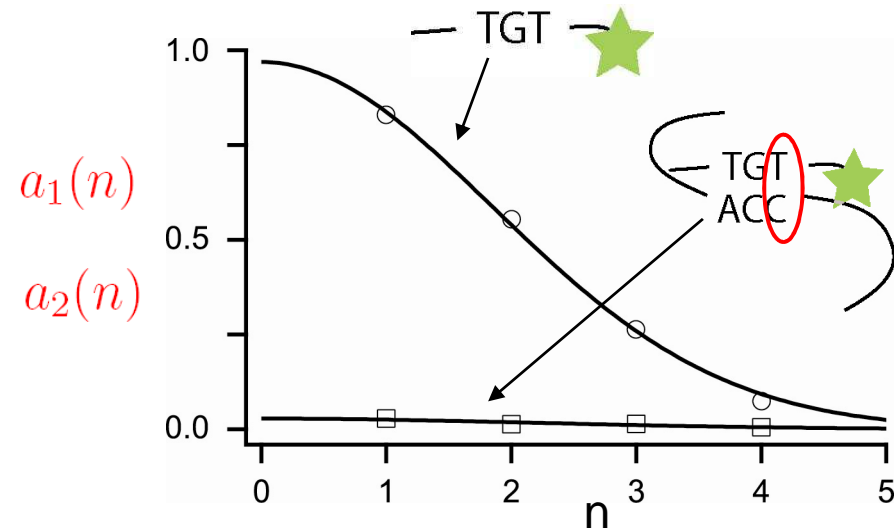
SNP detection

- 20 seconds
- 1 pmol
- Without matrix

Wild type

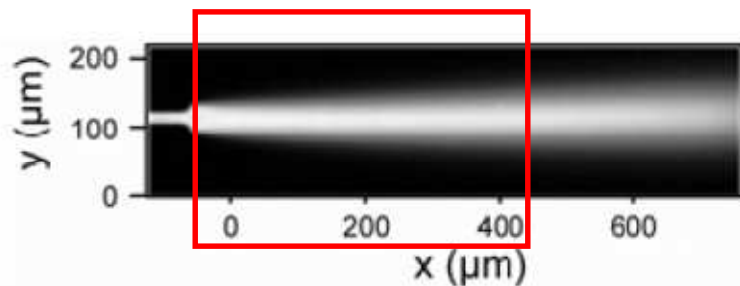


Mutant



Thermodynamic selectivity but very robust observable

# Measuring kinetics



$$t \sim \tau$$

	$k_1$ ( $10^5 \text{ M}^{-1}\text{s}^{-1}$ )	$k_2$ ( $\text{s}^{-1}$ )	$K$ ( $10^5$ )
On chip measurements	$1.2 \pm 0.3$	$0.33 \pm 0.05$	$4 \pm 1$
Independent measurements	$1.9 \pm 0.1$	$0.38 \pm 0.01$	$3.4 \pm 0.6$

Good understanding of the physical phenomenon

# Conclusion

An interesting concept

Electrodifusion

+

A biotechnological issue

SNP detection in DNA

1. A chemical system  
with controllable dynamics

- An oligonucleotide database with controlled  $k_1$ ,  $k_2$
- An easy-to-use mobility reduction strategy (cholesteryl-triton)
- A quadruplex molecular beacon tunes  $k_1$  with sequence

# Conclusion

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Electrodiffusion

+

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SNP detection in DNA

1. A chemical system  
with controllable dynamics

2. A versatile microlaboratory

- Electric fields in 2D
- Thermostated
- Electroosmosis control

# Conclusion

An interesting concept

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+

A biotechnological issue

SNP detection in DNA

1. A chemical system  
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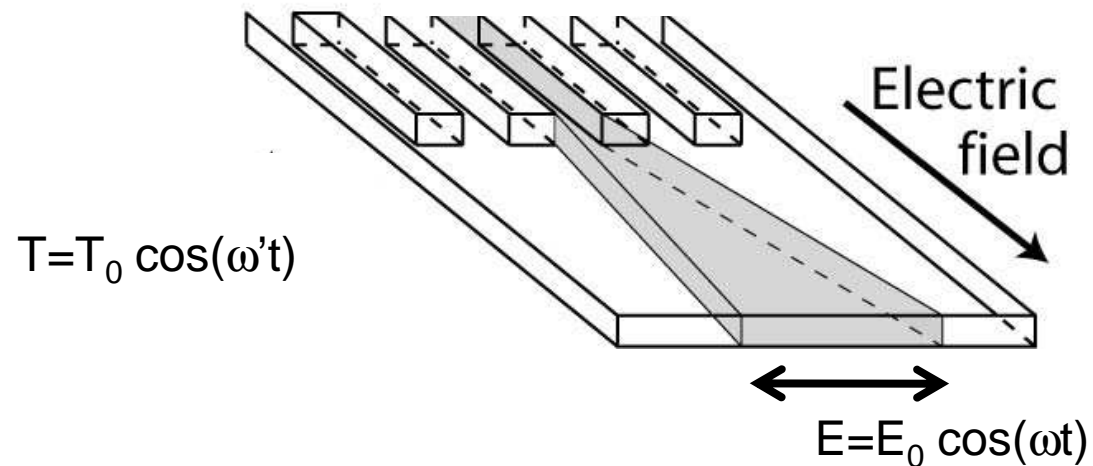
3. A powerful analysis to measure  
dynamics: Fourier transform

- $D$  and  $\mu$

- $k_1$ ,  $k_2$  and  $K$

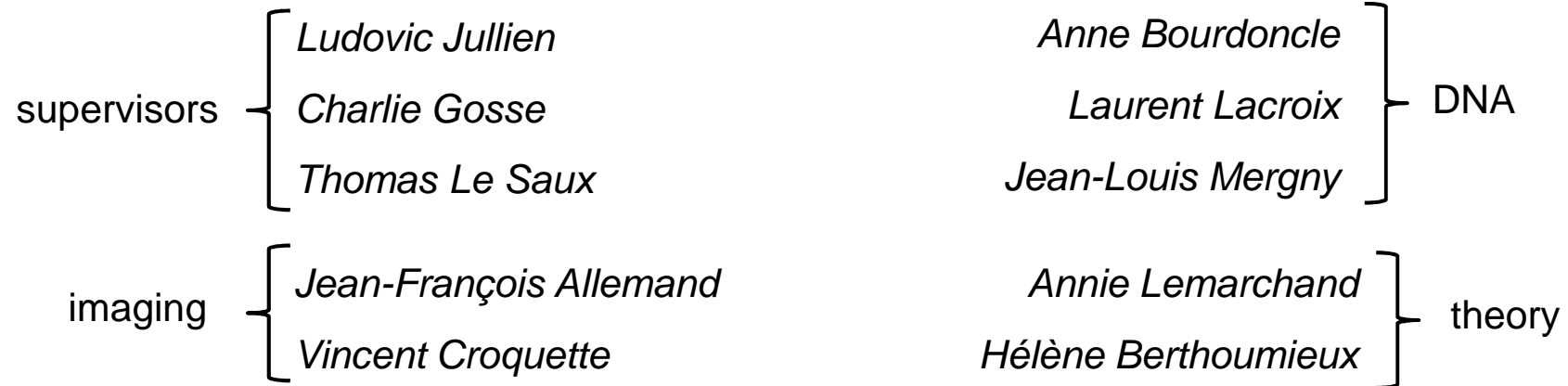
# Perspectives

- Electrodiffusion experiment ready to be performed



- Electric field + temperature modulation  $\longrightarrow$  oriented motion  
(Thomas Barilero)

# Thanks to



*Jonathan Garel*

*Antoine Diguët*

*Sara Fernandez*

*Adrien Georges*

*Jérôme Wong-Ng*

*Didier Chatenay*

*Jacques Goulpeau*

*Jérémy Weber*

*Patrick La Rizza*

*José Quintas da Silva*

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